# AUTOMATIC REACTIVE POWER COMPENSATOR: AN OPEN LOOP APPROACH 

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## ABSTRACT

Over the last few years the sudden increase of the use of non-linear loads such as personal computers and TV sets created a Power Factor (PF) problem. Although such loads consume relatively small amount of power, however the large number of these loads resulted on huge distortion in the power quality. One major element of the power quality is the PF. This thesis proposes an automatic PF correction circuit which can generate a leading as well as lagging reactive current which can be used to improve the PF. The proposed circuit consists of two semiconductor switches and two capacitors and an inductor. Such configuration is capable of generating not only variable reactive current, but also with very low distortion compared to other techniques, which usually generate a high distortion reactive current.

The proposed compensator is controlled by a microprocessor which generates the required switching pulses. The thesis also covers the protection circuits used to protect the semiconductor switches (MOSFETs) during the turn-on and turn-off times.

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## List of Abbreviations

| DC | Direct Current |
| :--- | :--- |
| PF | Power Factor |
| HVDC | High Voltage DC Transmission |
| TSC | Thyrister Switched Capacitor |
| MSC | Mechanical Switched Capacitor |
| PW | Pulse Width |
| PER | Period of the Cycle |
| RAM | Random Access Memory |
| ROM | Read Only Memory |
| EPROM | Erasable Programmable Read Only Memory |
| THD | Total Harmonic Distortion |
| FACTS | Flexible AC Transmission System |

## Chapter1

## Introduction

### 1.1 Problem Overview

In the past, most of the loads were linear loads. A linear load is the load where the voltage across it and the current through follow the same pattern. For example if the voltage is sinusoidal the current is also sinusoidal. Calculations of power, and power factors in such loads were straight forward and most of these loads were fed from sinusoidal voltage and the power factor in these loads is simply cos the angle between the voltage and current. However, over the last 50 years, large non-linear loads such static power converters used in High Voltage DC transmission (HVDC) started to appear and due to the semiconductor devices used in such converters, the linear relationship between the voltage and current is not valid any more. Such large non-linear loads were identifiable and mechanisms for dealing with improving the power factor in such large non-linear loads were fully investigated. The main problem started to appear over the last 20 years where the number of 'small' nonlinear loads has risen exponentially. For example a typical office building like the Howell building at Brunel University may have less than five PCs in 1985, it is now have more than 500 PCs. Such example is true for most of the buildings in the city. TV sets are another example of such 'small' non-linear loads, and it hardly to find a home now without at least two TV sets. This huge increase of 'small' non-linear loads comes with a price. The price is a very poor Power Factor (PF) and a much distorted current and voltage waveforms, in another word a very poor power quality. While 'large' non-linear loads are identifiable and correction devices can be installed to compensate for a predictable poor power factor, 'small' non-linear loads are widely spread and compensation mechanisms which are suitable for 'large' non-linear loads cannot be implemented for 'small' non-linear loads [2, 3].

This thesis investigates and proposes a compensator circuits which can be used to improve the power factor in both small linear and non-linear loads. The proposed compensators can be connected in shunt for 'retrofit application'. The advantages of this compensator are the ability to generate leading as well as lagging reactive powers and also the compactness of the design which make it more attractive and convenient in small size loads [11].

### 1.2 Aims and Objectives

The main aim of this research work is to design an automatic power factor compensation circuit which can be used to generate a variable leading as well as lagging reactive power for linear and non-linear loads. In order to achieve this main aim the following objectives were set:

- Investigate fully the PF problem in linear and non-linear loads.
- Proposing a compensator circuit.
- Finding a mathematical formula for the proposed circuit.
- Simulating the proposed compensator using PSPICE software.
- Investigating the control circuit and designing the protection for the semiconductor switches used in the compensator.
- Building and testing the proposed circuit.


### 1.3 Thesis Layout

This thesis is divided into six chapters. This chapter is introduction to the problems of feeding non-linear loads and also it gives a brief idea about compensation as basic solution for improving power factor in power system area.

The second chapter deals with the definition of power factor in linear and non-linear loads. The need for power factor correction was also summarised together with the costing analysis for power factor compensation. A numerical example to illustrate the need for a constantly variable capacitor for a changeable load was introduced. Two well known techniques (MSC and TSC) were briefly summarised. The TSC compensator was analysed in order to see the harmonic contents of such compensator. In some cases, and due to high current harmonics, such compensator will have negative effect on the power factor compensation.

The proposed automatic compensator is introduced in chapter three. The compensator is fully analysed for the possibility of generating leading as well as lagging power factors. The effective value of the capacitance of the compensator $\mathrm{C}_{\text {ceff-total }}$ is evaluated by calculation, simulation and a comparison between the two sets of curves is introduced. The practical results of the automatic compensator are
also introduced showing the ability of the compensator to generate a variable amount of reactive current at different switching pattern. Such performance will require several banks of capacitors if ordinary fixed capacitors are used as a reactive power compensator.

In chapter four the automatic compensator is tested for improving the power factor in both linear and non-linear loads. Simulation and practical results are introduced to illustrate how the automatic compensator can improve the power factor in passive inductive loads as well as in a.c. voltage controllers (as an example of non-linear loads).

The power factor in such non-linear load decreases as the triggering angle of the thyristor increases. Obviously such circuits are used to control the output voltage applied to a load and this is achieved through the variation of the triggering angle. This means that the power factor is likely to be very poor in such applications.

In chapter five, the control of the compensator is discussed. The use of the microprocessor to produce the switching pattern for controlling the MOSFET switches is also investigated. The microprocessor was mainly set to generate the main control pulses and then a hardware circuit was used to generate the required overlapping pulses. The protection of the MOSFETs used in the compensator is fully investigated in the same chapter.

Chapter six contains the conclusions and the future work of this thesis. All relevant work which is essential but could interrupt the flow of the thesis are given in the appendices.

## Chapter Two

Literature Review of Power Factor Compensator

### 2.1 Introduction

Inductive and capacitive loads create phase shift between voltage and current waveforms. The phase angle created by such loads can vary between 0 and 90 degrees. The current leads the voltage in the case of capacitive load and it lags the voltage in the case of inductive loads. This phase angle causes a poor power factor [1-3]. Also in non-linear loads such poor power factor can exist even if the load is a purely resistive. This chapter deals with problems caused by poor power factor and it also deals with methods for improving/correcting the power factor.

### 2.2 What is the Power Factor?

Power Factor (PF) is referred to in many literatures as the ratio of the Real Power to the Apparent Power and in the case of linear loads is 'cos' the angle between the voltage and current [1,5,14].

$$
\text { P.F. }=\frac{\text { Real Power }}{\text { Apparent Power }}=\cos \Phi
$$

In non-linear loads such equation has to be derived from the beginning as follows. The supply voltage $v(t)$ can be seen as a combination of several frequencies when added together they form the original voltage waveform. Similarly, the current in non-linear loads can also be seen as a combination of several frequencies when added together they form the original current waveform. Voltage and current harmonics having the same frequencies is referred to as ' $n$ ' terms in equations 2.2 and 2.3. Voltage harmonics which do not have equivalent current harmonics is referred to as ' $m$ ' terms in equations 2.2 and 2.3. Current harmonics which do not have equivalent voltage harmonics is referred to as ' $k$ ' terms in equations 2.2 and 2.3.
$v(t)=\sum^{n} \sqrt{2} V_{n} \sin \left(n \omega t+\alpha_{n}\right)+\sum^{m} \sqrt{2} V_{m} \sin \left(m \omega t+\alpha_{m}\right)$
$i(t)=\sum^{n} \sqrt{2} I_{n} \sin \left(n \omega t+\alpha_{n}+\phi_{n}\right)+\sum^{k} \sqrt{2} I_{k} \sin \left(k \omega t+\alpha_{k}\right)$

Power Factor $=\frac{\frac{1}{T} \int_{O}^{T} v i d t}{V I}$

$$
\sum^{n} V_{n} I_{n} \cos \phi_{n}
$$

Power Factor $=$

$$
\begin{equation*}
\sqrt{\left(\sum^{n} V_{n}^{2}+\sum^{m} V_{m}^{2}\right)\left(\sum^{n} I_{n}^{2}+\sum^{k} I_{k}^{2}\right)} \tag{2.4}
\end{equation*}
$$

The power factor in such generic non-linear load can be seen as the ratio of active power (including the power consumed by other frequencies apart from the fundamental) to the apparent power [37]. The best way is to illustrate this by the diagram shown in Fig. 2.1

Fig. 2.1: "3D" Power Triangle

where:
$P=$ Real Power
$D=$ Distortion Power (only exists in non-linear loads)
$Q=$ Reactive Power
F = Fictitious Power (=Reactive Power in linear loads)
$S=$ Phasor Power (= Apparent power in linear load)
$\mathrm{U}=$ Apparent Power (non-linear load)

The '3D' vector Apparent Power can be expressed as:

$$
\begin{equation*}
U=\sqrt{P^{2}+Q^{2}+D^{2}} \tag{2.5}
\end{equation*}
$$

If the voltage distortion is ignored then the PF equation can be reduced to:

$$
\begin{equation*}
P F=\frac{\mathrm{V}_{1} \mathrm{I}_{1}}{\mathrm{~V}_{1} \mathrm{I}} \cos \Phi_{1}=\frac{\mathrm{I}_{1}}{\mathrm{I}} \cos \Phi_{1} \tag{2.6}
\end{equation*}
$$

The first term can be referred to as the distortion factor and the second tern can be referred to as the displacement factor.

Obviously if the load is linear load and there is no current harmonics, then the distortion factor is ' 1 ' and the power factor equation is reduced to:

$$
P F=\cos \Phi
$$

The diagram in Fig. 2.2 shows the power factor triangle in linear loads.

(Q) Reactive Power (VAr)
(P) Useful Power (W)

Fig. 2.2: Power Triangle in linear-loads

### 2.3 Power Factor Correction

As it can be seen from the previous section, at poor power factor the apparent power is much bigger than the real power. In order to generate amount of power (VA) similar or near similar to the required power (W) the power factor need to be as close as possible to unity. In non linear loads that can be achieved by passive and active filters. In linear loads that can be achieved by capacitors in parallel with the load. In either linear or non-linear loads the cost of poor power factor could be significant [1, 37, 40]. Since utility companies provide both the active and reactive
powers to meet the need for industrial consumers, they charge for KVA. That means they charge for poor power factor. The graph shown in Fig. 2.3 illustrates a typical energy charge for a small industrial customer before and after power factor correction. The details of this graph which shows the monthly billing information is given in Appendix ' A '.

## Demand Charge before PF correction (\$)

(\$)

cost of operating at a poor PF is clearly illustrated. Those costs can be determined by understanding how the utility company calculates the electric bills. However, this is not the only cost associated with the poor PF, there are other hidden cost of poor power factor such as [1]:

- Reduces distribution system capacity
- Reduces terminal voltage equipment
- Increases heat loading in facility
- Shortens equipment life
- Creates kWh distribution losses that consumers pay for.

The following example illustrates how a poor PF reduces the capacity needed to supply additional loads:

System Capacity Released $=100 \times\left(1-\mathrm{Pf}_{\mathrm{o}} / \mathrm{PF}_{\mathrm{f}}\right)$

Where: $\quad \mathrm{Pf}_{0}=$ original PF
$\mathrm{PF}_{f}=$ final PF after correction
If the small industrial customer shown in Fig. 2.3 above wants to improve PF of 0.71 to 0.95 :
\% System Capacity Released $=100 \times(1-0.71 / 0.95)=25.3 \%$

That freed up capacity could allow the small industrial customer to add equipment, use smaller less expensive conductors, or avoid a costly capacity expansion project.

Improvement of power factor in linear loads using a fixed capacitor is well documented. However, a numerical example is introduced in this chapter as it will be taken as a case for a comparison when an automatic power factor correction is applied.

## Numerical Example:

An inductive load has a resistance of $20 \Omega$ and an inductance of 50 mH (connected in series) is supplied from $240 \mathrm{~V}, 50 \mathrm{~Hz}$ supply. Calculate the value of the shunt capacitor which can improve the power factor to 0.95 lagging.

Referring to Fig. 2.4:

$$
\begin{aligned}
& X_{L}=2 \times \pi \times f \times L=15.7 \Omega \\
& Z=\sqrt{ }\left(20^{2}+15.7^{2}\right)=25.43 \Omega \\
& i_{R L}=240 / 25.43=9.44 \mathrm{~A}
\end{aligned}
$$



Fig. 2.4: Numerical example diagram

$$
\begin{aligned}
& \Phi_{1}=\tan ^{-1}\left(X_{L} / R\right)=38^{\circ} \\
& \Phi_{2}=\cos ^{-1}(0.95)=18.2^{\circ} \\
& \sin \Phi_{1}=x / i_{R L} \\
& x=\sin 38 \times 9.44=5.8 \\
& k=\sqrt{ }\left(9.44^{2}-5.8^{2}\right)=7.45 \\
& \tan \Phi_{2}=y / k \\
& y=k \tan \Phi_{2}=2.45 \\
& x-y=7.45-2.45=5 \text { (ic should equal } 5 \text { Amp) } \\
& X_{c}=V / i_{c}=240 / 5=48 \Omega \\
& C=1 /\left(2 \pi f X_{c}\right)=66 \mu F \text { (This is the value of the capacitor which will } \\
& \text { improve the power factor to } 0.95 .
\end{aligned}
$$

It can be seen from the above example that if either the resistance or the inductance of the load varies, a different value of a compensating capacitor has to be reevaluated. Also the supply frequency will affect the value of the required compensating capacitor. This can be a problem in some linear loads where the nature of the load requires continuous variation of the values of ' $R$ ' and ' $L$ '. One solution is to use Thyristor-Switched Reactor (TSR) or Thyristor-Switched Capacitor (TSC). TSR is usually used for correcting the PF from a leading to a lagging. TSC is used for correcting the PF from a lagging to a leading. Since the proposed technique is used for lagging power factor correction, only the TSC is reviewed briefly below [8, 10].

### 2.4 Mechanically-Switched Capacitor (MSC)

In this technique capacitor is switched by circuit-breaker. Usually the MSC is switched only when needed. It could be a single capacitor with a single circuitbreaker or multi capacitors with multi circuit breakers in order to give variety of capacitances as shown in Fig. 2.5.


Single switch single circuit-breaker


Multi switch multi circuit-breaker

Fig. 2.5 MSC Compensator

### 2.5 Thyristor-Switched Capacitor (TSC)

In this technique, as shown in Fig. 2.6, the capacitor is connected in series with either two thyristors back to back or with a Triac. The thyristors (or the Triac) are either in zero or full conduction ( $\alpha=0^{\circ}$ or $\alpha=180^{\circ}$ ). The equivalent capacitive reactance in this circuit can be varied in stepwise manner. Although such technique can be effective in some applications, however the triggering of the thyristors in either zero or full conduction can cause the generation of huge amount of current harmonics. So although the displacement factor component in the power factor is improved, the distortion factor (due to the current harmonics) is significantly reduced. Fig. 2.7 illustrates the voltage and current waveforms as well as the frequency spectra of the current waveforms. It is very clear in this figure that the
current harmonics are having almost the same amplitude which is approximately $50 \%$ of the fundamental component of the current waveform [2, 20].

Fig. 2.6: TSC Compensator


Supply voltage (green) and compensator current (red) in the TSC circuit



Spectra of the current harmonics in the TSC circuit

Fig. 2.7: Waveforms in TSC circuit

### 2.6 Summary

In this chapter definition of power factor in linear and non-linear loads have been introduced. The need of power factor correction was also summarised together with the costing analysis for power factor compensation. A numerical example to illustrate the need for a constantly variable capacitor for a changeable load was introduced. Two well known techniques (MSC and TSC) were briefly summarised. The TSC compensator was analysed in order to see the harmonic contents of such
compensator. In some cases and due to high current harmonics, such compensator will have negative effect on the power factor compensation.

In the next chapter a more sophisticated technique for power factor compensation with low harmonic contents is introduced.

Chapter 3

## Proposed Compensator

### 3.1 Introduction

In this chapter an automatic capacitor compensator circuit is introduced. The compensator is then analysed, simulated and practically verified. Harmonic analysis of the compensator is carried out and the same numerical example shown in the previous chapter is re-introduced again but using the automatic compensator in order to compare the effectiveness of the proposed technique. In general the main purpose of this chapter is to show how the effective capacitance of an automatic capacitor circuit can be varied by simply varying the timing of the on-off switching.

### 3.2 The Automatic Compensator

The compensator is constructed from two fixed capacitors and two semiconductor switches. The choice of the semiconductor switches is discussed in details in chapter 5. However, in this chapter the switch can be seen as an ideal bidirectional switch where it can be switched on or off at any time and allow the current to flow in any direction as well as it can operate at relatively high frequency (less than 10 kHz ). The compensator consists of a semiconductor switch $S_{1}$ which is connected in series with a fixed capacitor $\mathrm{C}_{1}$ and $\mathrm{S}_{2}$ is similarly connected in series with $\mathrm{C}_{2}$. The two branches are then connected in parallel and the whole combination is connected in series with an inductor $L$ as shown in Fig. 3.1. The resistor shown in the figure only represents the resistance of the inductor, switches, capacitors, and the wires. The reason the resistor is used so that it can cause the circuit to reach the steady state in the simulation, and there is no actual resistance added in the practical setup [7, 17].

Fig. 3.1: The automatic compensator circuit


The two switches operate in anti-phase manor so that when $S_{1}$ is closed, $S_{2}$ is open and vice versa. The control pulses used for the control of the switches can be illustrated in Fig. 3.2


Fig. 3.2: Operation of $S_{1}$ and $S_{2}$

The 'on' time of the switch can be controlled so that the 'on'/('on'+'off') ratio can be varied from ' 0 ' to ' 1 '. This ratio is referred to as the switch duty cycle ' $\lambda$ '. If ' $\lambda$ ' is ' 0 ' for $S_{1}$, it will be ' 1 ' for $S_{2}$ and vice versa. For convenience the symbol ' $\lambda$ ' is used in conjunction with $S_{1}$ throughout the rest of this thesis.

### 3.3 Calculations of the Effective Capacitance

The objective of this section is to calculate the effective capacitor value of the automatic compensator.

With reference to Fig. 3.1, the supply voltage can be expressed as:

$$
V_{s}=L \frac{d i(t)}{d t}+\frac{1}{c} f_{s}(t) \int_{0}^{t} f_{s 1}(\tau) i(\tau) d \tau
$$

The above equation is considerably simplified for only fundamental component. Following the procedure described in reference [31] the effective value of the capacitance of the two capacitors and the two switches can be written as:

$$
C_{e f f}=\frac{C_{1}}{\lambda^{2}+\gamma(1-\lambda)^{2}}
$$

where:

$$
\begin{align*}
& \lambda=\frac{T_{o n}}{T_{o n}+T_{o f f}} \\
& \gamma=\frac{C_{1}}{C_{2}}
\end{align*}
$$

The equivalent capacitive reactance of $\mathrm{C}_{\text {eff }}$ can be written as:

$$
X_{C e f f}=\frac{1}{2 \pi f C_{e f f}}
$$

Similarly, the effective impedance ( $Z_{\text {eff }}$ ) of the compensator can be written as:

$$
Z_{e f f}=\sqrt{R^{2}+\left(\mathrm{X}_{\text {ceff }}-\mathrm{X}_{\mathrm{L}}\right)^{2}}
$$

where:

$$
X_{L}=2 \pi f L
$$

$R$ is the resistance of the inductor, switches, capacitors, and the wires as explained in section 3.2 above and therefore is very small.

If the value of the inductor is chosen to so that $X_{L}$ is smaller than $X_{\text {ceff }}$ for all value of $\lambda$, and $R$ is very small then $Z_{\text {eff }}$ will have the effect of a capacitor and the whole compensator circuit is a capacitive equivalent circuit. Therefore $Z_{\text {eff }}$ can be referred to as $X_{\text {ceff-total }}$ and the equivalent capacitance of the compensator in this case will be $\mathrm{C}_{\text {ceff-total }}$.

An Excel program was used to calculate the variable value of $\mathrm{C}_{\text {ceff-total }}$ against the duty cycle ( $\lambda$ ). Fig 3.3 illustrated this relationship and it can be seen from the figure that $\mathrm{C}_{\text {ceff-total }}$ equal $124 \mu \mathrm{~F}$ at $\lambda=0$ and $12.6 \mu \mathrm{~F}$ at $\lambda=1$. The maximum $\mathrm{C}_{\text {ceff-total }}$ occurs at $\lambda=0.1$ and has the value of $140 \mu \mathrm{~F}$. Also it is clear from the graph that by selecting the appropriate duty cycle $\mathrm{C}_{\text {ceff-total }}$ can be varied from $12.6 \mu \mathrm{~F}$ to $140 \mu \mathrm{~F}$. The range of $\mathrm{C}_{\text {ceff-total }}$ in this case is:
$140 \mu \mathrm{~F}-10.2 \mu \mathrm{~F}=129.8 \mu \mathrm{~F}$. The ratio of the value of this range to the maximum value of $\mathrm{C}_{\text {ceff-total }}$ (denoted as $\xi$ ) will be the following. The general Equation to $\xi$ :

$$
\xi=\frac{129.9 \mu F}{140 \mu F}=0.927 \text { (Say 93\%) }
$$



Fig. 3.3: The effective value of the capacitor as a function of the duty cycle $\lambda$. $\left(\mathrm{C}_{1}=10\right.$ uf, $\mathrm{C}_{2}=100$ uf, $\left.\mathrm{L}=5 \mathrm{mH}, \mathrm{R}=1 \Omega\right)$

If the value of the two fixed capacitors are equal, say $C_{1}=C_{2}=100 \mu \mathrm{~F}$, the peak value of $\mathrm{C}_{\text {ceff-total }}$ will be shifted to 0.5 duty cycle as shown in Fig.3.4. $\mathrm{C}_{\text {ceff-total }}$ at 0.1 duty cycle ( $\lambda=0.1$ ) in this case is the same as $\mathrm{C}_{\text {ceff-total }}$ at 0.9 duty cycle $(\lambda=0.9)$ and is equal to $124 \mu \mathrm{~F}$. The peak value of $\mathrm{C}_{\text {ceff-total }}$ at $\lambda=0.5$ in this case equals to 329 $\mu F$. The value of $\xi$ with reference to Fig. 3.4 in this case will be:

$$
\xi=\frac{329 \mu F-124 \mu F}{329 \mu}=0.623 \text { (Say 62\%) }
$$

It is obvious that a large value of $\xi$ is desirable, this is mainly because a wide range of $\mathrm{C}_{\text {ceff-total }}$ will allow a wide range of compensation. However, as it will be seen later in the simulation section that a large value of $\xi$ comes on the expense of a large harmonic distortion.


Fig. 3.4: The effective value of the capacitor as a function of the duty cycle $\lambda\left(C_{1}=100\right.$ uf, $C_{2}=100$ uf, $\left.L=5 \mathrm{mH}, \mathrm{R}=1 \Omega\right)$

The above two cases (Figs. 3.3 and 3.4) are the two extreme cases, where the value of $\xi$ is either minimum ( $\approx 0.62$ ) or maximum ( $\approx 0.93$ ). The graphs shown in Fig. 3.5 illustrate how the value of $\mathrm{C}_{\text {ceff-total }}$ respond to different duty cycles as well as to different ratios of $C_{1} / C_{2}$. This figure can help the designer in selecting the suitable fixed values for $C_{1}$ and $C_{2}$ for a particular $C_{\text {ceff-total }}$, however such choice is also determined by the harmonic contents of the compensating current as will be discussed in section 3.5. Fig. 3.6 shows the relation between $\xi$ to $\gamma$. It can be seen from this figure that $\gamma$ has an inversely proportional relationship with $\xi$. It is important to mention that the values of $\mathrm{C}_{\text {ceff-total }}$, shown in Fig. 3.5 did not take into consideration any harmonic contents in the compensating current. The graphs in this figure are only based on the calculation of the fundamental component. In the simulation and practical sections which will follow, the values of $\mathrm{C}_{\text {ceff-total }}$, will be represented but without ignoring any harmonic distortion. A comparison of the calculated, simulated and practical results will show that the calculated results presented in Fig. 3.5 gives an accurate envelop of $\mathrm{C}_{\text {ceff-total }}$.


Fig. 3.5: The effective value of the capacitor as a function of the duty cycle ( $\lambda$ ) at different value of capacitor ratios $(\gamma)$


Fig. 3.6: Calculated Relationship between $\xi$ and $\gamma$

Appendix $B$ contains the calculated values of $C_{\text {ceff-total }}$ for different values of ' $\lambda$ ' and ' $\gamma$ '.

### 3.4 Simulation of the Effective Capacitance

In order to verify the calculated results in section 3.3, the compensator circuit has been simulated using PSPICE software. The switches used in the simulation were ideal switches (Sbreak), and this is mainly to see the overall characteristics of the compensator. In chapter 5 the ideal switches are replaced by semiconductor switches (MOSFETs) in order to study the detail behaviour of the compensator (losses, etc.). The ideal switches are controlled by applying 'Vpulse', The parameters used in 'Vpulse' are shown in Fig. 3.7, where the value of ' $\lambda$ ' is 'PW/PER'. The switching frequency can be selected through 'PER' ( $f_{s}=1 / P E R$ ).


Fig. 3.7: Details of Vpulse
where $T_{d}$ is delay time and $T_{r}$ is rising time. Fig. 3.8 illustrates the circuit used in the simulation. The supply current and the compensator current are shown in Fig, 3.9. It is very clear from Fig. 3.9 that circuit current leads the supply voltage by $90^{\circ}$. This indicates that the compensator performs like a capacitor. The value of the compensator current can vary in magnitude simply by varying the duty cycle ' $\lambda$ ' of the switches, however the current at all values of ' $\lambda$ ' remains reactive current (i.e. leads the supply voltage by $90^{\circ}$.). This is illustrated in the current waveforms shown in Fig. 3.10 where ' $\lambda$ ' is 0.5 in one case and equals 0.25 in the other case. It is
noticeable that at ' $\lambda$ ' $=0.25$, the compensator current contains some harmonic distortion. This distortion analysis is covered in details in section 3.6.


Fig. 3.8: The automatic compensator circuit used in PSPICE


Fig. 3.9: Supply voltage and reactive current of the circuit in Fig. 3.7 (50Hz)


Fig. 3.10: Supply voltage and reactive currents at different duty cycles ( $\lambda$ ). ( 50 Hz ).

The simulated result for $\mathrm{C}_{\text {ceff-total }}$ when $\mathrm{C}_{1}$ is $0.1 \mathrm{C}_{2}$ is shown in Fig. 3.11. It can be seen from that figure that $\mathrm{C}_{\text {ceff-total }}$ can be varied from $\approx 14 \mu \mathrm{~F}$ to $\approx 160 \mu \mathrm{~F}$ through the selection of the appropriate duty cycle ' $\lambda$ '. The shapes of Figs 3.3 and 3.11 are almost identical; however there is a difference in the values of $\mathrm{C}_{\text {ceff-total }}$ in both cases. This difference is investigated in section 3.5.


Fig. 3.11: The simulated effective value of the capacitor as a function of the duty cycle $\lambda .\left(C_{1}=10 u f, C_{2}=100 u f, L=5 \mathrm{mH}, \mathrm{R}=1 \Omega\right)$

The graph at $\mathrm{C}_{1}=\mathrm{C}_{2}=100 \mathrm{uF}$ is shown in Fig. 3.12 and it has the same envelop as the calculated graph at the same values (shown Fig. 3.4). It can also be concluded from Figs 3.11 and 3.12 that $\gamma$ has an inversely proportional relationship with $\xi$. This can be shown in Fig. 3.13 where both the calculated graph (shown in Fig. 3.6) and the simulated graph are illustrated together for a comparison. The difference between the two graphs is discussed in section 3.5.


Fig. 3.12: The simulated effective value of the capacitor as a function of the duty cycle $\lambda .\left(C_{1}=C_{2}=100\right.$ uf, $\left.L=5 \mathrm{mH}, \mathrm{R}=1 \Omega\right)$


Fig. 3.13: Simulated and Calculated Relationship between $\xi$ and $\gamma$

### 3.5 Comparison between Simulation and Calculated Results

In the calculation results presented in section 3.1, it has been assumed that the total compensator current is free from any harmonics and hence the calculation of $\mathrm{C}_{\text {ceff-total }}$ was based on this assumption. If the harmonic in the current waveform is to be taken into consideration then the calculation would have been very complicated. Also by looking at the reactive compensator current (shown in Fig. 3.10), where the reactive current waveform is very close to a sinusoidal waveform, such assumption (ignoring current harmonics) can be justified. However, at some duty cycles and also at some values of ' $\gamma$ ', the harmonic distortion could be large.

As for the simulation results presented in the previous section (3.4), there was no need to make such assumption as the value of the current taken in the calculation of $\mathrm{C}_{\text {ceff-total }}$ was the total current and not just the fundamental as in the case of the calculated results. Therefore, the simulation curves are more accurate compared to the calculated curves. However it has to be noticed that both calculated and simulated curves have very similar envelops.

It should also be noticed that there are several levels of simulations depending of the packages used. For example a simulation based on MATLAB is very likely to give results very close to the calculated results, however a simulation based on PSpice is more likely to give results closer to the practical setting. This is mainly because in PSpice details of the circuit parameters are considered in the simulation and most of the practical devices (capacitors, inductors, switches, etc.) have PSpice library available which gives very close simulation performance like the practical ones.

In order to see the effect of the assumption of ignoring the harmonics in the compensated current, values of $\mathrm{C}_{\text {ceff-total }}$ for calculated and simulated results are put together for different values of ' $\gamma$ ' and for different duty cycle ' $\lambda$ ', as shown in Fig. 3.14. [see Appendix C]











Fig. 3.14: Calculated and simulated $\mathrm{C}_{\text {ceff-total }}$ at different values of ' $\gamma$ ' against duty cycles ( $\lambda$ ) . ${ }_{32}$ Simulation, $\qquad$ Calculation

### 3.6 Distortion Analysis

In this section the harmonics generated by the automatic compensator are investigated. One of the ways to measure the harmonic contents (voltage or current) is the Total Harmonic Distortion (THD). THD is the measure of how pure is the wave form. A zero THD means a pure sinusoidal waveform while a unity THD means that the total harmonics present in the system are equal to the fundamental component. THD can be expressed by the following equation:

$$
T H D=\frac{i_{h}}{i_{1}}
$$

where: $i_{h}=\sum_{n=1}^{\infty} i_{n}{ }^{2}$, and $i_{1}$ is the 50 Hz fundamental compoluлi
As can be seen, it very difficult to calculate the harmonic terms up too. Therefore, the THD is calculate by subtracting the fundamental component from the total current:

$$
i_{h}=\sqrt[2]{i_{t}^{2}-i_{1}^{2}}
$$

So the THD can be expressed as:

$$
T H D=\frac{\sqrt[2]{i_{t}^{2}-i_{1}^{2}}}{i_{1}}
$$

The THD for all values of the capacitor ratios ' $\gamma$ ' and all values of the duty cycle ' $\lambda$ ' have been calculated using PSpice (for evaluating the fundamental and the total current harmonics). The spread sheet shown in Appendix E illustrates these values. It can be seen from these values that the maximum THD is: 0.282321425 . The average THD in all cases is 0.119731625 (about $12 \%$ ). Such THD may appear to be high; however considering that the THD in some non-linear loads (such as TV sets and computer power supplies) can easily exceeds 500\% [15,18], the THD caused by the compensator could be acceptable.

### 3.7 Practical Results

In order to show that the automatic compensator is able to generate variable reactive currents at different duty cycles, the automatic compensator circuit was built and controlled using a microprocessor (details of the practical set up and control circuit are shown in Chapter 5). Figs. 3.15 and 3.16 illustrate the wave forms of the control switching pulses applied to $S_{1}$, the supply voltage and the compensator reactive current for two different cases. It is obvious that the compensator current is leading the supply voltage by $90^{\circ}$. Hence it shows the ability of the compensator to generate a variable reactive current at different duty cycles. Appendix F contains more practical results.


Fig. 3.15: Control pulses, supply voltage and reactive current waveforms $(\gamma=0.9, \lambda=0.5)$


Fig. 3.16: Control pulses, supply voltage and reactive current waveforms $(\gamma=1, \lambda=0.2)$

### 3.8 Summary

In this chapter the proposed automatic compensator is introduced showing that the generated current leads the supply voltage by $90^{\circ}$ and hence it is a reactive component. The effective value of the capacitance of the compensator $\mathrm{C}_{\text {ceff-total }}$ is evaluated by calculation, simulation and a comparison between the two sets of curves is introduced. The practical results of the automatic compensator are also introduced showing the ability of the compensator to generate a variable amount of reactive current at different switching pattern. Such performance will require several banks of capacitors if ordinary fixed capacitors are used as a reactive power compensator.

In the following chapter the automatic compensator is applied in order to improve the power factor in both linear and non-linear loads.

Chapter 4
Implementation of the Automatic Compensator In Linear and Non-Linear Loads

### 4.1 Introduction

In the previous chapter the automatic compensator was analysed, simulated and practically tested to show how it can generates a variable reactive current which can be used to improve the power factor. In this chapter the automatic compensator is tested for improving the power factor in both linear and non-linear loads. Simulation and practical results are introduced to illustrate how the automatic compensator can improve the power factor in passive inductive loads as well as in a.c. voltage controllers (as an example of non-linear loads).

### 4.2 Power Factor in Linear Loads

Considering the simple R-L circuit shown in Fig. 4.1, where the power factor of the circuit can be easily calculated using the simple equation:

$$
\text { P.F. }=\cos \left(\tan ^{-1}\left(\frac{X_{L}}{R}\right)\right)
$$



Fig. 4.1: Linear inductive circuit

The P.F. is calculated by fixing the value of $L$ and varying $R$ and also by fixing the value of $R$ and varying $L$. The power factor is plotted in both cases as shown in Figs. 4.2 and 4.3. It can be seen from this figures that the $P F$ is high at low value of $\left(X_{L} / R\right)$ and it declines as the value of $L$ is increased. The ratio of $X_{L} / R$ in both figures was taken so that the PF angle varies from 'almost' zero to $38^{\circ}$ [Appendix D].


Fig. 4.3: PF as a function of $R / X_{L}$

In order to improve the PF in such linear load a shunt capacitor is connected across $R-L$ and the value of the capacitor is calculated (as was illustrated in the numerical example in section 2.3). Fig. 4.4 shows the calculated value of the capacitor for every combination of $X_{L} / R$ in order to improve the PF to unity.

Fig. 4.5 shows the PSpice simulation for the RL circuit before and after the capacitor compensation.


Fig. 4.4: Calculated shunt capacitance as a function of $X_{L} / R$ for unity PF


Fig. 4.5: PSPICE simulation for the RL circuit before (top graph) and after (bottom graph) the capacitor compensation
$\qquad$ (supply voltage), $\qquad$ (supply current),

Obviously, it is not practical to keep changing the value of $C$ for every RL combination. Therefore the automatic compensator circuit will now be tested for such linear load. However in order to do that, $\mathrm{C}_{\text {ceff-total }}$ should be evaluated for every RL combination and then the duty cycle ' $\lambda$ ' is evaluated in order to generate this particular value of $\mathrm{C}_{\text {ceff-total }}$.

### 4.3 Power Factor in Non-Linear Loads

Non-linear loads are very common nowadays. Computer power supplies, ac voltage controllers and adjustable speed drives are some examples of such non-linear loads. As was explained in Chapter 2, the PF in non-linear loads is made (at least mathematically) of two components: distortion factor and displacement factor. Distortion factor can be improved by using passive or/and active filters; this is outside the scope of this thesis. However, the displacement factor which is defined as 'cos' the angle between the fundamental components of the current and voltage waveforms can be improved through the use of fixed capacitor or, for flexibility, through the use of the proposed automatic compensator as will be discussed in the following section.

A typical non-linear load is an ac voltage controller like the one shown in Fig. 4.6. In this circuit the two thyristors (connected back-to-back) are triggered in order to control the power supplied to the load. The effect of the triggering pulses is that the voltage and hence the current waveforms are chopped in a way so that the desired power is delivered to the load [2, 8, 20]. Such chopped waveform causes not only distortion to the input current wave form but also causes the fundamental component of the current to be displaced away from the supply voltage waveform as shown in Fig. 4.7.


Fig. 4.6: AC voltage controller as an example of a typical nonlinear load


Fig. 4.7: Output voltage waveforms at different triggering angles

The distortion, displacement and power factors are now investigated in this nonlinear circuit in order to calculate the optimum value of the power factor correction capacitor [7,13, 41].

The r.m.s. of the output voltage across the load can be expressed by the following equation:

$$
\begin{align*}
& V_{\text {out }(r m s)}=\sqrt{\frac{1}{\pi} \int_{\alpha}^{\pi} V_{\max }^{2} \sin ^{2} \theta d \theta} \\
& V_{\text {out }(r m s)}=\sqrt{\frac{V_{\max }^{2}}{\pi} \int_{\alpha}^{\pi} \frac{1}{2}(1-\cos 2 \theta) d \theta} \\
& V_{\text {out }(r m s)}=\frac{V_{\max }}{\sqrt{2}} \sqrt{\frac{1}{\pi}\left[\theta-\frac{\sin 2 \theta}{2}\right]_{\alpha}^{\pi}} \\
& V_{\text {out }(r m s)}=\frac{V_{\max }}{\sqrt{2}} \sqrt{\frac{1}{\pi}\left[\pi-\alpha+\frac{\sin 2 \alpha}{2}\right]} \\
& V_{\text {out }(r m s)}=\frac{V_{\max }}{\sqrt{2}} \sqrt{\frac{1}{\pi}\left[\pi-\alpha+\frac{\sin 2 \alpha}{2}\right]} \\
& V_{\text {out }(r m s)}=V_{\text {in }(r m s)} \sqrt[2]{1-\frac{\alpha}{\pi}+\frac{\sin 2 \alpha}{2 \pi}}
\end{align*}
$$

Since the load is assumed to be resistive, the RM. of the current waveform (the input and output current is the same in this circuit) can be expressed as:

$$
I_{r m s}=\frac{V_{\text {out }(r m s)}}{R}
$$

The load power (Real Power) can be expressed as:

$$
P_{\text {out }}=I^{2} R \quad \text { (W) }
$$

And the Apparent Power is defined as the total RMS of the input voltage $\times$ the RMS current:

$$
\begin{array}{lll}
\left.S=V_{\text {in }(r m s)}\right) & I_{r m s} \quad(\mathrm{VA}) & 4.9 \\
\text { Power Factor }(\mathrm{PF})=\frac{P_{\text {out }}}{V A} & 4.10
\end{array}
$$

In order to evaluate the distortion and displacement factors, the harmonic analysis of the voltage and current waveforms are evaluated as follows:

The average thyristor current

$$
\begin{aligned}
& I_{S C R(a v g)}=\frac{1}{2 \pi R} \sqrt{2} \int_{\alpha}^{\pi} V_{\text {in }(r m s)} \sin \theta d \theta \\
& I_{S C R(a v g)}=\frac{\sqrt{2} V_{i n(r m s)}}{2 \pi R}(\cos \alpha+1)
\end{aligned}
$$

The rms value of the thyristor current :

$$
\begin{align*}
& I_{S C R(\text { avg })}=\sqrt{\frac{1}{2 \pi R^{2}} \int_{\alpha}^{\pi} V_{\text {in }}^{2} \sin ^{2} \theta d \theta}=\sqrt[2]{\frac{2 V_{i n}^{2}}{4 \pi R^{2}} \int_{\alpha}^{\pi}(1-\cos 2 \theta) d \theta} \\
& I_{S C R(r m s)}=\frac{V_{\text {in }}}{\sqrt{2 R}} \sqrt[2]{1-\frac{\alpha}{\pi}+\frac{\sin 2 \alpha}{2 \pi}} \\
& V_{\text {out }}(\mathrm{t})=V_{d c}+\sum_{n=1,2, \ldots}^{\infty} a_{n} \cos \theta+\sum_{n=1,2, \ldots}^{\infty} b_{n} \sin \theta \\
& V_{d c}=\frac{1}{2 \pi} \int_{\alpha}^{2 \pi} V_{\max } \sin \theta \mathrm{d} \theta=0 \\
& a_{n}=\frac{1}{2 \pi}\left[\int_{\alpha}^{\pi}\left(V_{\max } \sin \theta\right) \cos n \theta d \theta+\int_{\pi+\alpha}^{2 \pi}\left(V_{\max } \sin \theta\right) \cos n \theta d \theta\right] \\
& a_{n}=0(\text { for } n=2,4,6 \\
& a_{1}=\frac{V_{m}}{2 \pi}(\cos 2 \alpha-1) \\
& a_{n}=\frac{V_{m}}{2 \pi}\left[\frac{2}{1+n}(\cos (1+n) \alpha-1)+\frac{2}{1-n}(\cos (1-n) \alpha-1)\right] \\
& \text { (for } n=3,5, \ldots)
\end{align*}
$$

$$
\begin{align*}
& b_{n}=\frac{1}{2 \pi}\left[\int_{\alpha}^{\pi}\left(V_{\max } \sin \theta\right) \operatorname{sinn} \theta d \theta+\int_{\pi+\alpha}^{2 \pi}\left(V_{\max } \sin \theta\right) \operatorname{sinn} \theta d \theta\right] \\
& b_{n}=0(\text { for } n=2,4,6, \ldots) \\
& b_{1}=\frac{V_{m}}{2 \pi}[\sin 2 \alpha+2(\pi-\alpha)] \quad(\text { for } n=1) \\
& \quad b_{n}=\frac{V_{m}}{2 \pi}\left[\frac{2}{1+n}(\sin ((1+n) \alpha))-\frac{2}{1-n}(\sin ((1-n) \alpha))\right] \\
& (\text { for } n=3,5, \ldots)
\end{align*}
$$

The maximum and rms values of the voltage and current waveforms for individual harmonics can be expressed as:

$$
\begin{align*}
& V_{n(\max )}=\sqrt{a_{n}^{2}+b_{n}^{2}} \\
& V_{n(r m s)}=\frac{\sqrt{a_{n}^{2}+b_{n}^{2}}}{\sqrt{2}} \\
& I_{n(\max )}=\frac{V_{n(\max )}}{R} \\
& I_{n(r m s)}=\frac{V_{n(r m s)}}{R}
\end{align*}
$$

The power factor of such non-linear load (as the one shown in Fig. 4.6) can be plotted against the triggering angle $\alpha$ using equations 4.6 to 4.10 . As it is shown in Fig. 4.8, the power factor decreases as the triggering angle of the thyristor increases. Obviously such circuits are used to control the output voltage applied to a load and this is achieved through the variation of the triggering angle. This mean that the power factor is likely to be very poor in such applications.


Fig. 4.8: Power factor at different triggering angles in ac voltage controller

The automatic power factor compensation can be used to improve the PF in such non-linear load. However, it is important to reemphasise the definition of the PF in non-linear loads as was explained in details in Chapter 2, equation 1.6. In that section the power factor in non-linear load was defined the as the product of the distortion factor and the displacement factor. The automatic PF compensation can improve the displacement factor which is 'cos' the angle between the fundamental component of the voltage and current waveforms. This displacement factor is created because of the triggering effect of the thyristors [2, 6, 7, 20]. However the distortion part of the PF cannot be improved with the automatic compensation. This component can be improved through the use of passive or active filters, which is outside the scope of this thesis. Fig. 4.9 illustrates the improvement in the displacement factor after using the automatic PF compensator. The compensator generates a variable reactive current to match the displacement angle between the fundamental current and voltage components, i.e for each triggering angle the automatic compensator (through the control of the switching duty cycle) generates the appropriate reactive current.


Fig. 4.9: Displacement factor before and after the use of the automatic PF compensation

The total PF after the improvement in the displacement factor is re- calculated using equations 4.6 to 4.10. The improvement in the PF is illustrated in Fig. 4.10.


Fig. 4.10: Power Factor before and after the use of the automatic PF compensation

Obviously the PF can be improved further through the use of passive/active filters as mentioned before, but the main objective of this work is to focus on the displacement improvement.

For each triggering angle the value of the capacitor is worked to find out the optimum improvement in the displacement factor. The value of the compensated capacitor is worked as follow:

1) The Fourier coefficients of the fundamental current component ( $a_{1}$ and $b_{1}$ ) are worked out from equations 4.11 and 4.13 for each triggering angle.
2) The phase angle of the fundamental component is worked out from the Fourier coefficients.
3) The value of the compensating capacitor current, $\mathrm{i}_{\mathrm{c}}$, is calculated based on the graph shown in Fig. 4.11


Fig. 4.11: Phasor diagram of the fundamental and compensated currents with respect to the supply voltage.
4) The value of ' $C$ ' is evaluated from the following equations

$$
\begin{aligned}
& X_{c}=v_{\text {supply }} / i_{c} \\
& C=1 /\left(2 \pi f X_{c}\right)
\end{aligned}
$$

The above steps is carried out for each triggering angle (steps of $1^{\circ}$ ) and the graph show in Fig. 4.12, illustrates the variation of the required compensated capacitor for each triggering angles [6]. It can be seen from this graph that the maximum capacitance required for the optimum compensation occurs at $90^{\circ}$. Such variable
capacitance is generated from the automatic compensator circuit as was described in Chapter 3.


Fig. 4.12: Compensated capacitor values vs triggering angle in A.C voltage controller.

Figs. 4.13, 4.14, and 4.15 shows the improvement achieved in the power factor at three different angles $\left(45^{\circ}, 90^{\circ}\right.$, and $135^{\circ}$ ) of the ac voltage controller. The value of the compensated capacitor is worked out for each of the three triggering angles and implemented in PSpice in order to see the improvement on the power factor. The figures show the transient and the steady state behaviour of the circuit, however the improvement should only be considered at the steady state; i.e. towards the end of the graph.


Fig. 4.13: Power Factor at $\alpha=45^{\circ}$
$\qquad$ Without correction capacitor
__ With correction capacitor ( $0.36 \mu \mathrm{~F}$ )


Fig. 4.14: Power Factor at $\alpha=90^{\circ}$
__ Without correction capacitor
__ With correction capacitor $(0.72 \mu \mathrm{~F})$


Fig. 4.15: Power Factor at $\alpha=135^{\circ}$
$\qquad$ Without correction capacitor With correction capacitor ( $0.36 \mu \mathrm{~F}$ )

The supply current before and after compensation for $\alpha=135^{\circ}$ is shown in Fig. 4.16. It can be seen from this figure the effect of the capacitor in the waveshape of the input current waveform.


Fig. 4.16: Input current waveform $\alpha=135^{\circ}$
__ Without correction capacitor
__ With correction capacitor ( $0.36 \mu \mathrm{~F}$ )

### 4.4 Summary

In this chapter the power factor in linear and non-linear loads was investigated and the automatic power factor correction circuits was implemented in order to improve the power factor. In linear loads the automatic compensator circuit was successfully used in achieving a unity power factor, since there is no distortion factor component in linear loads. However, in non-linear loads although the displacement factor was improved to unity, but the total power factor was not improved to unity and that is due to the fact that the automatic compensator circuit only compensates the angle of the fundamental component. The control, driver and snubber circuits used are discussed in details in the next chapter.

## Chapter 5

Control and Protection of the Proposed Compensator

### 5.1 Introduction

In chapter 3 and 4 the theory and implementation of the proposed compensator were introduced. Topics like the control strategy, drive circuits and devices protection were not covered in order to focus on the concept of the proposed compensator.

This chapter is mainly divided into two parts. The first one deals with use of microprocessor to control proposed compensator circuit, and experimental result involved in this work.

The second part deals with power losses in the proposed compensator circuit and the overall efficiency.

### 5.2 Control Circuit

The rapid growth in the microprocessor technology, lower prices and their flexibility make microprocessors ideal for many power electronic application circuits. In particular the flexibility required in controlling the power factor compensator can be achieved by storing the appropriate switching pattern in the microprocessor memory. A microprocessor in general is an integrated - circuit computer, a computer on a chip, and it represent an advanced kind of integrated circuit available. Microprocessors are essentially computer central processing units (CPUs), included an arithmetic unit, several registers, hardware stack implementation, on-chip memories (both RAM and ROM), and analogue input/output (I/O). Not all microprocessor include memory and I/O some have been optimised for computational speed and elegance, where others have been designed for simple applications where a minimum of 'support chips' is desirable.

Microprocessor can control the pattern required for the PF compensator by offering the suitable triggering pulses which depends on the frequency and the duty cycle $(\lambda)$. This is achieved through a fast, accurate and above all a flexible programme $[3,21$, 24].

### 5.3 Software Design

The triggering pulses depend on the switching angles and they are evaluated for each triggering angle and then stored in suitable addresses in the microprocessor EPROM. When the value of triggering angle is entered through the keyboard, the program searches for the corresponding switching angles and waits until the zero crossing pulse arrive through the interrupt (which indicates the beginning of the repetitive cycle of the program). The program is then executed and the required control pulses are transmitted to the drive circuits through the output port. The flowchart illustrated in Fig.5.1 shows the procedure used for generating the switching pulses.

The calculated switching angles are stored in the microprocessor memory and the pulses are then generated from the output port as two anti-phase signals. These two signals are practically the input signals to the driving circuits. Each switch has its own driving circuit, which is mainly to isolate the MOSFET sources from each others. The semiconductor switches used have a finite rising and falling times. If the two switches in the compensator circuit are overlapped, that will cause a circulating current between the two capacitors with nothing limiting this current except the internal resistance of the switches and capacitors. This can lead to a very high dv/dt across the switches and hence damaging them. If a dead-period is generated between the two switches in order to eliminate such problem, that will result on the inductor current being open circuit and that will equally damage on of the two switches due to a very high di/dt [20]. In order to avoid such high dv/dt or high di/dt a third branch consists of a semiconductor switch and a resistor is introduced in order to smooth the transfer between the two main switches. The pattern for the $3^{\text {rd }}$ branch could be generated from the microprocessor however for more efficient and accurate control, the microprocessor is only used to generate the main switching pattern and a separate analog circuit is used to generate the related switching patterns as shown in Fig. 5.3.


Fig. 5.1: Flowchart used in generating the switching pulses



Fig. 5.2: Block diagram of the experimental setup


Fig. 5.3: Practical implementation of the dead zone and complementary switching function generator

### 5.4 Zero Crossing Detector

A zero crossing detector or a phase locked loop is essential to synchronize the generated switching pattern with the supply voltage. The control pulses can be shifted through the software program stored in the EPROM of the microprocessor. This is required in order to operate the circuit in a closed loop mode. As for open loop mode the phase angle of the switching pattern can be controlled through shifting the zero crossing pluses which controls the beginning of the program.

The switching pattern for each value of convertor triggering angle ' $\alpha$ ' is evaluated and stored in the EPROM and the required switching pattern is set via the keyboard.

The microprocessor is capable of generating switching pulses for all three switches. The main pulses is generated to control $s_{1}$, complementary switching pulses is generated for $s_{2}$, and overlap pulses for $s_{3}$ on individual bases. However, it is more efficient if the microprocessor is used to generate switching pulses only for $\mathrm{s}_{1}$ and a logic circuit convert these switching pulses to complementary and overlap pulses for $\mathrm{s}_{2}$ and $\mathrm{s}_{3}$ as shown in Fig. 5.3.

### 5.5 Drive Circuits

Although MOSFETs are voltage driven devices, and they can be easily controlled from the output of the microprocessor, however, it is recommended to use appropriate drive circuits for the following reasons:

- The MOSFET switches are in the power circuit and they handles high voltage (mains) and they also carry the main reactive current. This could be very risky situation as if something goes wrong with the MOSFETs that may affect the expensive microprocessor circuit which is mainly a low power low voltage circuit.
- Each MOSFET switch is controlled through applying pulses between the gate and the source of this MOSFET. If the pulses are coming straight from the microprocessor that means that they will all be sharing the same ground. This is not acceptable as each MOSFET should have its own ground connected to separate sources.

For the above two reasons a drive circuit is required to act as a buffer between the microprocessor and the MOSFETs and also to drive the MOSFETs into hard saturation so that the voltage across them is almost zero when they are fully on and the current is almost zero when they are fully off. There are so many drive circuits which can be used for such applications. The circuit shown in Fig. 5.4 is the one used in the practical setup. It consists of an opt-isolator chip (6N137) and driver chip (ICL7667). The reason for the opt-isolator is to isolate the microprocessor from the MOSFETs and also to create different grounds for each MOSFET.


Fig. 5.4: Schematic Diagram of the MOSFET
Driver Circuit

### 5.6 MOSFET Protection

MOSFETs used in the proposed circuit are subjected to high di/dt and high dv/dt. In order to remove or at least to reduce the stress from the MOSFETs, a snubber circuits are used to divert the power loss from the MOSFETs into an external resistor. Snubber are small network of parts in the power switching circuits whose function is to control the effects of reactances, enhance the performance of the switching circuits and resulting in higher reliability and efficiency. However, the main
intent of a snubber is to absorb energy from the reactive element in the circuit and to release stress from the semiconductor switch [2, 6, 20].

When a snubber is properly designed and implemented, the switch will have lower average power dissipative, lower operating voltage and current and this consider valuable technique to reduce the device's switching loss by modifying the switching waveform through adding passive component to the load circuit.

In order to understand the operation of the snubber circuit the voltage $\mathrm{v}_{\mathrm{s}}(\mathrm{t})$ and current $i_{s}(t)$ across and through the switch are plotted in function of time as shown in Fig. 5.5-a. They can also be plotted against each other as locus diagram as shown in Fig. 5.5-b. In common with the waveform from which it is derived, the shape of the locus depends on both the switching device and the load circuit. The switchinglocus representation is useful because by using the same axes two other plots can be drawn. Since power is defined by ' $\mathrm{p}=\mathrm{vi}$ ', every point on the $\mathrm{v}_{\mathrm{s}}-\mathrm{i}_{\mathrm{s}}$ plane has a power associated with it. Curves joining points of equal power $p_{s}$ may be ploted. The higher the power, the farther the curve lies from the origin. Zero power is dissipated at points lying on the axes $\mathrm{v}_{\mathrm{s}}=0$ and $\mathrm{i}_{\mathrm{s}}=0$. In order to minimise the switching loss, the switching locus should lie as close to the axes as possible. Moreover, as $t$ change, the points tracing out the locus should pass as quickly as possible through the higher-power regions of the $v_{s}-i_{s}$ plane.

Every semiconductor switching device has ratings which must not be exceededvoltage, current, power, etc. The rating may be plotted on the $v_{s}-i_{s}$ plane to enclose what is known as the 'the safe operating area' (SOA) of the device, as shown in Fig. $5.5-\mathrm{c}$. It is important that the switching locus lies within the SOA or the switching device will be overstressed and may fail.


Fig. 5.5: (a) Switching waveform; (b) Switching locus; (c) Safe operating area (SOA).

### 5.6.1 Switching Resistive Load

With a purely resistive load fed from a voltage V, Fig.5.6, the switch current and voltage are related by ohm's law. The switching locus is
$i_{s}\left(v_{s}\right)=\left(v_{s}\right)\left(i_{s}\right) / R$
Which is simply a straight line between the ON point $(0, I)$, where $I=V / R$, and the OFF point $(\mathrm{V}, 0)$. It is convenient to assume that the semiconductor switch causes it to change linearly during the switching interval $t_{r}$ and $t_{f}$. The switching locus for $a$ resistive load is then traversed at a constant speed.

By integrating $v_{s}(t)$. $i_{s}(t)$ over the interval $t_{r}$ and $t_{f}$ it can found that the energy dissipated during tune-on as $1 / 6 \mathrm{VIt}_{r}$ and during turn-off as $1 / 6 \mathrm{VIt}_{f}$. Thus the total switching loss is

$$
\mathrm{P}_{\mathrm{s}}(\mathrm{sw})=\mathrm{VI}\left(\mathrm{t}_{\mathrm{r}}+\mathrm{t}_{\mathrm{f}}\right) / 6 \mathrm{~T}
$$



Fig. 5.6: Switching a resistive load. (a) circuit diagram; (b) Switching locus

### 5.6.2 Switching Inductive Load

The important case of a highly inductive load as shown in Fig. 5.7 The inductive is so large that it maintains virtually constant current ' $I$ ' throughout the switching cycle. Usually there will be a diode to provide a path for 'l' when the switch is open. The voltage across a diode must remain at zero as long as any current is flowing through it. So during $t_{r}$ and $t_{f}$, the switch and the diode are each carrying part of the current ' I ', with $S$ having to support the whole of V . For this case the switching loss may be found as

$$
\mathrm{P}_{\mathrm{s}}(\mathrm{sw})=\mathrm{VI}\left(\mathrm{t}_{\mathrm{r}}+\mathrm{t}_{\mathrm{f}}\right) / 2 \mathrm{~T}
$$


(b)


Fig. 5.7: Switching an inductive load. (a) Voltage and current waveforms; (b) Switching locus

### 5.6.3 Dissipative Snubber for Inductive Loads

The simplest form of snubber is dissipative. They contain resistors and therefore inefficient. Typically the snubber may dissipate power in the order of $5 \%$ of the converter's throughout. Often such inefficiency is tolerated because, in effect, heat is transferred from delicate switching devices to the rugged snubber resistors, improving the reliability and decreasing the cost of the circuit as a whole [6, 7].

### 5.6.4 Turn-on Snubber

The turn-on snubber of Fig. 5.8 Operates as follows. Initially no current flows in ' S ' and the small snubber inductance $L$. As the current through ' S ' rises during $\mathrm{t}_{\mathrm{r}} \mathrm{a}$ voltage $\mathrm{V}_{\mathrm{L}}=\mathrm{Ldi} \mathrm{s}_{\mathrm{s}} / \mathrm{dt}$ is developed across ' L '. Assuming again that $\mathrm{i}_{\mathrm{s}}$ increases linearly with $\mathrm{t}, \mathrm{v}_{\mathrm{L}}=\mathrm{LI} / \mathrm{tr}$ can be found. If L is chosen so that $\mathrm{v}_{\mathrm{L}}=\mathrm{v}$, there will be zero voltage developed across the switch ' S ' during $\mathrm{t}_{\mathrm{r}}$, giving zero turn on loss in the switching device. The switching locus for this network is shown in Fig. 5.9.


Fig. 5.8: Turn-on snubber network for an inductive load. (a) Circuit diagram; (b) Voltage and current waveforms



Fig. 5.9: The switching locus for turn-on snubber

Energy of $1 / 2 L I^{2}$ is stored in $L$ and must be removed (during $t_{\text {off) }}$ ) so that the snubber is reset by the start of the next cycle. The simplest way to do this is to add a blocking diode $D_{1}$ and a resistor $R$, which dissipates the energy as heat. The current in $L$ decays exponentially when the switch is open. The value of $R$ is not critical, but two factors restrict it:

The time-constant L/ R must be short enough that the current can decay sufficiently during $\mathrm{t}_{\text {off. }}$. If 3 time-constants are allowed, the current will have decayed to $1 / 20$, and hence the stored energy will have decayed to a negligible $1 / 400$ of its initial value.

Immediately after $S$ has opened it sees a voltage $V+I R$ across it, greater than the unsnubbed voltage, V . The voltage rating of ' S ' must therefore be increased relative to the unsnubbed case.

The power dissipated in $S$ during $t_{r}$ is ideally $P_{s}(r)=0$. The power dissipated in $R$ is simply the stored energy multiplied by the switching frequency $1 / T$, i.e.
$\mathrm{P}_{\mathrm{s}(\mathrm{r})}+\mathrm{P}_{\mathrm{R}}=\mathrm{P}_{\text {out }}=\mathrm{VIt}_{\mathrm{r}} / 2 \mathrm{~T}$
Note that this is independent of the value of $R$.
If $L$ is smaller than its optimum value some power will be dissipated in $S$ but correspondingly less will be dissipated in R. The total loss $P_{s}(r)+P R$ remains the same. On the other hand if $L$ is larger than its optimum value, the power dissipated in S stays at zero while the dissipation in R increases. These relationships are shown
in Fig. 5.10, where $P_{0}$ is the unsnubbed turn-on loss. The optimum value $L_{\text {opt }}=\mathrm{Vt}_{\mathrm{r}} / \mathrm{l}$ ensures that all of the turn-on loss is transferred from the switching device to the snubber resistor, with no extra loss incurred. For $L \leq L_{\text {opt }}$,
$\mathrm{P}_{\mathrm{S}}+\mathrm{P}_{\mathrm{R}}=\mathrm{P}_{\mathrm{o}}=\mathrm{VIt}_{\mathrm{r}} / 2 \mathrm{~T}$
This circuit is often known as an RLD snubber, after the components used.

### 5.6.5 Turn-off Snubber

The turn-off snubber of Fig. 5.10 operates as follows. Initially current ' 1 ' is flowing in $S$ and the small snubber capacitance $C$ is uncharged. As the current through $S$ decreases, $C$ and $D_{1}$, provides an alternative path for balance of $I$, and $D_{2}$ remains reverse-biased. Assuming that $I_{s}$ falls linearly during $T_{f}$ we have $\mathrm{i}_{\mathrm{s}(\mathrm{t})}=\mathrm{l}\left(1-\mathrm{t} / \mathrm{t}_{\mathrm{f}}\right)$, where the time origin has been taken at the start of turn-off. The current flowing into C therefore increases linearly according to $i_{c}=/ t / t_{f}$. Putting this into the capacitance equation " $\mathrm{i}=\mathrm{Cdv} / \mathrm{dt}$ "and integrating, the capacitor voltage waveforms can be expressed as:

$$
\mathrm{V}_{\mathrm{c}}(\mathrm{t})=\frac{1}{C} \int_{0}^{t} I \frac{t}{t_{f}} \mathrm{dt}+\mathrm{V}_{\mathrm{c}}(0)=I \frac{\mathrm{t}^{2}}{2 \mathrm{Ct}_{\mathrm{f}}}
$$

Thus $\mathrm{V}_{\mathrm{C}}$, and hence $\mathrm{V}_{\mathrm{S}}$ rises parabolically from $\mathrm{V}_{\mathrm{C}}(0)=0$ to $\mathrm{V}_{\mathrm{c}}\left(\mathrm{t}_{\mathrm{f}}\right)=\mathrm{It}_{\mathrm{f}} / 2 \mathrm{C}$ the end of turn-off. (Assumed that C is large enough that $\mathrm{v}_{\mathrm{C}}\left(\mathrm{t}_{\mathrm{f}}\right)<\mathrm{V}$; if not, the above analysis must be modified.) The energy dissipated in $S$ during turn-off can be found by integrating $P_{s}(t)=v_{s}(t)$. $\mathrm{i}_{\mathrm{s}}(\mathrm{t})$ over the interval $\mathrm{t}_{\mathrm{f}}$. Since $\mathrm{D}_{1}$ is conducting, $\mathrm{v}_{\mathrm{S}}=\mathrm{v}_{\mathrm{c}}$ and we have

$$
\mathrm{W}=\int_{0}^{t_{r}} I \frac{\mathrm{t}_{\mathrm{r}}^{2}}{2 \mathrm{Ct}_{\mathrm{f}}} \cdot I\left\{1-\frac{t}{t_{f}}\right\} \mathrm{dt}=\frac{I^{2}}{24 \mathrm{C}} t_{f}^{2}
$$

Subsequently $C$ is charged at the full choke current I until $V_{C}$ reach $V$, at which point $D_{2}$ becomes forward-biased and conducts the whole of $I$.

Energy of $1 / 2 C V^{2}$ is stored in $C$ and must be removed (during $t_{o n}$ ). The simplest way to do this is to add $D_{1}$ and $R$ to the snubber. The voltage across $C$ decays exponentially when the switch is closed. The value of $R$ is not critical but two factors restrict it:

- The time-constant CR must be short enough that $\mathrm{V}_{\mathrm{C}}$ can decay to a negligible value during $\mathrm{T}_{\text {on }}$. Once again 3 time-constants will be sufficient.
- Immediately after the switch closes, it passes a current of I + V/R, greater than the unsnubbed current, I. The current rating of $S$ must therefore be increased relative to the unsnubbed case.

The turn-off loss in S is found by multiplying W of eq. ... by the switching frequency:

$$
\mathrm{P}_{\mathrm{s}(\mathrm{f})}=\frac{I^{2}}{24 C} t_{f}^{2}
$$

The power dissipated in $R$ is the stored energy multiplied by the switching frequency, and again, this is independent of $R$ :
$\mathrm{P}_{\mathrm{R}}=C \mathrm{~V}^{2} / 2 \mathrm{~T}$
If a full analysis of the turn-off snubber is carried out, it will be found that the total turn-off loss $\mathrm{Ps}_{(f)}+\mathrm{P}_{\mathrm{R}}$ follows a curve as shown in Fig. 5.11. Here $\mathrm{P}_{0}=\mathrm{VIt}_{f} / 2 \mathrm{~T}$, the unsnubbed turn-off loss. The choice of an optimum snubber capacitance $\mathrm{C}_{\mathrm{opt}}$ is not as obvious the choice of $\mathrm{L}_{\text {opt }}$ was, but two possibilities are:

- Choose $C_{\text {opt }}$ to minimise the total turn-off loss: $C_{\text {opt }(1)}=0.22 \mathrm{I} \mathrm{t}_{\mathrm{f}} / \mathrm{V}$. Then P $P_{s(f)}=0.33 P_{0}$ and $P_{R}=0.22 P_{0}$ (With this rather small value of capacitance, $\mathrm{V}_{\mathrm{C}}$, rises to V at $0.67 \mathrm{t}_{\mathrm{f}}$ and stays there during the remainder of the turn-off interval; the analysis above is invalid since it was assumed that $\left.\mathrm{V}_{\mathrm{C}}\left(\mathrm{t}_{\mathrm{f}}\right)<\mathrm{V}\right)$.
- Choose $C$ opt to minimise the loss in $S$ without increasing the total loss above $\mathrm{P}_{0}: \mathrm{C}_{\text {opt(2) }}=0.91 /_{\text {tf }}$ Then $\mathrm{P}_{\mathrm{s}(\mathrm{f})}=0.09 \mathrm{P}_{0}$ and $\mathrm{P}_{\mathrm{R}}=0.91 \mathrm{P}_{0}$. With this choice $\mathrm{V}_{\mathrm{C}}$ rises to $=0.55 \mathrm{~V}$ at $\mathrm{t}_{\mathrm{f}}$.

This circuit is often known as RCD snubber, and is frequently met within power electronic switching circuits.

Turn-off snubber


Fig. 5.10: Turn-off snubber network for an inductive load


Fig. 5.11: Turn-off switching losses as a function of the snubber capacitance.

### 5.6.6 Turn-off / Turn-on Snubber

To snub both turn-on and turn-off, both of the above circuits can be incorporated or the combined snubber can be used. The values of $C$ and $L$ are determined as before. R must now be able to dissipate the sum of the turn-on PR and the turn-off $P R$. The value of $R$ must be chosen with care as it forms part of both the turn-on and turn-off snubbers.

In practice, snubber design is an exercise in compromise.
The values of $L$ and $C$ may be chosen either on loss considerations as above, or to shape the switching locus to keep it within the SOA of the switching device. In the latter case the values of $L$ and $C$ might tend to be larger than the "optimum" values indicated above.

In most applications the load current I is usually not fixed but can vary over a wide range. The supply voltage V can also vary. Since both V an I appear in the formulae for $L$ and $C$, the "optimum" snubber components depend on the circuit conditions. In
practice the snubbers are often designed for nominal operating conditions (e.g., full rated output) then adjusted empirically to obtain satisfactory performance over the whole operating range.

When designing the turn-on snubber for an inductive load, charge storage in the freewheel diode should be taken into account. An important effect of the snubber inductance is to limit the reverse recovery current of the diode.

In a transformer-coupled converter it may be necessary to have snubber components on the primary side (associated with the switch) and an RC damping network on the secondary side (associated with the rectifiers). The two networks will interact their values may have to be adjusted empirically. There may be no need for a turn-on snubber though, because the transformer will often possess enough leakage inductance to have some snubbing effect.

There is a good proportion of art as well as some science in the design of snubber networks!

### 5.7 Summary

In this chapter, the control of the compensator is discussed. The use of the microprocessor to produce the switching patter for controlling the MOSFET switches is discussed. The microprocessor was mainly set to generate the main control pulses and then a hardware circuit was used to generate the required overlapping pulses.

In order to operate the MOSFETs safely and efficiently, drive circuits have been designed and used as a buffer between the microprocessor and the MOSFET switches. A separate driver circuit was used for each MOSFET in order to ensure a complete isolation between the switches.

The control signals have to be synchronised with the mains in order to make sure that the compensator is generating the correct reactive current at the correct instant. This is achieved through the use of a zero crossing detector.

Finally in order to protect the MOSFET switches and in order to remove the stress caused to the switch during the turning on and turning off, a snubber circuits were designed to divert the losses from the MOSFETs to an external resistor. The design
and analysis of the turn-on and turn-off snubber circuits are covered in details in this chapter.

## Chapter 6

Conclusions and Future Work

### 6.1 Conclusions

The main aim of this thesis is to develop an automatic power factor compensation which can be used in any types of linear and non-linear loads. Such compensator is needed especially with large number of low power non-linear loads. The proposed compensator can be used in shunt in conjunction with all types of loads. In principle there is no power limit for the proposed compensator, and the same idea can be applied for any power range. However, the compensator uses relatively fast semiconductor switches (MOSFETs) and the voltage and current ratings for such devices is still limited to low power applications. Gate Turn Off Thyristors (GTOs) can be used for high power applications and such devices will be used in the same configuration exactly the same way as the MOSFETs that are used in the proposed compensator [ 2,8,14,].

The compensator circuits are analysed, simulated and practically constructed, controlled and tested. The compensator generates the required reactive power which is needed to improve the power factor for any type of loads. The simulation package used to simulate the proposed compensator is PSpice. The reason of using this software is that it simulates at 'low level', i.e. as close to the practical setting as possible. For example, when MOSFET is used in the simulation, the characteristics of the simulated MOSFET are almost identical to the characteristics of the actual one.

The main advantage of the compensator is its ability to generate a smooth leading as well as lagging reactive power using only two capacitors and two switches. This is achieved through controlling the duty cycle of the semiconductor switches [6, 16,17]. The duty cycle is controlled via an 8085 microprocessor which gives flexibility as well as the speed of control. The implementation of the proposed circuit has to be considered carefully, for example issues like driving and protecting the MOSFETs has to be fully investigated before the practical work. The investigation, design, and implementation of such circuits are fully covered in the thesis.

### 6.2 Future Work

In fact the research work which was introduced in this thesis has in turn created more future research work compared to the original one which was intended to cover. However this is the nature of research. The following future research points which spun from this work and needs to be investigated further could be summarised in the following points:

- The compensator should be tested on high power loads, that could means the use of high power devices such as forced commutated thyristors of Gate Turn-Off Thyristors (GTOs). Obviously the design of the protection circuit has to be worked out as the dv/dt and di/dt will be much higher in this case. Also issue like Electromagnetic Compatibility (EMC) has to be fully investigated.
- Although the resonance phenomena has been briefly investigated when the compensator was designed, a more in-depth investigation is required particularly if the compensated capacitor (effective value) resonates with the supply impedance at the switching frequency.
- The proposed compensator focused mainly for improving the displacement component of the power factor. The distortion component was outside the scope of this research work. Future work could develop the compensator so that it contains an element of active filter which can be used to compensate for both the displacement as well as the distortion components of the power factor.
- So far the controller used was an external controller. The use of a single chip controller could be investigated further in such application. In that case the controller could be integrated within the compensator and the whole circuit would be wholly compatible.


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## APPENDIX A

Saving due to PF Improvement in small industrial customer [1]

The table below shows typical monthly billing information which is used to calculate the penalty imposed by the utility and the cost analysis of improving the site power factor to 0.95 .

Table A. 1

| Month | Power <br> Factor | Actual <br> KW <br> Demand | KVAR <br> Required | KW Billing Demand <br> Before <br> Correction | After <br> Correction | Before <br> Correction(\$) | After <br> Correction(\$) | Demand <br> Saving <br> $(\$)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0.74 | 228 | 132 | 293 | 228 | 1244 | 969 | 275 |
|  | 0.7 | 241 | 167 | 327 | 241 | 1390 | 1024 | 366 |
| Mar | 0.72 | 233 | 148 | 307 | 233 | 1307 | 990 | 316 |
| Apr | 0.71 | 256 | 170 | 343 | 265 | 1466 | 1088 | 368 |
| May | 0.7 | 219 | 151 | 297 | 219 | 1263 | 931 | 332 |
| Jun | 0.69 | 274 | 197 | 377 | 274 | 1603 | 1165 | 439 |
| July | 0.68 | 281 | 211 | 393 | 281 | 1668 | 1194 | 474 |
| Aug | 0.67 | 261 | 203 | 370 | 261 | 1573 | 1109 | 464 |
| Sep | 0.72 | 238 | 151 | 314 | 238 | 1335 | 1012 | 323 |
| Oct | 0.74 | 232 | 136 | 298 | 232 | 1266 | 986 | 280 |
| Nov | 0.72 | 245 | 156 | 323 | 245 | 1374 | 1041 | 333 |
| Dec | 0.71 | 247 | 164 | 330 | 247 | 1405 | 1050 | 355 |

Total 16,883 12,559

## APPENDIX B

Result of Calculations of $\mathrm{C}_{\text {eff }}$ against $\boldsymbol{\lambda}$

## CALCULATION

Depending on the following equation which expresses the relationship between capacitor value ( $\mathrm{C}_{\text {eff }}$ ) and C1 \& C2 and lambda ( $\lambda$ ).
$C_{\text {eff }}=C 1 /\left\{(\lambda * \lambda)+\left(x^{*} x\right) k\right\}$
, where $\mathrm{x}=1-\lambda \quad$ and $\mathrm{k}=\mathrm{C} 1 / \mathrm{C} 2$
By using the Excel program, we can calculate the values of the effective capacitor. As it is clear from table below, we also, could find the capacitive impedance and to get more accurate values, we included the values of series circuit ( $\mathrm{R}-\mathrm{L}$ ) in our calculation, like inductive impedance ( XI ) and the resistance( R ) and in our case we consider:
$\mathrm{L}=5 \mathrm{mh}, \mathrm{R}=1 \Omega$, then C 1 has been increased by 10uf up to 100 uf as shown at following tables:
calculation at C1=10uf

| Lambda( $\lambda$ ) | C1 | $\lambda^{*} \lambda$ | $\begin{aligned} & x=1- \\ & \lambda \end{aligned}$ | $x^{*} x$ | $\left(x^{*} \mathrm{x}\right)^{*} 0.1$ | $\left(\lambda^{*} \lambda\right)+\left(x^{*} x\right)^{*} 0.1$ | C | Xc | XI | Xeff | Ceff |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.00001 | 0 | 1 | 1 | 0.1 | 0.1 | 0.0001 | 31.83102 | 6.28318 | 25.5674 | 0.000124 |
| 0.1 | 0.00001 | 0.01 | 0.9 | 0.81 | 0.081 | 0.091 | 0.00011 | 28.96622 | 6.28318 | 22.70508 | 0.00014 |
| 0.2 | 0.00001 | 0.04 | 0.8 | 0.64 | 0.064 | 0.104 | $9.62 \mathrm{E}-05$ | 33.10426 | 6.28318 | 26.83971 | 0.000119 |
| 0.3 | 0.00001 | 0.09 | 0.7 | 0.49 | 0.049 | 0.139 | $7.19 \mathrm{E}-05$ | 44.24511 | 6.28318 | 37.9751 | $8.38 \mathrm{E}-05$ |
| 0.4 | 0.00001 | 0.16 | 0.6 | 0.36 | 0.036 | 0.196 | 5.1E-05 | 62.38879 | 6.28318 | 56.11452 | $5.67 \mathrm{E}-05$ |
| 0.5 | 0.00001 | 0.25 | 0.5 | 0.25 | 0.025 | 0.275 | 3.64E-05 | 87.53529 | 6.28318 | 81.25827 | 3.92E-05 |
| 0.6 | 0.00001 | 0.36 | 0.4 | 0.16 | 0.016 | 0.376 | $2.66 \mathrm{E}-05$ | 119.6846 | 6.28318 | 113.4058 | $2.81 \mathrm{E}-05$ |
| 0.7 | 0.00001 | 0.49 | 0.3 | 0.09 | 0.009 | 0.499 | 2E-05 | 158.8368 | 6.28318 | 152.5569 | 2.09E-05 |
| 0.8 | 0.00001 | 0.64 | 0.2 | 0.04 | 0.004 | 0.644 | $1.55 \mathrm{E}-05$ | 204.9917 | 6.28318 | 198.7111 | $1.6 \mathrm{E}-05$ |
| 0.9 | 0.00001 | 0.81 | 0.1 | 0.01 | 0.001 | 0.811 | $1.23 \mathrm{E}-05$ | 258.1495 | 6.28318 | 251.8683 | $1.26 \mathrm{E}-05$ |


calculation at $\mathrm{C} 1=20 \mathrm{uf}$

| lambda | C1 | $y^{*} y$ | $x=1-y$ | $x^{*} x$ | $\left(x^{*} x\right)^{*} 0.1$ | $\left(y^{*} y\right)+\left(x^{*} x\right)^{*} 0.1$ | $C$ | Xc | XI | Xeff | Ceff |
| ---: | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 0.00002 | 0 | 1 | 1 | 0.2 | 0.2 | 0.0001 | 31.83102 | 6.28318 | 25.5674 | 0.000124499 |
| 0.1 | 0.00002 | 0.01 | 0.9 | 0.81 | 0.162 | 0.172 | 0.000116 | 27.37467 | 6.28318 | 21.11519 | 0.00015075 |
| 0.2 | 0.00002 | 0.04 | 0.8 | 0.64 | 0.128 | 0.168 | 0.000119 | 26.73805 | 6.28318 | 20.4793 | 0.000155431 |
| 0.3 | 0.00002 | 0.09 | 0.7 | 0.49 | 0.098 | 0.188 | 0.000106 | 29.92115 | 6.28318 | 23.65912 | 0.000134541 |
| 0.4 | 0.00002 | 0.16 | 0.6 | 0.36 | 0.072 | 0.232 | $8.62 \mathrm{E}-05$ | 36.92398 | 6.28318 | 30.65711 | 0.000103829 |
| 0.5 | 0.00002 | 0.25 | 0.5 | 0.25 | 0.05 | 0.3 | $6.67 \mathrm{E}-05$ | 47.74652 | 6.28318 | 41.4754 | $7.6747 \mathrm{E}-05$ |
| 0.6 | 0.00002 | 0.36 | 0.4 | 0.16 | 0.032 | 0.392 | $5.1 \mathrm{E}-05$ | 62.38879 | 6.28318 | 56.11452 | $5.67253 \mathrm{E}-05$ |
| 0.7 | 0.00002 | 0.49 | 0.3 | 0.09 | 0.018 | 0.508 | $3.94 \mathrm{E}-05$ | 80.85078 | 6.28318 | 74.5743 | $4.26838 \mathrm{E}-05$ |
| 0.8 | 0.00002 | 0.64 | 0.2 | 0.04 | 0.008 | 0.648 | $3.09 \mathrm{E}-05$ | 103.1325 | 6.28318 | 96.85447 | $3.28649 \mathrm{E}-05$ |
| 0.9 | 0.00002 | 0.81 | 0.1 | 0.01 | 0.002 | 0.812 | $2.46 \mathrm{E}-05$ | 129.2339 | 6.28318 | 122.9548 | $2.58885 \mathrm{E}-05$ |


calculation atC1=30uf

| lambda | C1 | $y^{*} y$ | $x=1-y$ | $\mathrm{x}^{*} \mathrm{x}$ | $\left(x^{*} x\right)^{*} 0.1$ | $\left(y^{*} y\right)+\left(x^{*} x\right) * 0.1$ | C | Xc | XI | Xeff | Ceff |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0.00003 | 0 | 1 | 1 | 0.3 | 0.3 | 0.0001 | 31.831 | 6.28318 | 25.5674 | 0.000124 |
| 0.1 | 0.00003 | 0 | 0.9 | 0.8 | 0.243 | 0.253 | 0.0001 | 26.844 | 6.28318 | 20.58528 | 0.000155 |
| 0.2 | 0.00003 | 0 | 0.8 | 0.6 | 0.192 | 0.232 | 0.0001 | 24.616 | 6.28318 | 18.36006 | 0.000173 |
| 0.3 | 0.00003 | 0.1 | 0.7 | 0.5 | 0.147 | 0.237 | 0.0001 | 25.147 | 6.28318 | 18.88981 | 0.000169 |
| 0.4 | 0.00003 | 0.2 | 0.6 | 0.4 | 0.108 | 0.268 | 0.0001 | 28.436 | 6.28318 | 22.17509 | 0.000144 |
| 0.5 | 0.00003 | 0.3 | 0.5 | 0.3 | 0.075 | 0.325 | 9E-05 | 34.484 | 6.28318 | 28.21814 | 0.000113 |
| 0.6 | 0.00003 | 0.4 | 0.4 | 0.2 | 0.048 | 0.408 | 7E-05 | 43.29 | 6.28318 | 37.02051 | 8.6E-05 |
| 0.7 | 0.00003 | 0.5 | 0.3 | 0.1 | 0.027 | 0.517 | 6E-05 | 54.855 | 6.28318 | 48.58256 | $6.55 \mathrm{E}-05$ |
| 0.8 | 0.00003 | 0.6 | 0.2 | 0 | 0.012 | 0.652 | 5E-05 | 69.179 | 6.28318 | 62.90418 | 5.06E-05 |
| 0.9 | 0.00003 | 0.8 | 0.1 | 0 | 0.003 | 0.813 | 4E-05 | 86.262 | 6.28318 | 79.98512 | $3.98 \mathrm{E}-05$ |



|  |  |  |  |  |  | Calculaton at C1=40uf |  |  | L=20mh |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| lambda | C1 |  | $\begin{aligned} & x=1- \\ & y \end{aligned}$ | $x^{*} x$ | $\left(x^{*} x\right)^{*} 0.1$ | $\left(y^{*} y\right)+\left(x^{*} x\right)^{*} 0.1$ | C | Xc | XI | Xeff | Ceff |
| 0.1 | 0.00004 | 0.01 | 0.9 | 0.81 | 0.324 | 0.334 | 0.00012 | 26.5789 | 6.28318 | 20.3203 | 0.000157 |
| 0.2 | 0.00004 | 0.04 | 0.8 | 0.64 | 0.256 | 0.296 | 0.00014 | 23.555 | 6.28318 | 17.3007 | 0.000184 |
| 0.3 | 0.00004 | 0.09 | 0.7 | 0.49 | 0.196 | 0.286 | 0.00014 | 22.7592 | 6.28318 | 16.5063 | 0.000193 |
| 0.4 | 0.00004 | 0.16 | 0.6 | 0.36 | 0.144 | 0.304 | 0.00013 | 24.1916 | 6.28318 | 17.9363 | 0.000177 |
| 0.5 | 0.00004 | 0.25 | 0.5 | 0.25 | 0.1 | 0.35 | 0.00011 | 27.8521 | 6.28318 | 21.5921 | 0.000147 |
| 0.6 | 0.00004 | 0.36 | 0.4 | 0.16 | 0.064 | 0.424 | $9.4 \mathrm{E}-05$ | 33.7409 | 6.28318 | 27.4759 | 0.000116 |
| 0.7 | 0.00004 | 0.49 | 0.3 | 0.09 | 0.036 | 0.526 | 7.6E-05 | 41.8578 | 6.28318 | 35.5887 | 8.94E-05 |
| 0.8 | 0.00004 | 0.64 | 0.2 | 0.04 | 0.016 | 0.656 | $6.1 \mathrm{E}-05$ | 52.2029 | 6.28318 | 45.9306 | 6.93E-05 |
| 0.9 | 0.00004 | 0.81 | 0.1 | 0.01 | 0.004 | 0.814 | $4.9 \mathrm{E}-05$ | 64.7761 | 6.28318 | 58.5015 | $5.44 \mathrm{E}-05$ |



| calculation atC1=50uf |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (y)lambda | C1 | $y^{*} y$ | $\begin{aligned} & x=1- \\ & y \end{aligned}$ | $x^{*} x$ | $\left(x^{*} \mathrm{x}\right)^{*} 0.1$ | $\left(y^{*} y\right)+\left(x^{*} x\right)^{*} 0.1$ | C | Xc | XI | Xeff | Ceff |
| 0 | 0.00005 | 0 | 1 | 1 | 0.5 | 0.5 | 0.0001 | 31.831 | 6.283 | 25.5674 | 0.000124 |
| 0.1 | 0.00005 | 0.01 | 0.9 | 0.81 | 0.405 | 0.415 | 0.0001 | 26.42 | 6.283 | 20.16138 | 0.000158 |
| 0.2 | 0.00005 | 0.04 | 0.8 | 0.64 | 0.32 | 0.36 | 0.0001 | 22.918 | 6.283 | 16.66518 | 0.000191 |
| 0.3 | 0.00005 | 0.09 | 0.7 | 0.49 | 0.245 | 0.335 | 0.0001 | 21.327 | 6.283 | 15.0768 | 0.000211 |
| 0.4 | 0.00005 | 0.16 | 0.6 | 0.36 | 0.18 | 0.34 | 0.0001 | 21.645 | 6.283 | 15.39442 | 0.000207 |
| 0.5 | 0.00005 | 0.25 | 0.5 | 0.25 | 0.125 | 0.375 | 0.0001 | 23.873 | 6.283 | 17.61848 | 0.000181 |
| 0.6 | 0.00005 | 0.36 | 0.4 | 0.16 | 0.08 | 0.44 | 0.0001 | 28.011 | 6.283 | 21.75111 | 0.000146 |
| 0.7 | 0.00005 | 0.49 | 0.3 | 0.09 | 0.045 | 0.535 | 9E-05 | 34.059 | 6.283 | 27.794 | 0.000115 |
| 0.8 | 0.00005 | 0.64 | 0.2 | 0.04 | 0.02 | 0.66 | 8E-05 | 42.017 | 6.283 | 35.74775 | $8.9 \mathrm{E}-05$ |
| 0.9 | 0.00005 | 0.81 | 0.1 | 0.01 | 0.005 | 0.815 | 6E-05 | 51.885 | 6.283 | 45.61234 | $6.98 \mathrm{E}-05$ |


calculation at $\mathrm{C} 1=60$ uf

| lambda | C1 | $\lambda^{*} \lambda$ | $\begin{aligned} & x=1- \\ & \lambda \end{aligned}$ | $\mathrm{x}^{*} \mathrm{x}$ | $\left(x^{*} \mathrm{x}\right)^{*} 0.1$ | $\left(y^{*} y\right)+\left(x^{*} x\right)^{*} 0.1$ | C | Xc | XI | Xeff | Ceff |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.1 | 0.00006 | 0 | 0.9 | 0.8 | 0.486 | 0.496 | 0.0001 | 26.314 | 6.28318 | 20.05541 | 0.000159 |
| 0.2 | 0.00006 | 0 | 0.8 | 0.6 | 0.384 | 0.424 | 0.0001 | 22.494 | 6.28318 | 16.24155 | 0.000196 |
| 0.3 | 0.00006 | 0.1 | 0.7 | 0.5 | 0.294 | 0.384 | 0.0002 | 20.372 | 6.28318 | 14.12411 | 0.000225 |
| 0.4 | 0.00006 | 0.2 | 0.6 | 0.4 | 0.216 | 0.376 | 0.0002 | 19.947 | 6.28318 | 13.7008 | 0.000232 |
| 0.5 | 0.00006 | 0.3 | 0.5 | 0.3 | 0.15 | 0.4 | 0.0002 | 21.221 | 6.28318 | 14.97093 | 0.000213 |
| 0.6 | 0.00006 | 0.4 | 0.4 | 0.2 | 0.096 | 0.456 | 0.0001 | 24.192 | 6.28318 | 17.93629 | 0.000177 |
| 0.7 | 0.00006 | 0.5 | 0.3 | 0.1 | 0.054 | 0.544 | 0.0001 | 28.86 | 6.28318 | 22.59908 | 0.000141 |
| 0.8 | 0.00006 | 0.6 | 0.2 | 0 | 0.024 | 0.664 | 9E-05 | 35.226 | 6.28318 | 28.96041 | 0.00011 |
| 0.9 | 0.00006 | 0.8 | 0.1 | 0 | 0.006 | 0.816 | 7E-05 | 43.29 | 6.28318 | 37.02051 | 8.6E-05 |


calculation at $\mathrm{C}=70 \mathrm{uf}$

| 0.1 | 0.00007 | 0.01 | 0.9 | 0.81 | 0.567 | 0.577 | 0.0001 | 26.23785 | 6.28318 | 19.97971 | 0.000159 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0.2 | 0.00007 | 0.04 | 0.8 | 0.64 | 0.448 | 0.488 | 0.0001 | 22.19077 | 6.28318 | 15.93899 | 0.0002 |
| 0.3 | 0.00007 | 0.09 | 0.7 | 0.49 | 0.343 | 0.433 | 0.0002 | 19.68976 | 6.28318 | 13.44382 | 0.000237 |
| 0.4 | 0.00007 | 0.16 | 0.6 | 0.36 | 0.252 | 0.412 | 0.0002 | 18.73483 | 6.28318 | 12.49174 | 0.000255 |
| 0.5 | 0.00007 | 0.25 | 0.5 | 0.25 | 0.175 | 0.425 | 0.0002 | 19.32597 | 6.28318 | 13.08107 | 0.000243 |
| 0.6 | 0.00007 | 0.36 | 0.4 | 0.16 | 0.112 | 0.472 | 0.0001 | 21.4632 | 6.28318 | 15.21292 | 0.000209 |
| 0.7 | 0.00007 | 0.49 | 0.3 | 0.09 | 0.063 | 0.553 | 0.0001 | 25.1465 | 6.28318 | 18.88981 | 0.000169 |
| 0.8 | 0.00007 | 0.64 | 0.2 | 0.04 | 0.028 | 0.668 | 0.0001 | 30.37588 | 6.28318 | 24.11345 | 0.000132 |
| 0.9 | 0.00007 | 0.81 | 0.1 | 0.01 | 0.007 | 0.817 | $9 \mathrm{E}-05$ | 37.15134 | 6.28318 | 30.88436 | 0.000103 |


calculation at $\mathrm{C} 1=80 \mathrm{uf}$

| 0.1 | 0.00008 | 0.01 | 0.9 | 0.81 | 0.648 | 0.658 | 0.00012 | 26.18101 | 6.28318 | 19.92294 | 0.00016 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0.2 | 0.00008 | 0.04 | 0.8 | 0.64 | 0.512 | 0.552 | 0.00014 | 21.9634 | 6.28318 | 15.71208 | 0.000203 |
| 0.3 | 0.00008 | 0.09 | 0.7 | 0.49 | 0.392 | 0.482 | 0.00017 | 19.17819 | 6.28318 | 12.93372 | 0.000246 |
| 0.4 | 0.00008 | 0.16 | 0.6 | 0.36 | 0.288 | 0.448 | 0.00018 | 17.82537 | 6.28318 | 11.58543 | 0.000275 |
| 0.5 | 0.00008 | 0.25 | 0.5 | 0.25 | 0.2 | 0.45 | 0.00018 | 17.90495 | 6.28318 | 11.66471 | 0.000273 |
| 0.6 | 0.00008 | 0.36 | 0.4 | 0.16 | 0.128 | 0.488 | 0.00016 | 19.41692 | 6.28318 | 13.17175 | 0.000242 |
| 0.7 | 0.00008 | 0.49 | 0.3 | 0.09 | 0.072 | 0.562 | 0.00014 | 22.36129 | 6.28318 | 16.10918 | 0.000198 |
| 0.8 | 0.00008 | 0.64 | 0.2 | 0.04 | 0.032 | 0.672 | 0.00012 | 26.73805 | 6.28318 | 20.4793 | 0.000155 |
| 0.9 | 0.00008 | 0.81 | 0.1 | 0.01 | 0.008 | 0.818 | $9.8 \mathrm{E}-05$ | 32.54721 | 6.28318 | 26.28306 | 0.000121 |



C1=90uf

| 0.1 | 0.00009 | 0.01 | 0.9 | 0.81 | 0.729 | 0.739 | 0.000122 | 26.1368 | 6.28318 | 19.87879 | 0.00016013 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0.2 | 0.00009 | 0.04 | 0.8 | 0.64 | 0.576 | 0.616 | 0.000146 | 21.78656 | 6.28318 | 15.5356 | 0.00020489 |
| 0.3 | 0.00009 | 0.09 | 0.7 | 0.49 | 0.441 | 0.531 | 0.000169 | 18.7803 | 6.28318 | 12.53706 | 0.0002539 |
| 0.4 | 0.00009 | 0.16 | 0.6 | 0.36 | 0.324 | 0.484 | 0.000186 | 17.11801 | 6.28318 | 10.88088 | 0.00029254 |
| 0.5 | 0.00009 | 0.25 | 0.5 | 0.25 | 0.225 | 0.475 | 0.000189 | 16.7997 | 6.28318 | 10.56396 | 0.00030132 |
| 0.6 | 0.00009 | 0.36 | 0.4 | 0.16 | 0.144 | 0.504 | 0.000179 | 17.82537 | 6.28318 | 11.58543 | 0.00027475 |
| 0.7 | 0.00009 | 0.49 | 0.3 | 0.09 | 0.081 | 0.571 | 0.000158 | 20.19501 | 6.28318 | 13.94773 | 0.00022822 |
| 0.8 | 0.00009 | 0.64 | 0.2 | 0.04 | 0.036 | 0.676 | 0.000133 | 23.90863 | 6.28318 | 17.65379 | 0.00018031 |
| 0.9 | 0.00009 | 0.81 | 0.1 | 0.01 | 0.009 | 0.819 | 0.00011 | 28.96622 | 6.28318 | 22.70508 | 0.00014019 |


calculation at C1=C2=100uf

| 0.1 | 0.0001 | 0.01 | 0.9 | 0.81 | 0.81 | 0.82 | 0.000122 | 26.10143 | 6.28318 | 19.84347 | 0.00016 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0.2 | 0.0001 | 0.04 | 0.8 | 0.64 | 0.64 | 0.68 | 0.000147 | 21.64509 | 6.28318 | 15.39442 | 0.000207 |
| 0.3 | 0.0001 | 0.09 | 0.7 | 0.49 | 0.49 | 0.58 | 0.000172 | 18.46199 | 6.28318 | 12.21979 | 0.00026 |
| 0.4 | 0.0001 | 0.16 | 0.6 | 0.36 | 0.36 | 0.52 | 0.000192 | 16.55213 | 6.28318 | 10.31752 | 0.000309 |
| 0.5 | 0.0001 | 0.25 | 0.5 | 0.25 | 0.25 | 0.5 | 0.0002 | 15.91551 | 6.28318 | 9.684097 | 0.000329 |
| 0.6 | 0.0001 | 0.36 | 0.4 | 0.16 | 0.16 | 0.52 | 0.000192 | 16.55213 | 6.28318 | 10.31752 | 0.000309 |
| 0.7 | 0.0001 | 0.49 | 0.3 | 0.09 | 0.09 | 0.58 | 0.000172 | 18.46199 | 6.28318 | 12.21979 | 0.00026 |
| 0.8 | 0.0001 | 0.64 | 0.2 | 0.04 | 0.04 | 0.68 | 0.000147 | 21.64509 | 6.28318 | 15.39442 | 0.000207 |
| 0.9 | 0.0001 | 0.81 | 0.1 | 0.01 | 0.01 | 0.82 | 0.000122 | 26.10143 | 6.28318 | 19.84347 | 0.00016 |



Total saving $=4,324$

## APPENDIX C

Simulation Results of $\mathrm{C}_{\text {eff }}$ against $\boldsymbol{\lambda}$












## APPENDIX D

Change in Power Factor as a Function of R/L



Fig. Capacitor versus $R / X L$ when $R$ is changing

## APPENDIX E

Total Harmonic Distortion as a Function of $\boldsymbol{\lambda}$

|  |  | Iambda | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 | 1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|  |  | 0.1 | 0.094827 | 0.091032 | 0.187452 | 0.106163 | 0.114774 | 0.131916 | 0.122603 | 0.117884 | 0.13423 | 0.138658 |  |
|  |  | 0.2 | 0.097177 | 0.132743 | 0.107476 | 0.119816 | 0.118709 | 0.125639 | 0.148662 | 0.148825 | 0.131119 | 0.145387 |  |
|  |  | 0.3 | 0.130206 | 0.119532 | 0.167351 | 0.205153 | 0.126676 | 0.180144 | 0.14923 | 0.233769 | 0.197272 | 0.148297 |  |
|  |  | 0.4 | 0.259577 | 0.094813 | 0.098827 | 0.101752 | 0.127146 | 0.136686 | 0.145147 | 0.15145 | 0.150526 | 0.146633 |  |
|  |  | 0.5 | 0.274235 | 0.088298 | 0.242874 | 0.133777 | 0.196533 | 0.124641 | 0.173801 | 0.04469 | 0.159424 | 0.157562 |  |
|  |  | 0.6 | 0.176774 | 0.053266 | 0.271484 | 0.206111 | 0.136268 | 0.120853 | 0.133861 | 0.089181 | 0.141774 | 0.138993 |  |
|  |  | 0.7 | 0.282321 | 0.15173 | 0.234094 | 0.176049 | 0.171422 | 0.180611 | 0.113399 | 0.145792 | 0.134198 | 0.146212 |  |
|  |  | 0.8 | 0.239855 | 0.115626 | 0.055189 | 0.136818 | 0.171522 | 0.114194 | 0.274674 | 0.132995 | 0.160537 | 0.132177 |  |
|  |  | 0.9 | 0.10443 | 0.117333 | 0.079758 | 0.164094 | 0.125742 | 0.111138 | 0.122245 | 0.14282 | 0.146447 | 0.137374 |  |
|  |  | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|  |  | Max: | 0.282321 | 0.15173 | 0.271484 | 0.206111 | 0.196533 | 0.180611 | 0.274674 | 0.233769 | 0.197272 | 0.157562 |  |
| Max THD | 0.282321 |  |  |  |  |  |  |  |  |  |  |  |  |
| Min THD | 0.15173 |  |  |  |  |  |  |  |  |  |  |  |  |
| AVG THD | 0.119732 |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## APPENDIX F

## Practical Results of The Compensated Reactive Currents and the Equivalent Switching Patterns















Tek

## 0.6


0.7

0.8




$\lambda$

$$
\operatorname{Gama}(\gamma=(C 1 / C 2)(0.5)
$$


0.1

0.2



## 0.3


0.4
Tek
$\operatorname{Gama}(\gamma=0.6$




Tek MPos: 0.000s

## 0.6




## 0.7



0.8

Tek ${ }_{c}^{\text {M M Pos: } 0.000 \mathrm{~s}}$ Stop


0.9

Tek











Tek

## 0.2


0.3
Tek
0.4


0.5

0.6









