Quasi-Periodicities Detection Using Phase-Rectified Signal Averaging in EEG Signals as a Depth of Anesthesia Monitor

Quan Liu, Yi-Feng Chen, Shou-Zen Fan, Maysam F. Abbod, and Jiann-Shing Shieh*

Abstract—Phase-rectified signal averaging (PRSA) has been known to be a useful method to detect periodicities in non-stationary biological signals. Determination of quasi-periodicities in electroencephalogram (EEG) is a candidate for quantifying the changes of depth of anesthesia (DOA). In this paper, DOA monitoring capacity of periodicities detected using PRSA were quantified by assessing EEG signals collected from 56 patients during surgery. The method is compared to sample entropy (SampEn), detrended fluctuation analysis (DFA) and permutation entropy (PE). The performance of quasi-periodicities defined by acceleration capacity (AC) and deceleration capacity (DC) was tested using the area under the receiver operating characteristic curve (AUC) and Pearson correlation coefficient. During the surgery, a significant difference ($p < 0.05$) in the quasi-periodicities was observed among three different stages under general anesthesia. There is a larger mean AUC and correlation coefficient of quasi-periodicities compared to SampEn, DFA and PE using expert assessment of conscious level (EACL) and bispectral index (BIS) as the gold standard, respectively. Quasi-periodicities detected using PRSA in EEG signals are powerful monitor of DOA and perform more accurate and robust results compared to SampEn, DFA and PE. The results do provide a valuable reference to researchers in the filed of clinical applications.

Index Terms—depth of anesthesia, electroencephalogram (EEG), phase-rectified signal averaging, quasi-periodicities.

GENERAL anesthesia is an indispensable procedure during surgery to guarantee unconsciousness and total lack of sensation. In preparing for an operation, anesthesiologists are responsible for choosing and determining the optimal combination of anesthetic agents and dosages according to type of surgical procedure and the particular patient. To ensure patients’ safety and a successful procedure, anesthetists need to adjust the dosage of anesthetics and sedatives based on patients’ hypnotic state to avoid overdosing, and underdosing. Short et al. [1] have designed a balanced anesthesia study to determine whether causality exists between relatively deep anesthesia and the increased postoperative mortality. Several evidences indicate that excessive anesthetic due to overdosing can contribute to a potential hazardous despite a controversy over association with postoperative mortality [2-5], and inadequate anesthesia because of underdosing may cause intraoperative awareness and further lead to a potential incidence of postoperative psychosomatic dysfunction [6, 7]. Therefore, a reliable monitor to trace the change of anesthetic drug effects and determine depth of anesthesia (DOA) can help anesthesiologists to maintain adequate anesthesia with minimal agents.

Unfortunately, the biochemical mechanism of action of general anesthesia are still poorly understood [8, 9], and scientific definition of consciousness have not been accepted, thus is difficult to measure. Therefore, a golden standard directly associated with consciousness level for measurement of DOA remains not yet available [10]. To induce unconsciousness, anesthetic drugs act on myriad sites in the central nervous system (CNS) include the brain and spinal cord. The brain is the major functional unit of the central nervous system [11] which produce electroencephalogram (EEG) which reflects electrical activity of the brain. EEG have been widely used to determine the DOA [10, 12, 13].

Currently, commercially EEG-based monitors mainly contain bispectral index (BIS) [14], Entropy index [15], patient state index [16] and Narcotrend index [17]. These monitors provide a single dimension index ranged from 0 (EEG silence) to 100 (awake) to indicate the DOA. The BIS, most popular used in the hospital, is a complex parameter derived from analysis in time domain, frequency domain and high order statistics [14]. Entropy monitoring, developed by Datex-Ohmeda, evaluates the complexity in EEG signals based on spectral entropy and provide two parameters (RE-Response
Entropy, SE-State Entropy) associated with different frequency components [15]. In the patient state index, EEG power, frequency and phase information reflecting different dimensions of brain electrical activity are weighted combined to obtain a complex indicator [16]. Narcotrend uses a multivariate analysis algorithm to extract numerous quantitative features such as spectral parameters, entropy measures and autoregressive parameters from the time and the frequency domain in EEG [17]. However, the reliability of these monitors have been questioned in some special cases. BIS is insensitive to some commonly used drugs in general anesthesia such as ketamine and nitrous oxide [18, 19] and sensitive to artifacts [20]. In addition, its technology leads to a large time delay in the detection of the different stages of anesthesia [21]. The spectral entropy in entropy monitoring is calculated mainly in the frequency domain based on the power spectrum of the EEG using Fast Fourier Transformation (FFT). FFT as a linear algorithm is usually suitable for linear and stationary signals, but it cannot clearly reflect dynamic behavior in nonlinear and non-stationary EEG. Furthermore, Narcotrend does not have the ability to differentiate reliably between awareness and unconsciousness in the challenging data set from loss and return of consciousness [22], hence Narcotrend monitor ability to differentiate consciousness from unconsciousness for some agents is seriously doubted [23].

Recently, due to the nonlinear and non-stationary characteristics of EEG signals, sophisticated nonlinear dynamical approaches have been proposed to measure the DOA. Complexity measurement in EEG such as Lempel-Ziv complexity (LZC), approximate entropy (ApEn), sample entropy (SampEn), and permutation entropy (PE) provided a novel trend in the development of DOA monitoring [24, 25]. Detrended fluctuation analysis (DFA) has also been introduced to assess the scaling behavior in EEG as a measure of DOA [26, 27]. Nguyen-Ky et al. proposed a new method called wavelet-based depth of anesthesia (WDOA) index based on discrete wavelet transform (DWT) in 2011 [13] and then applied statistical method based on Bayesian techniques to analyze EEG signals for consciousness and DOA assessment in 2012 [28]. Hayashi et al. used SD1/SD2 ratio based on Poincaré plot to study dynamical changes of EEG induced by anesthesia in the state-space trajectory [29]. Furthermore, recurrence quantification analysis [30] and dimensionality reduction method [31] were also used to assess the depth of anesthesia.

In this paper, a technique called phase-rectified signal averaging (PRSA) is introduced to detect the quasi-periodicities in EEG for the assessment of DOA. PRSA was originally proposed by Bauer et al. to study quasi-periodic oscillations in noisy, non-stationary signals [32] and have been widely applied to analyzing heart rate variability (HRV) [33-35]. This is the first time PRSA is used to study the quasi-periodicities in EEG as a measure of DOA. In human being, CNS continuously receives internal regulations and noxious stimuli under the control of brain and processing this information to determine the correct response and then sending the information to body. During general anesthesia, the loops are interrupted or changed causing anesthesia induced unconsciousness [36, 37]. Quasiperiodic oscillations in EEG reflect regulation processes of the CNS. The EEG originating from multiple regions of the brain such as cerebral cortex and thalamus is of high complexity and always contaminated by artifacts. While PRSA has advantages in the analysis of nonlinear and non-stationary signals over conventional spectral methods and can eliminating artifacts or noise. Furthermore, PRSA provides a way to analyze periodic behavior that is related to acceleration and deceleration in EEG during anesthesia, which offers a possibility for anesthesia monitoring. In the present study, the acceleration capacity (AC) and deceleration capacity (DC) of EEG signals are quantified for monitoring the DOA. The results are compared to the gold standard indicator decided by five experienced anesthesiologists known as expert assessment of conscious level (EACL) [38, 39] and bispectral index (BIS) [39].

II. MATERIALS AND METHODS

A. Data Sources

A single channel raw EEG data and BIS were collected from 56 ASA physical status I-III patients (age 18-75 years) during surgery in operation room using the MP60 system (Philip, Intellivue MP60 BIS module). The patients are undergoing ear, nose, and throat (ENT) surgery at the National Taiwan University Hospital (NTUH) of Taiwan. Normally, EEG recording begins before surgery starts and ends after patient’s awareness recovery. Before starting the drug administration, all patients were awake and had awareness. Then they all received propofol and fentanyl for induction of anesthesia. Muscle relaxants were also administered at the discretion of the anesthesiologist.

Sevoflurane, desflurane and propofol were administered individually by an anesthesiologist for maintenance of anesthesia. The corresponding anesthetic technique are sevoflurane for endotracheal intubation for 11 patients, desflurane for endotracheal intubation for 13 patients, sevoflurane for laryngeal mask airway (LMA) for 16 patients, desflurane for laryngeal mask airway (LMA) of 4 patients, and propofol for total intravenous anesthesia of 12 patients, respectively. At the end of surgery, sevoflurane, desflurane and propofol were discontinued. Then the patients were asked to be wakened from anesthesia state. The sampling rate of EEG is 125 Hz and the BIS is 0.2 Hz. The present research received the approval of Institutional Review Board at NTUH of Taiwan. Written informed consents were obtained from the 56 patients.

B. Expert Assessment of Conscious Level

Expert assessments of conscious level (EACL) are derived from five experienced anesthesiologists from NTUH in Taiwan to trace patients’ state of anesthetic depth [38, 39]. During the whole duration of the surgery, two nurses continuously observed the patients’ state and recorded the vital signs possibly associated with drug effects on patients. The operation type, clinical indices include blood pressure, heart rate and SpO2, the detailed information of operation events happened during surgery such as induction, extubation and drugs administration, the type of anesthetics and their dose, and MAC values were all recorded on the operation record during the whole period of anesthesia. The age, weight, height, gender and medical history of patients were also recorded. The anesthesiologists took the record into consideration and made their own decision independently based on their previous experiences to plot the state of anesthetic depth of patients.
between 0 (i.e., EEG silence) and 100 (i.e., awake) consisting with commonly used monitors. Other continuous signs were digitized at a sample rate of 0.2 Hz such as BIS. Each person of the five anesthesiologists can provide different value for the state of anesthesia depth at the same time, therefore, the mean value was obtained from the five EACL decided by anesthesiologists for increasing reliability and accuracy. Because these selected five doctors have worked as anesthesiologists for many years, the EACL are reliable and can be used to as a real gold standard for the recognition of different anesthesia states of patients. Fig. 1 shows an example of EACL from five doctors and their mean and standard deviation.

C. Phase-Rectified Signal Averaging

Phase-rectified signal averaging (PRSA) is a recently introduced signal processing technique to analyze non-stationary and nonlinear time series contaminated by noise or artifacts [32]. It has been widely used for analysis of acceleration capacity (AC) and deceleration capacity (DC) of heart rate [33]. In this paper, PRSA is used on EEG signals to detect the quasi-periodicities by deceleration capacity and acceleration capacity. Fig. 2 provides a detailed interpretation of PRSA for studying EEG. Firstly the maxima and minima in EEG segments are detected and transferred the EEG data to calculate the maximum-to-maximum or minimum-to-minimum
interval (MMI) which is the time interval between successive maxima or minima. Fig. 2(a) shows the maxima and minima detection and MMI definition. Fig. 2(b) shows the MMI sequences extracted from EEG. For AC calculation, the increased points in MMI sequences are selected as anchors (i.e., \( v_1, v_2, \ldots, v_n \)) as shown in Fig. 2(b). The decreased points in MMI sequences are selected for DC calculation. Surroundings of window length 2L around the anchor points are selected and L is set to be 10 in Fig. 2(c), then the extracted surroundings are aligned at the anchor points. The PRSA curve is derived from averaging over all aligned surroundings as shown in Fig. 2(d) marked with red line. Finally, the AD and DC are quantified as follows:

\[
AC(DC) = \frac{X_0 + X_1 - X_2 - X_3}{4}
\]  

where \( X_1 \) is the average of MMI at all anchor points, \( X_2 \) is the following point adjacent to \( X_0 \) in PRSA curve, \( X_3 \) and \( X_4 \) are preceding points adjacent to \( X_3 \) as shown in Fig. 2(e).

Mathematically, the quantification of AC and DC is based wavelet transform associated with the Haar wavelet defined as (2) [32]. The discrete wavelet transform applied to PRSA signal at time scale \( s \) and position \( p \) is generally expressed with (3) [32]. It captures both frequency and location information, and the wavelet coefficients along time scale \( s \) indicate the characteristics of periodicities or frequencies in the signals. Actually, the AC and DC are central wavelet amplitude \( x_s(2,0) \) calculated using Haar wavelet analysis where \( s = 2 \) and \( p = 0 \). Hence, they carry the time scales information of the periodicities in the PRSA signal. In the procedure of PRSA, non-periodic components are cancel out due to the averaging of all aligned surroundings around the anchor points, thus this calculation is robust to noise or artifacts and can be applied to extract information about the quasi-periodicities from complex signals which may be non-stationary and noisy.

\[
\phi(t) = \begin{cases} 
1 & 0 \leq t < 1 \\
-1 & -1 \leq t < 0 \\
0 & \text{otherwise}
\end{cases}
\]  

\[
x_s(s, p) = \sum_{k,s} x_s(k-p)/s
\]  

D. EMD/MEMD based Filter

Generally, EEG records electrical signals from activity of the brain along the scalp and almost always contaminated by biological and environmental artifacts, such as EOG, EMG, power line interference and baseline drift and so on. And the amplitude of artifacts can be highly larger than the signals of interest. Therefore, it is necessary to remove them from EEG before analysis for the purpose of accuracy. Empirical mode decomposition (EMD) introduced by Huang et al. [40] has been widely used in analysis of non-stationary and nonlinear signals. EMD decomposes the original signals into finite components called intrinsic mode functions (IMFs) from high to low frequency adaptively by a sifting process given by:

\[
x(t) = \sum_{i} IMF_i(t) + r_n(t)
\]

where \( x(t) \) is the original signal, \( N \) is the total number of IMFs, \( IMF_i(t) \) is the \( i \)th component, and \( r_n(t) \) is the residual. Then, the filtered signal \( \hat{x}(t) \) can be reconstructed using selected IMFs dominated by signal of interest [41, 42], as follows:

\[
\hat{x}(t) = \sum_{i=p}^{q} IMF_i(t) \quad (1 \leq p \leq q \leq N)
\]

or

\[
\hat{x}(t) = \sum_{i=p}^{q} IMF_i(t) + \sum_{i=q+1}^{N} IMF_i(t) \quad (1 \leq p \leq q \leq N)
\]

Multivariate empirical mode decomposition (MEMD) as an improved algorithm of EMD was proposed to decompose multichannel signals [43, 44]. In order to solve the mode mixing problem, MEMD was applied in this study to decompose a three channel signal consisting of one channel EEG and two channels independent white noise. Then the IMFs corresponding to EEG channel are extracted. According to previous researches, the authors [39, 45, 46] set \( p = 2, q = 3 \) to reconstruct the filtered EEG signals. Therefore, \( IMF_2(t) \) and \( IMF_3(t) \) were selected as the filtered EEG in this paper.

E. Statistical Analyses

To assess the performance of proposed quasi-periodicities quantification by AC and DC in EEG for DOA measurement, statistical analyses were used. Firstly, two-tailed Student’s \( t \)-tests were performed to indicate whether there is a significant difference to distinguish different anesthesia states. Then AC and DC were compared with EACL and BIS, respectively. The Pearson correlation coefficient was applied to assess the correlation between AC (DC) and EACL and BIS, respectively. This was used to evaluate the ability of AC and DC to track the changes of patients’ state undergoing anesthesia. In addition, receiver operating characteristic (ROC) analysis was used and area under the receiver operating characteristic curve (AUC) of AC and DC was calculated to illustrate their performance to monitor DOA. The two-tailed Student’s \( t \)-tests and ROC analysis were performed in SPSS (v19, SPSS Inc.; Chicago, IL, USA). The level of statistical significance was set at \( p < 0.05 \).

The whole diagram for monitoring the DOA based on the proposed method is shown in Fig. 3. The raw EEG signal is firstly filtered using MEMD method. Then the signal is reconstructed by summing up IMF2 and IMF3 as the filtered signal [39]. After that the AC and DC indices are extracted based on PRSA method from the signal to assess the DOA. The values of AC and DC have different scales from EACL and BIS, therefore, both of them are converted to the same scale as EACL and BIS via an artificial neural network (ANN). The output of ANN is used to monitor the DOA. The ANN topology is 1-20-1 neurons for the input layer, hidden layer and output layer respectively. The network is feed-forward back-propagation type. Each of the parameters including AC and DC was used as input and EACL or BIS was used as target data, respectively to train, validate and test the ANN model. The samples percentages divided randomly for training, validation, and testing are 70%, 15%, and 15%, respectively. The training data set is firstly used to train the neural network. During training, current values of the weights and biases are applied to the validation data set and the error on the validation set is monitored to avoid model overfitting. The test data is not used at all during the training process. After training completes, the accuracy of the resulting neural network model’s weights...
and biases are applied to the test data. The ANN network was implemented in MATLAB (v7.13, MathWorks, Inc., USA).

Anesthesia is conducted and they totally lose their consciousness. Anesthesia must be continuously maintained in order to avoid recovery of consciousness until the operation is finished. After the operation, the concentration of administered agent drops, patients recover their awareness and consciousness.

First, the behavior of AC and DC to distinguish the states under different anesthesia stages is investigated. Fig. 4 presents the acceleration and deceleration-related PRSA signals of MMI of EEG recording in a patient under stage 1, stage 2 and stage 3 from top to bottom, respectively. All oscillations are in phase at the anchor point, thus AC and DC are the sum of the all periodic oscillations corresponding to acceleration and deceleration. In this patient, AC and DC provide a clear index to indicate the DOA under three different stages, and the absolute values of both AC and DC are largest in the middle line (i.e., stage 2) when the patient is under anesthesia without awareness and consciousness. Both AC and DC calculated from maximum-to-maximum or minimum-to-minimum interval of EEG recording are substantially symmetric and correspond in absolute value.

The statistical distribution of AC and DC for each stage from 56 patients undergoing general anesthesia is presented in Fig. 5. It can be seen that the absolute values of both AC and DC clearly increase from stage 1 to stage 2, and then decrease from stage 2 to stage 3. They increase when patients lose their awareness and consciousness and decrease with recovery.

In general, the general anesthesia can be divided into pre-operation (i.e., stage 1), induction and maintenance (i.e., stage 2) and recovery (i.e., stage 3) during the whole surgical procedure. Patients are awake and keep a high consciousness level during the pre-operation. Then induction of general anesthesia is conducted and they totally lose their consciousness. Anesthesia must be continuously maintained in order to avoid recovery of consciousness until the operation is finished. After the operation, the concentration of administered agent drops, patients recover their awareness and consciousness.

First, the behavior of AC and DC to distinguish the states under different anesthesia stages is investigated. Fig. 4 presents the acceleration and deceleration-related PRSA signals of MMI of EEG recording in a patient under stage 1, stage 2 and stage 3 from top to bottom, respectively. All oscillations are in phase at the anchor point, thus AC and DC are the sum of the all periodic oscillations corresponding to acceleration and deceleration. In this patient, AC and DC provide a clear index to indicate the DOA under three different stages, and the absolute values of both AC and DC are largest in the middle line (i.e., stage 2) when the patient is under anesthesia without awareness and consciousness. Both AC and DC calculated from maximum-to-maximum or minimum-to-minimum interval of EEG recording are substantially symmetric and correspond in absolute value.

The statistical distribution of AC and DC for each stage from 56 patients undergoing general anesthesia is presented in Fig. 5. It can be seen that the absolute values of both AC and DC clearly increase from stage 1 to stage 2, and then decrease from stage 2 to stage 3. They increase when patients lose their awareness and consciousness and decrease with recovery.
Fig. 5. Box plots of AC and DC at different anesthesia stages from 56 patients undergoing general anesthesia during surgery at NTUH of Taiwan. The edges of the box are the 25th and 75th percentiles. (a) and (b) are the results of acceleration and deceleration-related PRSA signals of maximum-to-maximum interval of EEG recording, (c) and (d) are the results of acceleration and deceleration-related PRSA signals of minimum-to-minimum interval of EEG recording. The two-tailed Student’s t-tests are used to indicate the significant difference between two different stages. Those giving p-value lower that 0.05 are marked with asterisk (*).

Fig. 6. An example of DOA measures against time for a patient undergoing general anesthesia during the whole surgery. (a) The real gold standard from five experienced anesthesiologists (i.e., EACL) and the most commonly used commercial monitor (i.e., BIS). (b) Acceleration capacity (AC) of maximum-to-maximum and minimum-to-minimum interval. (c) Deceleration capacity (DC) of maximum-to-maximum and minimum-to-minimum interval.
Capacity of AC and DC for Tracing the Consciousness Level during Surgery

In this section, PRSA is used to trace the consciousness level of 56 patients undergoing general anesthesia during surgery. The AC and DC indicators are compared with a real gold standard from five experienced anesthesiologists (i.e., EACL) and the most commonly used commercial monitor (i.e., BIS) for monitoring changes in anesthesia states of patients. Because EACL and BIS are sampled at 0.2 Hz and the sampling rate of EEG data is 125 Hz, therefore a fixed-size sliding window moving once every 5 s with 625 points was used, and the window size was set to be 3750 data points with duration of 30s according to our previous studies [39, 46]. An example of anesthesia state monitoring of one patient undergoing general anesthesia during surgery is shown in Fig. 6. AC values which are inverse to EACL and BIS trend increase with losing awareness and consciousness under anesthesia of the patient, and then decrease during recovery when the anesthesia states is getting lighter. Larger AC values indicate deeper anesthesia level. On the contrary, the DC values consisting with EACL and BIS trend changes from high values to low values when patient’s states change from awake to anesthesia.

The performance of the proposed method was compared with other existing algorithms, such as sample entropy (SampEn), detrended fluctuation analysis (DFA) [27] and permutation entropy (PE) [25, 47]. The detailed algorithms and parameters selection of SampEn and PE were illustrated in our previous study [46]. In calculation of SampEn, the value of embedding dimension $m$ is set to 2 and the value of tolerance $r$ is set to $0.2 \times std$, where $std$ stands for standard deviation. The DFA is calculated according to the illustration in [27].

To evaluate the performance of the proposed method for tracing the DOA, ROC analysis is carried out. AUC is a commonly used measure in medical diagnosis referred to as the discrimination. EACL and BIS were used to determine the anesthesia and awake states. In general, the BIS value ranged from 40 to 60 indicates an appropriate anesthesia level during surgery, thus the threshold to identify anesthesia state is set to be 60. The value of EACL and BIS below 60 is defined as anesthesia state and value above 60 is defined as awake state. Fig. 7 shows a graphical plot of ROC that illustrates the performance of AC, DC, SampEn, DFA and PE for anesthesia discrimination. The best classification has the largest AUC. The AUC of AC and DC is larger than that of SampEn, DFA and PE. The SampEn yields the lowest AUC. This result suggests that classification based on both AC and DC has an improved predictive power in discriminating awake state from anesthesia state in comparison with SampEn, DFA and PE. The mean and standard deviation values of AUC of AC, DC, SampEn, DFA and PE from 56 patients are shown in TABLE I. The AC and DC have a high discrimination of the difference between anesthesia state and awake state. The mean values of AUC of AC and DC are significantly larger than that of SampEn, DFA and PE ($p < 0.05$) before and after regression via ANN.

Furthermore, Pearson correlation coefficient between AC, DC, SampEn, DFA and PE from 56 patients were calculated to test their performance using EACL and BIS as gold standard. Those giving $P$-value lower that 0.05 of difference from SampEn, DFA and PE are marked with asterisk (*), dagger (†) and double dagger (‡), respectively.

### TABLE I

<table>
<thead>
<tr>
<th>Without ANN</th>
<th>MAXI_AC</th>
<th>MAXI_DC</th>
<th>MINI_AC</th>
<th>MINI_DC</th>
<th>SampEn</th>
<th>DFA</th>
<th>PE</th>
</tr>
</thead>
<tbody>
<tr>
<td>vs. EACL</td>
<td>0.90(0.07) *†‡</td>
<td>0.90(0.08) *†‡</td>
<td>0.90(0.08) *†‡</td>
<td>0.89(0.08) *†‡</td>
<td>0.49(0.19)</td>
<td>0.70(0.21)</td>
<td>0.81(0.16)</td>
</tr>
<tr>
<td>vs. BIS</td>
<td>0.90(0.08) *†‡</td>
<td>0.91(0.07) *†‡</td>
<td>0.91(0.07) *†‡</td>
<td>0.91(0.07) *†‡</td>
<td>0.57(0.19)</td>
<td>0.68(0.20)</td>
<td>0.85(0.14)</td>
</tr>
</tbody>
</table>

With ANN
C. Capacity of AC and DC for Artifacts Rejection during Surgery

It is noted that the amplitude of EEG signal is very weak and almost always contaminated by noise or artifacts. Therefore, a good enough EEG-based indicator should be insensitive to noise or artifacts for accuracy in measurement of DOA. In this section, AC, DC, SampEn, DFA and PE after filtering using MEMD method were compared with that before filtering mentioned in the previous section to evaluate their sensitivity to artifacts in EEG.

| TABLE III | The values are presented with mean (SD). The original EEG signals without filtering were used. Those giving p-value lower that 0.05 of difference from SampEn, DFA and PE are marked with asterisk (*), dagger (†) and double dagger (‡), respectively. |
| Without ANN | | | | | | | |
| MAXI_AC | MAXI_DC | MINI_AC | MINI_DC | SampEn | DFA | PE |
| vs. BIS | 0.94(0.07) * | 0.94(0.07) *† | 0.91(0.09) *† | 0.91(0.09) *† | 0.75(0.15) | 0.79(0.13) | 0.84(0.10) |
| vs. EACL | 0.93(0.06) * | 0.94(0.06) *† | 0.92(0.07) *† | 0.93(0.07) *† | 0.71(0.14) | 0.75(0.16) | 0.88(0.09) |

TABLE III presents the statistical result of AUC of ROCs for AC, DC, SampEn, DFA and PE from 56 patients’ EEG signals after filtering. Those giving p-value indicate the statistically significant difference level compared with the corresponding index before filtering. The AC and DC still present a high discrimination of the difference between anesthesia state and awake state and yield a larger AUC than SampEn, DFA and PE after filtering. Furthermore, it can be seen in 4th row in TABLE III that the p-values of AC and DC (i.e., 0.61, 0.71, 0.84 and 0.53) using EACL as the gold standard without ANN have no statistically significant difference (p > 0.05) compared with TABLE I before filtering. The larger p-values in the 6th row in TABLE III indicate that the significance of the difference for AC and DC (i.e., 0.04, 0.04, 0.04, 0.08) between before and after filtering using BIS as the gold standard without ANN is less than that for SampEn (i.e., 0.00). There is a statistically significant improvement (p < 0.05) for SampEn in discrimination of the difference between anesthesia state and awake state. The AC and DC of minimum-to-minimum interval perform no significant difference between before and after filtering using EACL and BIS as the gold standard after regression via ANN. AC and DC of maximum-to-maximum after regression via ANN preserve a higher discrimination after filtering than SampEn, DFA and PE in spite of a difference compared with before filtering. Therefore, the measure of AC and DC in EEG are less sensitive to noise or artifacts and better than SampEn, DFA and PE for DOA monitoring. Especially, the p-values of AC and DC using EACL as gold standard in 4th and 9th rows in
TABLE III are larger than that using BIS as gold standard in 6th and 11th rows in TABLE III which indicates that the proposed method is more robust to determine the anesthesia state using the real gold standard (i.e., EACL).

In addition, TABLE IV presents the Pearson correlation coefficient between AC, DC, SampEn, DFA and PE and EACL, BIS after filtering, respectively. The correlation coefficients of AC and DC are clearly significantly larger (p < 0.05) than SampEn and DFA. There is a high linear correlation (i.e., 0.78 ± 0.12) between AC, DC and EACL. The SampEn are more close to the EACL and BIS trend after filtering. The p-values in 9th row (i.e., 0.09, 0.11, 0.08 and 0.08) in TABLE IV show that the AC and DC have no significant difference between before and after filtering using EACL as the gold standard after regression via ANN. The AC and DC are more close to EACL with higher correlation coefficients than BIS trend consisting with the conclusion as mentioned above.

### TABLE III

The statistical result of AUC of ROCs for AC, DC, SampEn, DFA and PE from 56 patients. The values are presented with mean (SD). The EEG signals after filtering were used. Those giving p-value lower that 0.05 of difference from SampEn, DFA and PE are marked with asterisk (*), dagger (†) and double dagger (‡), respectively. The p-value in the table indicates the statistical significant difference level compared with before filtering.

<table>
<thead>
<tr>
<th></th>
<th>MAXI_AC</th>
<th>MAXI_DC</th>
<th>MINI_AC</th>
<th>MINI_DC</th>
<th>SampEn</th>
<th>DFA</th>
<th>PE</th>
</tr>
</thead>
<tbody>
<tr>
<td>vs. EACL</td>
<td>0.90(0.09) *†</td>
<td>0.90(0.09) *†</td>
<td>0.90(0.09) *†</td>
<td>0.90(0.09) *†</td>
<td>0.73(0.14)</td>
<td>0.66(0.12)</td>
<td>0.88(0.11)</td>
</tr>
<tr>
<td>p-value</td>
<td>0.61</td>
<td>0.71</td>
<td>0.84</td>
<td>0.53</td>
<td>0.00</td>
<td>0.16</td>
<td>0.00</td>
</tr>
<tr>
<td>vs. BIS</td>
<td>0.88(0.10) *†</td>
<td>0.89(0.10) *†</td>
<td>0.88(0.10) *†</td>
<td>0.89(0.10) *†</td>
<td>0.79(0.15)</td>
<td>0.66(0.10)</td>
<td>0.87(0.12)</td>
</tr>
<tr>
<td>p-value</td>
<td>0.04</td>
<td>0.04</td>
<td>0.04</td>
<td>0.08</td>
<td>0.00</td>
<td>0.61</td>
<td>0.09</td>
</tr>
</tbody>
</table>

### TABLE IV

The statistical result of Pearson correlation coefficient between AC, DC, SampEn, DFA, PE and EACL, BIS from 56 patients. The values are presented with mean (SD). The EEG signals after filtering were used. Those giving p-value lower that 0.05 of difference from SampEn, DFA and PE are marked with asterisk (*), dagger (†) and double dagger (‡), respectively. The p-value in the table indicates the statistical significant difference level compared with the corresponding index before filtering.

<table>
<thead>
<tr>
<th></th>
<th>MAXI_AC</th>
<th>MAXI_DC</th>
<th>MINI_AC</th>
<th>MINI_DC</th>
<th>SampEn</th>
<th>DFA</th>
<th>PE</th>
</tr>
</thead>
<tbody>
<tr>
<td>vs. EACL</td>
<td>0.92(0.08) *†</td>
<td>0.92(0.08) *†</td>
<td>0.91(0.08) *†</td>
<td>0.92(0.07) *†</td>
<td>0.83(0.11)</td>
<td>0.78(0.11)</td>
<td>0.86(0.13)</td>
</tr>
<tr>
<td>p-value</td>
<td>0.04</td>
<td>0.03</td>
<td>0.66</td>
<td>0.46</td>
<td>0.00</td>
<td>0.12</td>
<td>0.09</td>
</tr>
<tr>
<td>vs. BIS</td>
<td>0.91(0.09) *†</td>
<td>0.91(0.09) *†</td>
<td>0.90(0.09) *†</td>
<td>0.92(0.08) *†</td>
<td>0.80(0.15)</td>
<td>0.79(0.12)</td>
<td>0.89(0.10)</td>
</tr>
<tr>
<td>p-value</td>
<td>0.00</td>
<td>0.01</td>
<td>0.05</td>
<td>0.28</td>
<td>0.00</td>
<td>0.08</td>
<td>0.26</td>
</tr>
</tbody>
</table>

### Without ANN

<table>
<thead>
<tr>
<th></th>
<th>MAXI_AC</th>
<th>MAXI_DC</th>
<th>MINI_AC</th>
<th>MINI_DC</th>
<th>SampEn</th>
<th>DFA</th>
<th>PE</th>
</tr>
</thead>
<tbody>
<tr>
<td>vs. EACL</td>
<td>0.64(0.14) *†</td>
<td>0.64(0.14) *†</td>
<td>0.64(0.14) *†</td>
<td>0.64(0.14) *†</td>
<td>0.25(0.29)</td>
<td>0.18(0.19)</td>
<td>0.61(0.21)</td>
</tr>
<tr>
<td>p-value</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.05</td>
<td>0.00</td>
</tr>
</tbody>
</table>
proven by our findings in TABLE IV that there are larger correlation coefficient values using EACL as the gold standard. So our proposed method can be used as a more accurate reference of the DOA estimation based on EACL.

There are various limitations in this study. First, burst suppression EEG pattern occurring during deep anesthesia was not taken into consideration. Burst suppression is a serious problem in the DOA monitors based on EEG, which can be regarded as light anesthesia level in spite of under deep anesthesia [50]. BIS index has solved this problem by introducing a ratio to indicate burst suppression behavior [51]. In current study, no burst suppression was found in the analyzed EEG collected from 56 patients. So there is no impact on our findings. However, future works still are needed to confirm whether the proposed method can detect burst suppression pattern and is robust to measure the DOA accurately. Second, three type of agents including propofol, sevoflurane and desflurane were used to induce and maintain an appropriate anesthesia level in 56 patients, and they have the same mechanisms to causes anesthesia by gamma-aminobutyric acid (GABA$_\text{A}$) receptor to depress CNS activity [49, 52]. So our results support the agents with the same the mechanism of action. Nevertheless, several anesthetic agents such as ketamine and nitrous oxide have different mechanism to produce general anesthesia, so whether the proposed method can be applied to measure anesthesia with the agent-specific mechanism also needs more potential works to confirm.

V. Conclusion

This paper study a PRSA technique to detect the quasi-periodicities of EEG signal defined by AC and DC parameters for DOA monitoring under general anesthesia. First, maximum-to-maximum and minimum-to-minimum intervals (MMI) of the original EEG signal are extracted. So the abnormal absolute amplitude of EEG due to artifacts have less impact on the accuracy. Second, PRSA was used to process extracted MMI sequences from EEG, the phases of all periodic segments are synchronized by alignment at the anchor points, and the artifacts can be eliminated by segments averaging. There is a significant difference (i.e., $p < 0.05$) for AC and DC to distinguish stage 1, stage 2 and stage 3 during the whole general anesthesia. The proposed method provides a strong discrimination between anesthesia and awake states and a good correlation with EACL via ANN. Furthermore, we also compared their performance before and after filtering using the sum of $\text{IMF}_2(t)$ and $\text{IMF}_3(t)$, AC and DC perform better than SampEn, DFA and PE in the case of accuracy and robustness to measure the DOA under general anesthesia.
It is noted that there is a stronger correlation between AC, DC and EACI than BIS in spite of similar AUC. The EACI as the real gold standard derived from five experienced anesthesiologists provides a reliable target to define and trace the consciousness level. It would not have the drawbacks occurring in BIS. Consequently, the AC and DC after regression via ANN using EACI as target are more acceptable and present a real DOA monitor ranged from 0 to 100 to indicate the anesthesia trend.

REFERENCES


