

1 **Effects of Si solution in θ -Al₁₃Fe₄ on phase transformation** 2 **between Fe-containing intermetallic compounds in Al** 3 **alloys**

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10

11 **Abstract**

12 θ -Al₁₃Fe₄ is one of the common Fe-containing intermetallic compounds (FIMCs) that forms
13 during solidification in Al- alloys. Silicon (Si) as impurity or solute in Al alloys is easily doped
14 into θ -Al₁₃Fe₄, which not only causes compositional variations but also modifies the lattice
15 parameters, and in some circumstances, modifies or changes the crystal structure of θ -Al₁₃Fe₄.
16 In this study, multiple Al-Fe and Al-Fe-Si alloys which solidified θ -Al₁₃Fe₄ as equilibrium or
17 non-equilibrium phase in primary or eutectic structures were designed and investigated.
18 Different types of phase transformation among θ -Al₁₃Fe₄ and the other FIMCs such as α' -
19 Al₈Fe₂Si, α -Al₁₅(Fe,Mn)₃Si₂ and β -Al₅FeSi were investigated with scanning electron
20 microscopy (SEM), transmission electron microscopy (TEM) and single crystal X-ray analysis.
21 The composition and lattice parameters of FIMCs observed in this study were measured by
22 TEM and X-ray analysis. The orientation relationships between θ -Al₁₃Fe₄ and the other types
23 of FIMCs (α' -Al₈Fe₂Si, α -Al₁₅(Fe,Mn)₃Si₂ and β -Al₅FeSi) were determined with TEM
24 analysis. The phase selection and solidification sequence were investigated by comparing the
25 phase diagram calculation and the casting experiments. The configuration entropy of FIMCs
26 was calculated to build up structural models. Finally, the influence of incorporation of Si into
27 θ -Al₁₃Fe₄ on the phase transformation between θ -Al₁₃Fe₄ and the other types of FIMCs were
28 discussed from crystallographic and thermal stability perspectives.

29 **Key words:** θ -Al₁₃Fe₄, silicon substitution, phase transformation, orientation relationship, Al
30 alloys

31

32 **1. Introduction**

33 Iron (Fe) is inevitably picked up during the fabrication of primary Al, and it cannot be removed
34 completely during recycling [1-2]. Due to the low solid solubility in aluminum especially at
35 the low temperature, the Fe usually forms intermetallic phases in Al alloys, such as θ -Al₁₃Fe₄,
36 α -Al₁₅(Fe, Mn)₃Si₂, and β -Al₅FeSi, etc. [4-7]. These Fe-containing intermetallic compounds
37 (FIMCs) usually form as large particles with different morphologies, such as plate-like, needle-
38 like, Chinese script [7-11]. They deteriorate the mechanical properties dramatically, especially
39 the ductility. In the last decades, much effort has been made to reduce the detrimental effect on
40 the mechanical properties, such as removal of Fe, modification of FIMCs morphology, and
41 refinement of FIMCs, etc. However, it is reported that [12] the removal Fe is very limited when
42 Fe is lower than 0.7wt.%, which is still undesirable for the mechanical properties. The
43 techniques or theories on direct removal of iron from aluminum has so far made no satisfactory
44 progress. Some transition metal elements such as Mn, Co, and Cr were used to modify the
45 morphology of FIMCs [13-17]. However, these elements will increase the total amount of
46 FIMCs, which is also harmful to the mechanical properties of Al alloys. In recent years,
47 research has focused to some extent on the development of grain refinement techniques for
48 these FIMCs by applying the heterogeneous nucleation theory [10,18-20]. The bottlenecks in
49 technology development are due to the lack of the fundamental understanding on the formation
50 mechanism of FIMCs and the relationship between different types of FIMCs. In recent years,
51 our group has worked on the understanding on the heterogeneous nucleation of FIMCs and
52 phase relationship between different types of FIMCs by investigating different types of phase
53 transformation among these FIMCs experimentally and using crystallographic methods [21-
54 24].

55 Many different types of FIMCs were reported in various Al-alloys. In Al-Fe-Si casting alloys,
56 the most commonly observed FIMCs are θ -Al₁₃M₄ (M= Fe, Ni, Cr, Cu, etc.) (monoclinic), β -
57 Al₅FeSi (monoclinic), α -Al₁₅(Fe, Mn)₃Si₂ (complex body-centered cubic (BCC)) and α' -
58 Al₈Fe₂Si (complex hexagonal) [3-6, 25]. The formation of these FIMCs is very sensitive to the
59 alloy composition. The composition and lattice parameters of these FIMCs change with the
60 alloy composition and formation conditions. These FIMCs have a range of compositions and
61 lattice parameters, and they act like the “solid solution compounds”. For example, atomic
62 positions of Al in θ -Al₁₃Fe₄, α -Al₁₅(Fe, Mn)₃Si₂ can be replaced with Si, and the atomic
63 positions of Fe are substituted by other transition elements such as Mn or Cr. This also the case
64 for the other FIMCs such as β -Al₅FeSi and α' -Al₈Fe₂Si. The alloying elements incorporated
65 into the parent FIMCs not only causes change in crystal structure but also induce phase
66 transition, e.g., Mn doping in β -Al₅FeSi (monoclinic) cause transformation into α -Al₁₅(Fe,
67 Mn)₃Si₂ (BCC). The modification achieves more desirable types of FIMCs in terms of retaining
68 mechanical properties especially the ductility by modifying the morphology of the FIMCs.
69 However, the modification result in complicated heterogeneous nucleation and phase
70 transformation process among different types of FIMCs, which makes the microstructure
71 control even more difficult.

72 θ -Al₁₃Fe₄ as one of the most common FIMCs in as-cast Al alloys is reported a monoclinic
73 crystal structure with lattice parameters: $a = 15.447 \text{ \AA}$, $b = 8.057 \text{ \AA}$, $c = 12.429 \text{ \AA}$ and $\beta =$
74 107.80° [6]. It has a monoclinic lattice with space group C2/m (nr. 12) [13]. There are 20
75 crystallographically different atomic sites (5 Fe and 15 Al) and 102 atoms in total in a unit cell.
76 The Al atoms have 10 to 12 neighbours including 2 to 4 Fe, except the Al₂ atoms at the
77 Wyckoff 4i sites which have only 6 neighbours including two Fe with Fe-Al bond-lengths
78 below 3.0 \AA ($1 \text{ \AA} = 0.1 \text{ nm} = 10^{-10} \text{ m}$). θ -Al₁₃Fe₄ is an extremely impurity tolerant intermetallic
79 compound as both Al and Fe may be substituted with other elements, such as Si, Cr, Ni, Mn,
80 etc. [26-31]. Experiments show that Si can easily incorporate into the θ -Al₁₃Fe₄ at impurity or
81 solute concentration levels in Al alloys. The elemental solution and the composition changes
82 in FIMCs not only can cause the lattice parameters variation, but also can lead to phase
83 transformations [21-22, 32-34]. Research published recently [21] reported the multi-step phase
84 transformation from θ -Al₁₃Fe₄ to the other types of FIMCs α' -Al₈Fe₂Si, β -Al₅FeSi and δ -
85 Al₄FeSi₂. The variation on the phase transformation among the FIMCs have been reported in
86 literature to be dependent on the composition and cooling conditions. The experimental
87 evidence shows that the multi-step phase transformation from θ -Al₁₃Fe₄ to the other types of
88 FIMCs is a diffusion-controlled phase transformation which is mainly affected by the Si
89 diffusion.

90 However, the understanding of the reasons behind the variable phase transformation among the
91 FIMCs is very limited due to the lack of the fundamental research on the mechanisms of phase
92 transformation, the phase relationships, and the changes in crystal structure during the
93 experiment. Our research group focus on the fundamental research on formation and grain
94 refinement of FIMCs in Al alloys recent years. In this paper, we summarized the findings on
95 the phase transformation between θ -Al₁₃Fe₄ and the other types of FIMCs in a number of Al
96 alloys with different Si, Fe ratios. The effect of Si dissolution on the crystallography and the
97 internal defects of the θ -Al₁₃Fe₄ crystals in different Al alloys were investigated. The phase
98 relationship between θ -Al₁₃Fe₄ and the other FIMCs were investigated using TEM and single
99 crystal X-ray analysis. The Si solubility in multiple types of FIMCs were investigated through
100 the development of the structural models of different types of FIMCs. Finally, a mechanism of
101 phase transformation between θ -Al₁₃Fe₄ and the other FIMCs is proposed.

102

103 2. Experimental

104 In this study, numbers of Al casting alloys containing θ -Al₁₃Fe₄ which phase transformed into
105 other types of FIMCs were investigated. The phase diagrams of these Al alloys were calculated
106 using Pandat software using PanAluminum 2020 database [48]. The alloy compositions of
107 these Al alloys were listed in Table 1. The starting materials (in wt.%) used in this work were
108 high purity (HP) Al (99.99%), commercial purity (CP) Al (>99.86%), Al-45Fe, Al-20Mn, Al-
109 50Si and CP Mg (>99.8%) master alloys. The melting temperatures of these alloys were
110 calculated with the Pandat software using Scheil solidification model, as shown in Table 1. The
111 casting temperatures are about 50°C above the melting temperatures of these alloys. The alloys

112 were produced by melting HP Al or CP Al and the master alloys in an electric resistance
113 furnace. The master alloys were added to the molten HP Al or CP Al melts in the sequence of
114 Al-Fe, Al-Mn, Al-Si (as required for the alloy), following by a completely mixing and
115 sufficiently long holding time to ensure chemical homogeneity of the melt. The preheated CP
116 Mg (200°C) covered with Al foil (as required by some alloys) was inserted into the melt as the
117 last addition. After sufficiently mixing and holding isothermally for 20 minutes, the slag in
118 these Al alloys was removed and cast into TP-1 moulds preheated to 380 °C [35]. To achieve
119 the samples with bigger particles for single crystal X-ray tests, the remainder of melt in the
120 crucibles was cooled to 200°C in the furnace, with an average cooling rate of 0.01K/s.

121 In addition to experimental alloys, an Al-3.7Ti-1B master alloy which contains 1wt.% Si and
122 1.5wt.% Fe was also investigated. This alloy was produced by adding Al-Fe and Al-Si master
123 alloys into the Al-3.7Ti-1.5B master alloy melt, and casted at 1K/s in a steel mold into a flat
124 sample with thickness of 1-5mm was achieved. The casting procedure in details will be
125 reported in our other contributions [36]. In this alloy, TiB₂ particles formed in Al-Fe-Si alloy
126 with 0.4wt.% free Ti. Therefore, to simplify, we refer this alloy containing Al-1.5Fe-1Si-3.7Ti-
127 1B as Al-1Si-1Fe alloy. In this study, the focus is on the phase transformation between FIMCs.
128 An AlFe intermetallic compound with B2-type (CsCl) was observed. The phase transformation
129 between AlFe and θ -Al₁₃Fe₄ was examined with the aid of this alloy. A square sample was
130 sectioned from the flat sample of Al-1Si-1Fe alloy. The microstructural characterization was
131 carried out on the middle of the thickness by grinding and polishing both surface of the flat
132 sample. Samples for microstructural characterisation were prepared from the cross section of
133 TP1 samples at the 38mm height from the bottom which solidifies at 3.5K/s [35], with the
134 exception of Al-1Si-1Fe alloy. Metallographic specimens were prepared using the standard
135 procedures. To observe the 3-dimensional morphology of the structure, the samples were
136 gently etched in 10vol.% HCl+H₂O solution for a few minutes followed by cleaning in ethanol.
137 The as-solidified microstructure characteristics of the samples were examined using a Zeiss
138 optical microscope fitted with the Axio Vision 4.3 image analysis system and a Zeiss Supra 35,
139 field emission gun scanning electron microscope (FEG-SEM), operated at an accelerating
140 voltage between 5-20kV. Thin foils for high resolution transmission electron microscopy
141 (TEM) examinations were prepared from samples which were mechanically ground and cut
142 into 3mm diameter discs. The discs were then manually ground to a thickness of less than 50
143 μ m, followed by ion-beam-thinning using a Gatan precision ion polishing system (PIPS) at an
144 energy of 2.0-5.0kV and an incident angle of 3-5°. TEM examination was performed on a JEOL
145 2100F transmission electron microscope equipped with EDX spectrometer operated at an
146 accelerating voltage of 200kV. The 3-dimensional morphology of the FIMCs was examined
147 on Zeiss X radial 410 Versa X-ray –microscope operating at 80kV with power set to 10W to
148 achieve the clearest image of intermetallic particles.

149 To investigate the crystal structure variation of FIMCs, the FIMCs crystal from different
150 samples were examined with a single crystal X-ray diffraction. The lattice parameters from the

151 literature and the casting conditions of samples examined are shown in Table 3. The slowly
152 cooled samples were deep etched in 5-10% HCl+H₂O solution for a few minutes followed by
153 ultrasonic cleaning in ethanol. After deep cleaning and drying, the large crystals of intermetallic
154 particles from desired microstructure was cut under optical microscope and transferred to a
155 clean glass slide. The crystal samples were further cut into the desired size (<100 μm) for the
156 single crystal analysis. Single crystal data were collected at 100K using a Rigaku SuperNova,
157 Dualflex, AtlasS2 diffractometer with Cu-Kα radiation (λ=1.54184 Å). CrysAlis Pro software
158 was used for data collection, absorption correction and data reduction.

159 In order to get reliable information about the effects of Si solution on the stability and structural
160 information about the related FIMCs, we performed first-principles study on these compounds
161 [24, 41]. We utilized a plane-wave approach which is implanted into the first-principles code
162 VASP (Vienna Ab initio Simulation Package) [46]. The Generalized Gradient Approximation
163 (GGA-PBE) [47] was used for the exchange and correlation energy terms. We used a cut-off
164 energy of 550 eV for the wave functions and the cut-off energy of 700 eV for the augmentation
165 functions. More details are included in [24, 41].

166

167 3. Results

168 3.1 θ-Al₁₃Fe₄ in Al-Fe alloys

169 Si as one of the major impurities in Al alloys is easily picked up during casting or from the
170 master alloys. It is reported that Si can dope in θ-Al₁₃Fe₄ by replacing the Al atoms. The effects
171 of the Si on the crystal structure and the consequently phase transformation of θ-Al₁₃Fe₄ will
172 be investigated in this study. Firstly, the initial structure of the θ-Al₁₃Fe₄ free of Si was
173 investigated as the reference. To produce such high pure θ-Al₁₃Fe₄ particles, the high pure Al
174 and the Al-45Fe master alloy were used to minimize the effect of Si impurity. The high pure
175 Al was previously melted at 900 °C, and then the Al-45Fe master alloy was added into the Al
176 melt with completely stirring until fully molten. An Al-3Fe alloy actually containing 3.25±0.5
177 wt.% Fe was produced.

178 To compare the effect of Si as impurity on the θ-Al₁₃Fe₄ phase, the other Al-1Fe alloy was
179 produced with commercial pure Al and same Al-45Fe master alloy. The commercial pure Al
180 was previously melted at 750 °C, and then the Al-45Fe was added into the Al melt and stirred
181 until fully molten. The final composition of these two alloys were list in Table 1. It shows that
182 the Si content in Al-3Fe is negligible when HP Al was used. The measured EDX composition
183 of θ-Al₁₃Fe₄ phase (Table 2) show that the Si concentration in (HP) Al-3Fe is negligible, but
184 0.3at. % Si can be detected in the (CP) Al-1Fe. The single crystal X-ray results are shown in
185 Table 3. The lattice parameters *a*, *b*, and *c* in θ-Al₁₃Fe₄ in (HP) Al-3Fe are larger than that of
186 θ-Al₁₃Fe₄ in (CP) Al-1Fe. Table 3 also indicates that the lattice parameters *a*, *b*, and *c* of θ-
187 Al₁₃Fe₄ decreased with the increase in Si concentration.

188 The as-cast microstructure of the (HP)Al-3Fe, Fig.1, shows the typical star-like primary θ -
189 $\text{Al}_{13}\text{Fe}_4$ phase and the needle-like $\theta\text{-Al}_{13}\text{Fe}_4 + \alpha\text{-Al}$ eutectic structure (Fig 1a). The 3D
190 morphology of these two structures were shown in Figs.1b-c, respectively. Fig.1b shows that
191 the primary $\theta\text{-Al}_{13}\text{Fe}_4$ phase has the multi-faceted star-like morphology in cross section. The
192 eutectic $\theta\text{-Al}_{13}\text{Fe}_4$ phase associated with the primary θ has plate-like morphology, as shown in
193 Fig.1b. Some eutectic $\theta\text{-Al}_{13}\text{Fe}_4$ phase was observed as needle-like morphology which is away
194 from primary θ , as illustrated in Fig 1c. There is no appreciable difference in the morphology
195 of $\theta\text{-Al}_{13}\text{Fe}_4$ in HP Al-3Fe and CP Al-3Fe (Fig.1d) except the particle size.

196 Fig.2a shows the bright field TEM image presenting the needle-like morphology of eutectic θ -
197 $\text{Al}_{13}\text{Fe}_4$ phase in (CP)Al-1Fe alloy solidified from 720 °C at a cooling rate of 3.5 K/s. Two
198 different types of faceted planes were observed on $\theta\text{-Al}_{13}\text{Fe}_4$ phase, Figs.2b-c. The high
199 resolution TEM (HRTEM) images show the faceted (010) planes and (102) planes of $\theta\text{-Al}_{13}\text{Fe}_4$
200 phase when viewed along the $[\bar{2}01]$ zone direction.

201 As reported [37], $\theta\text{-Al}_{13}\text{Fe}_4$ can be twinned easily. In as-cast Al-1Fe (CP Al) alloy, the twinning
202 structure of $\theta\text{-Al}_{13}\text{Fe}_4$ is readily observed. One example is shown in Fig.3. The HRTEM image
203 (Fig.3a) and the corresponding selected area diffraction (SAED) patterns (Figs.3b-c) show that
204 the $\theta\text{-Al}_{13}\text{Fe}_4$ crystal has leaf-like symmetrical twinning. The SAED pattern, Fig.3d, contains
205 two overlapping patterns with a $36\pm 0.5^\circ$ rotation angle between the two sets of the SAED
206 patterns. This provides for tenfold twins, as the orientation difference between neighbouring
207 twins are very close to 36° . The higher magnification HRTEM image, Fig.3e, shows that in the
208 very localised areas, there are multi-step twinning and some disordered regions.

209

210 3.2 $\theta\text{-Al}_{13}\text{Fe}_4$ in Al-4Fe-4Si alloy

211 Section 3.1 reported the result that Si can incorporate in $\theta\text{-Al}_{13}\text{Fe}_4$ at impurity concentration
212 level in Al alloys. Here, the effect of Si on the crystal structure of $\theta\text{-Al}_{13}\text{Fe}_4$ in Al-Si-Fe alloys
213 will be investigated. An Al-4Si-4Fe alloy with approximately equal concentration of Si and Fe
214 (wt.%) was designed and cast. The Al alloy in this work had a composition of 4.21 ± 0.5 Si, and
215 4.10 ± 0.6 Fe (in wt%) with Al balance. The phase diagram of the Al-4Fe-xSi system was
216 calculated with the Pandat software and its associated Al-database as shown in Fig.12b. It
217 shows that the $\theta\text{-Al}_{13}\text{Fe}_4$ is calculated as the primary equilibrium phase. The melting
218 temperature of Al-4Fe-4Si is calculated as 715°C with the Scheil solidification model. The
219 microstructure of Al-4Si-4Fe alloy cast from 770°C at a cooling rate of 3.5K/s is shown in
220 Fig.4. The microstructure consisted of multiple types of FIMCs which have star-like (θ -
221 $\text{Al}_{13}\text{Fe}_4$) and compacted morphology ($\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$), and multiple FIMCs in eutectic structures
222 which have Chinese script morphology ($\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$) and needle-like morphology ($\theta\text{-Al}_{13}\text{Fe}_4$).
223 All the phases in this study were identified with SEM-EDX and subsequent TEM analysis. The
224 details of primary star-like $\theta\text{-Al}_{13}\text{Fe}_4$ was examined carefully with SEM, and the results are

225 shown in Figs.4b-c. Fig.4b shows the high magnification SEM-BSE (backscattered electron)
226 image of a primary $\text{Al}_{13}\text{Fe}_4$ particle with a brighter central phase ($\theta\text{-Al}_{13}\text{Fe}_4$) and grey surface
227 phase ($\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$). The interface between $\theta\text{-Al}_{13}\text{Fe}_4$ and $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ presents irregular under
228 SEM-BSE observation. The morphology in Fig.4b indicates a reaction typical of a
229 transformation: $\text{L} + \theta\text{-Al}_{13}\text{Fe}_4 \rightarrow \alpha'\text{-Al}_8\text{Fe}_2\text{Si} + \alpha\text{-Al}$.

230 It is noted that more than one type of phase transformation was observed on the surface of
231 primary $\theta\text{-Al}_{13}\text{Fe}_4$. Fig.4c shows the primary $\theta\text{-Al}_{13}\text{Fe}_4$ particle with bright white central region
232 ($\theta\text{-Al}_{13}\text{Fe}_4$) and sharp needle-like grey surface phase ($\beta\text{-Al}_5\text{FeSi}$). The interface is irregular
233 based on SEM observations. The morphology in Fig.4c also indicates a reaction: $\text{L} + \theta\text{-Al}_{13}\text{Fe}_4$
234 $\rightarrow \beta\text{-Al}_5\text{FeSi} + \alpha\text{-Al}$.

235 The TEM-EDX compositions of $\theta\text{-Al}_{13}\text{Fe}_4$, $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ and $\beta\text{-Al}_5\text{FeSi}$ observed in this alloy
236 are listed in Table 2. The $\theta\text{-Al}_{13}\text{Fe}_4$ phase contains 2.7 ± 0.2 at. %Si. However, the transformed
237 $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ and $\beta\text{-Al}_5\text{FeSi}$ have much higher Si concentration at 10.4 ± 0.1 at. % and 16.9 ± 0.1 at.
238 %, respectively.

239 To investigate the phase transformation mechanisms between $\theta\text{-Al}_{13}\text{Fe}_4$ and the other FIMCs,
240 the interface between $\theta\text{-Al}_{13}\text{Fe}_4$ /FIMCs were observed under TEM. The orientation
241 relationships between the parent θ phase and the transformed FIMCs are examined from several
242 different pairs of zone directions during the TEM analysis. Some examples with lower indexed
243 zone directions will be presented here.

244 The HRTEM image, Fig.5a, shows the interface between $\theta\text{-Al}_{13}\text{Fe}_4$ and $\text{Al}_8\text{Fe}_2\text{Si}$ when viewed
245 along the zone direction of $[\bar{1}\bar{3}\bar{4}]$ of $\theta\text{-Al}_{13}\text{Fe}_4$ and $[\bar{3}2\bar{1}]$ of $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$. The interface is not
246 sharp, and some transition area can be observed at the interface. The fast Fourier transformation
247 (FFT) patterns of $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ phase and $\theta\text{-Al}_{13}\text{Fe}_4$ phase are shown in Fig.5b-c. The FFT
248 pattern (Fig.5d) containing both phases and its indexed pattern (Fig.5e) reveal an orientation
249 relationship (OR) between $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ and $\theta\text{-Al}_{13}\text{Fe}_4$: $(10\bar{3}) [\bar{3}2\bar{1}] \alpha'\text{-Al}_8\text{Fe}_2\text{Si} // (11\bar{1}) [\bar{1}\bar{3}\bar{4}]$
250 $\theta\text{-Al}_{13}\text{Fe}_4$.

251 The TEM-EDX composition of $\theta\text{-Al}_{13}\text{Fe}_4$ in Al-4Fe-4Si contains 2.7 ± 0.2 at.% Si, and 20.6 ± 0.5
252 at.% Fe, and the composition of $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ is 10.4 ± 0.1 at.% Si, and 15.3 ± 0.1 at.% Fe. The
253 lattice parameters of $\theta\text{-Al}_{13}\text{Fe}_4$ measured with single crystal X-ray was 15.424 \AA (a), 8.052 \AA
254 (b), 12.404 \AA (c), with 107.7° (β). The lattice parameters of $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ measured with TEM
255 was 12.13 \AA (a), 12.13 \AA (b), 26.68 \AA (c).

256 The HRTEM image, Fig.6a, shows the interface between $\theta\text{-Al}_{13}\text{Fe}_4$ and $\beta\text{-Al}_5\text{FeSi}$ when
257 viewed along the zone direction of $[001]$ of $\theta\text{-Al}_{13}\text{Fe}_4$ and $[100]$ of $\beta\text{-Al}_5\text{FeSi}$. The interface is
258 again a diffuse interface, and a transition area can be observed at the interface, suggesting
259 continuous incorporation of Si into the structure. The fast Fourier transformation (FFT) patterns
260 of $\beta\text{-Al}_5\text{FeSi}$ phase and $\theta\text{-Al}_{13}\text{Fe}_4$ phase are shown in Figs.6b-c. The FFT patterns containing

261 both phases are shown in Fig.6d. The schematic diagram showing the indexed FFT of Fig.6d
262 is in Fig.6e. These results indicate an OR between θ -Al₁₃Fe₄ and β -Al₅FeSi to be: (020) [100]
263 β -Al₅FeSi // (010) [001] θ -Al₁₃Fe₄. The TEM-EDX result, Table 2, shows that the β -Al₅FeSi
264 contains 16.9±0.1 at. % Si, which is higher than that of θ -Al₁₃Fe₄ (2.7±0.2 at. % Si) and α' -
265 Al₈Fe₂Si (10.4±0.1 at. % Si).

266

267 3.3 θ -Al₁₃Fe₄ in Al-1Fe-1Si (-3.7Ti-1.5B) alloy

268 The phase transformation between θ -Al₁₃Fe₄ and AlFe in Al-1Fe-1Si alloy containing TiB₂
269 particles was investigated to understand the effect of heterogeneous sites for nucleation on the
270 choice of FIMC. The SEM-SE (secondary electron) image, Fig.7, shows the microstructure of
271 Al-1Si-1Fe(-3.7Ti-1.5B) alloy with 0.4wt.% free Ti solidified at 1K/s, indicating a
272 microstructure with a mixture of FIMCs. The TiB₂ particles agglomerations distribute
273 randomly in the Al grains or at the grain boundary. Some larger FIMC particles with long plate-
274 like or needle-like morphology distribute in the Al grains, which can be considered as primary
275 FIMCs. This FIMC was identified as AlFe which has B2-CsCl structure via TEM analysis. The
276 AlFe phase observed here is not expected according to the Al-Fe phase diagram calculations.
277 We expect localised inhomogeneities in the liquid composition and the presence of TiB₂
278 particles may promote this phase. The phase transformation from AlFe to θ -Al₁₃Fe₄ observed
279 in this alloy illustrates the instability of this phase. Some smaller plate or needle-like FIMCs
280 distribute at the grain boundaries, which are likely to be FIMCs in the eutectic structures. These
281 FIMC in the eutectic structure was identified as θ -Al₁₃Fe₄ phase with TEM analysis. AlFe
282 phase is rarely reported in cast Al alloys. In addition, a phase transformation was observed at
283 the surface of AlFe with TEM, and a well-defined OR was identified and shown in Fig.8.

284 The bright field TEM image, Fig.8a, shows the needle-like central AlFe phase with the θ -
285 Al₁₃Fe₄ phase at the surface. The TEM-EDX results, Table 2, show that the AlFe contains
286 1.5±0.1 at. % Si, and the θ -Al₁₃Fe₄ contains 2.4±0.1 at. % Si. The Si is likely to be continuously
287 incorporated into AlFe phase during the solidification progresses, and the phase transformation
288 occurs from AlFe to θ -Al₁₃Fe₄ through a reaction: L + AlFe → θ -Al₁₃Fe₄ + α -Al.

289 The SAED patterns from AlFe, θ -Al₁₃Fe₄ and from a region containing both phases are shown
290 in Figs.8b-d, when viewed along the [112] zone direction of AlFe and [100] θ -Al₁₃Fe₄,
291 respectively. Fig.8e shows the schematic illustration of the SAED in Fig.8d. The HRTEM
292 image, Fig.8f, shows the interface between AlFe and θ -Al₁₃Fe₄. Many planar defects can be
293 observed on the θ -Al₁₃Fe₄ phase. The interface between the two phases reveals an orientation
294 relationship of (1 $\bar{1}\bar{1}$)AlFe// (001) θ -Al₁₃Fe₄, and [112] AlFe// [100] θ -Al₁₃Fe₄.

295

296 3.4 θ -Al₁₃Fe₄ in Al-Fe-Mn-Si-Mg alloys

297 The phase transformation between θ -Al₁₃Fe₄ and the α -Al₁₅(Fe,Mn)₃Si₂ was observed in Al-
298 5Mg-2Si-0.7Mn-1.2Fe alloy. The Al alloy in this work had a composition of 5.1±0.5Mg,
299 2.0±0.3 Si, 0.6±0.1 Mn and 1.3±0.05 Fe (in wt%) with Al balance. The phase diagram of the
300 Al-5Mg-2Si-0.6Mn-xFe system was calculated with the Pandat software and its associated Al-
301 database as shown in Fig.12c. It shows that the α -Al₁₅(Fe,Mn)₃Si₂ is calculated as primary
302 equilibrium phase. The as-cast microstructure of this alloy solidified at 3.5K/s is shown in
303 Fig.9. The formation of FIMCs in this alloy is complicated and the details has been reported in
304 pervious contribution [22]. The SEM-BSE image, Fig.9a, shows that in this sample, the FIMCs
305 are mainly in plate-like and Chinese script morphologies. The high magnification SEM
306 observation on the local area marked in Fig.9a is shown in Fig.9b. The compacted grey particles
307 (α -Al₁₅(Fe,Mn)₃Si₂) which leading a Chinese script morphology FIMC connects and grows
308 from the plate-like FIMC (θ -Al₁₃Fe₄). The calculated phase diagram, Fig.12c, shows that the
309 equilibrium primary phase of Al-5Mg-2Si-0.7Mn-1.2Fe alloy supposed to be α -
310 Al₁₅(Fe,Mn)₃Si₂, but not θ -Al₁₃Fe₄. However, due to the smaller nucleation undercooling [20],
311 the θ -Al₁₃Fe₄ nucleated firstly on the native MgAl₂O₄ particles [22], and transformed into α -
312 Al₁₅(Fe,Mn)₃Si₂ via a reaction: $L + \theta\text{-Al}_{13}\text{Fe}_4 \rightarrow \alpha\text{-Al}_{15}(\text{Fe,Mn})_3\text{Si}_2 + \alpha\text{-Al}$.

313 The interface between θ -Al₁₃Fe₄ and α -Al₁₅(Fe,Mn)₃Si₂ was investigated with TEM, Fig.10. A
314 well-defined OR between these two phases was identified. The dark field TEM image, Fig.10a,
315 shows the interface between θ -Al₁₃Fe₄ and α -Al₁₅(Fe,Mn)₃Si₂ when viewed along the [010]
316 zone direction of θ -Al₁₃Fe₄. Some nano-scaled size α -Al can be seen from the α -
317 Al₁₅(Fe,Mn)₃Si₂, which indicates the alloy elements diffusion during the phase transformation.
318 The HRTEM image containing both θ -Al₁₃Fe₄ and α -Al₁₅(Fe,Mn)₃Si₂ are shown in Fig.10b
319 [22]. The corresponding schematic indexed FFT patterns is shown in Fig.10c [22]. The results
320 reveal an orientation relationship between θ -Al₁₃Fe₄ and α -Al₁₅(Fe, Mn)₃Si₂: $(\bar{2}01) \theta\text{-Al}_{13}\text{Fe}_4$
321 $// 2.3^\circ (0\bar{1}1)\alpha\text{-Al}_{15}(\text{Fe, Mn})_3\text{Si}_2$, and $[010] \theta\text{-Al}_{13}\text{Fe}_4 // [100] \alpha\text{-Al}_{15}(\text{Fe, Mn})_3\text{Si}_2$. In addition,
322 the TEM-EDX result, Table 2, shows that in this alloy, not only Si (1.8±0.1 at.%), but also Mn
323 (6.4±0.1at.%) can incorporate into θ -Al₁₃Fe₄ phase in Al-5Mg-2Si-0.7Mn-1.2Fe alloy, which
324 requires further investigation.

325

326 3.5 First principles calculation and related thermodynamics for the FIMCs

327 The experimental results revealed that the phase transformation between different types of
328 FIMCs is a diffusion-controlled process. During the phase transformation, the vital element
329 which determinate different phase transformation reactions is Si. Each FIMC has significant
330 difference in Si concentration, Table 2. Therefore, the difference in crystal structure and the
331 atomic sites of these FIMCs were investigated based on the reported structural models [3, 24-
332 25, 38]. The solubility of Si in and phase stability of different FIMCs are compared based on
333 the structural models in the literature, Table 4. Further to that, the solubility of Si using different

334 structural models were calculated and compared to the experimentally measured Si
335 concentration.

336 The solubility of Si in different FIMCs based on the above crystal structural models were
337 calculated and shown in Table 4. It shows that the Si solubility in FIMCs has a sequence as: β -
338 Al_5FeSi (15.38%) > α' - $\text{Al}_8\text{Fe}_2\text{Si}$ (9.80%) > α - $\text{Al}_{15}(\text{Fe}, \text{Mn})_3\text{Si}_2$ (7.68%) > θ - $\text{Al}_{13}\text{Fe}_4$ (4.9%). The
339 Si concentration in θ - $\text{Al}_{13}\text{Fe}_4$ (4.9%) compound is based on the compound model calculated
340 with DFT. As shown in Table 4, the Si concentrations in compounds α' - $\text{Al}_8\text{Fe}_2\text{Si}$, β - $\text{Al}_{4.5}\text{FeSi_I}$
341 and α - $\text{Al}_{15}(\text{Fe}, \text{Mn})_3\text{Si}_2$ are based on the compound models calculated from the literatures [25,
342 38, 3] which based on the experimental compound compositions. The Si concentrations in
343 compound β - $\text{Al}_{4.5}\text{FeSi_II}$ and β - $\text{Al}_{4.375}\text{FeSi}_{1.125_III}$ is based on the First-principles calculation
344 done in this work. Our measured experimental Si concentrations in different types of FIMCs
345 using TEM-EDX shows the same trend in the amount of Si incorporated into the structures as
346 those of the calculated Si concentrations sequence. There is a significantly large gap between
347 the maximum Si concentrations determined purely on DFT calculations and the experimentally
348 measured Si solubility in FIMCs. Our experimental result shows that a 2.7 at.% Si is
349 incorporated into θ - $\text{Al}_{13}\text{Fe}_4$, but the result from crystal structural model calculated with DFT is
350 up to 4.9 at.% [24]. The DFT calculation reveals a theoretical possibility of Si concentration in
351 compounds regardless of phase stability, which can provide some valuable information for the
352 further investigation. Further studies are going to continue to build new crystal structural
353 models for the other FIMCs using DFT calculations.

354 Both experimental and theoretical efforts have been made to obtain structural models for the
355 FIMCs investigated. Experimental evidence revealed the complexity of crystal structures with
356 partial occupation and/or multiple atomic species occupations at the Wyckoff sites in these
357 FIMCs. This provides extra freedom for the crystals, Table 4. The primary FIMCs form at
358 elevated temperatures during casting. At high temperature, the extra freedom at the atomic sites
359 becomes an important factor in determining the relative stability of the FIMCs. To obtain a
360 further insight into the crystal chemistry of the Fe-IMCs, parameters-free first-principles
361 methods have been used [24, 39-41]. The first-principles calculations have been conducted to
362 investigate the Si solution in FIMCs including θ - $\text{Al}_{13}\text{Fe}_4$ [24] and β - $\text{Al}_{5.5}\text{Fe}$ [41]. The calculated
363 results are summarized in Fig.11. The β - $\text{Al}_{5.5}\text{Fe}$ has higher formation energy compared with θ -
364 $\text{Al}_{13}\text{Fe}_4$, in agreement with the experimental observations that the θ -phase is the stable phase
365 whereas the β -phase is not in the binary Fe-Al phase diagram. At low temperatures, the most
366 stable configuration is θ - $\text{Al}_{5.69}(\text{Si}^{\text{IX}})_{0.31}\text{Fe}_4$ containing 3.92 at. % of Si [24].

367 First-principles calculation, Fig.11b, reveals that a high concentration of Si goes into solution
368 in β -phase and the configuration of the highest stability with respect to the elemental Al, Si and
369 Fe is when Al11 sites (β - $\text{Al}_{4.5}\text{Si}^{\text{I}}\text{Fe}$) or Al6 site (β - $\text{Al}_{4.5}\text{Si}^{\text{VI}}\text{Fe}$) which contains 15.38 at% Si,
370 are fully occupied by Si at the ambient conditions [39]. The first-principles calculations also
371 showed that addition of more Si to the configurations of high stability at ambient condition,

372 e.g. (β -Al_{4.5}Si¹Fe) may increase the formation energy, but it also increases the number of
373 configurations significantly. At 1000K the β -phase has 15.38at% to 21.15at % Si content [39],
374 whereas the Si content in the θ -phase is between 2.94 at% and 4.90at% due to the configuration
375 entropy contributions [24]. This indicates that the Si concentration in the Fe-IMCs depends on
376 the chemical compositions of the alloy and the casting process.

377 4. Discussion

378

379 4.1 Heterogeneous nucleation effects on phase transformation of θ -Al₁₃Fe₄

380 In this study, 5 different Al-Fe alloys were investigated, where θ -Al₁₃Fe₄ phase formed during
381 solidification as a primary intermetallic or as an intermetallic in the eutectic structure. Multiple
382 types of phase transformation were observed in corresponding samples from θ -Al₁₃Fe₄ to the
383 other types of FIMCs. The θ -Al₁₃Fe₄ in Al-1Fe-1Si, Al-4Fe-4Si alloys was calculated as
384 equilibrium phase using Pandat software based on Scheil solidification model to illustrate the
385 2D vertical-sections at given alloy chemistry with varying Si concentrations, Figs.12a-b. The
386 Al₁₃Fe₄ in other alloys such as Al-5Mg-2Si-0.7Mn-1.2Fe alloy was calculated to be a non-
387 equilibrium phase, Fig.12c. However, during the casting process, the phase selection of the
388 FIMCs can be different to that calculated phases due to the non-equilibrium phase selections
389 [11, 21-22]. The changes to phase selection during the solidification process will cause the
390 non-equilibrium phase transformation and solidification sequence. For example, the Al₁₃Fe₄
391 formed in place of the equilibrium α -Al₁₅(Fe, Mn)₃Si₂ phase in Al-5Mg-2Si-0.7Mn-1.2Fe alloy
392 and then transformed into equilibrium α -Al₁₅(Fe, Mn)₃Si₂ during further cooling. The AlFe
393 formed first instead of the equilibrium θ -Al₁₃Fe₄ phase in Al-1Fe-1Si(-3.7Ti-1.5B) alloy and
394 then transformed into the equilibrium θ -Al₁₃Fe₄. The most complicated case is the FIMCs
395 formation in the Al-4Fe-4Si alloy, Fig.12b. Multiple primary FIMCs such as θ -Al₁₃Fe₄ and α' -
396 Al₈Fe₂Si formed (Fig.4a), and multiple types of phase transformation between θ -Al₁₃Fe₄ and
397 the other types of FIMCs such as α' -Al₈Fe₂Si, β -Al₅FeSi were observed. The solidification
398 sequence and the complicated transformation sequence was presented in detail in a separate
399 contribution [45].

400 The previous research [11, 21-22, 32-34] showed that the formation of FIMCs during the
401 solidification is very sensitive to the alloy compositions, solidification conditions etc., which
402 can easily be changed. Many types of phase transformation between different types of FIMCs
403 have been reported in different alloys under different casting conditions. Recent research
404 reported [20, 22] that the variations in phase selection among these FIMCs is due to the
405 difficulties associated with nucleation which required multiple constitutive elements and large
406 undercooling. It also shows that the θ -Al₁₃Fe₄ requires smaller number of elements and smaller
407 nucleation undercooling compared to the other types of common FIMCs in as-cast Al alloys.
408 This is likely why it is easier to form θ -Al₁₃Fe₄ in Al alloys such as Al-5Mg-2Si-0.7Mn-1.2Fe
409 than the calculated equilibrium α -Al₁₅(Fe, Mn)₃Si₂ phase. The other factors such as the TiB₂

410 can also change the phase selection of FIMCs. In this study, the Al-1Fe-1Si alloy containing
411 TiB₂ particles and 0.4% free Ti promoted a metastable AlFe phase formation in place of θ -
412 Al₁₃Fe₄. The non-equilibrium AlFe phase is not stable in the alloy and subsequently
413 transformed into θ -Al₁₃Fe₄. It is reported [20, 42-43] that the additional elements in the Al-Ti-
414 B master alloys can change the interfacial segregation on the TiB₂ interface, which therefore
415 changed the nucleation potency of these TiB₂ particles and promote the formation of one phase
416 over another.

417 4.2 Effects of Si on the crystal structural of θ -Al₁₃Fe₄ and β -phase

418 Structurally, θ -Al₁₃Fe₄ has a large range of crystal chemistries due to Si and transition metal
419 incorporation. It has a monoclinic lattice with space group C2/m [6, 44]. There are 20
420 crystallographically distinct atomic sites (5 Fe and 15 Al) and 102 atoms in total in a unit cell
421 [6]. A recent work [24] on the calculation of the Si solution in θ -Al₁₃Fe₄ phase using first-
422 principles density-Functional Theory (DFT) showed that it is energetically favorable for Si to
423 replace some Al in specific sites in θ -Al₁₃Fe₄, but Si substitution into the Fe sites is very
424 unlikely due to the high energy associated with this. It showed that the increased energy
425 associated with Si substitution on 2 Al sites (Al8 and Al9) is negative, and on the other 2 sites
426 (Al6 and Al4) is less favourable with but with very minor increase in energy. It also revealed
427 that partial replacements of Al by Si at these sites break the local symmetry of the crystal,
428 resulting in a localised triclinic structure compared with the global monoclinic structure.

429 In this study, the lattice parameters of θ -Al₁₃Fe₄ without and with Si incorporation in different
430 Al alloys were measured and shown in Table 3, and the corresponding compositions of θ -
431 Al₁₃Fe₄ particles were measured and listed in Table 2. The X-ray diffraction patterns for the
432 single crystals revealed the lattice parameters: $a = 15.4824(3)$ Å, $b = 8.08146(15)$ Å, $c =$
433 $12.4689(3)$ Å and $\beta = 107.689(2)$ ° for a single crystal without Si, θ -Al₁₃Fe₄; and $a =$
434 $15.44239(11)$ Å, $b = 8.0521(5)$ Å, $c = 12.4040(8)$ Å and $\beta = 107.649(7)$ ° for a single crystal
435 with Si, θ -(Al_{1-x}Si_x)₁₃Fe₄ with $x = 0.024$. The results showed the crystal structure of θ -Al₁₃Fe₄
436 remains monoclinic, although the Si substitutes in θ -Al₁₃Fe₄ phase with a concentration is up
437 to 2.7at. %. The experimental results in this work revealed that the lattice parameters and cell
438 volume of θ -Al₁₃Fe₄ decreases with the increase of Si concentration. This is supported by the
439 DFT calculation [24]. After increased amount of Si atoms diffused into θ -Al₁₃Fe₄ crystals, more
440 Al sites were replaced with Si and the symmetry of θ -Al₁₃Fe₄ crystal was gradually changed
441 and finally transformed into the other types of FIMCs.

442 Both the calculation and the experimental results indicated that Si can go into θ phase but only
443 up to a given concentration. Our calculation results shown in Fig.11 revealed that the FIMCs
444 became unstable when the Si concentration reach their solubility. Therefore, the Si
445 concentration of FIMCs at the interface that phase transformed to the other types of FIMCs can
446 be considered as their maximum solubility. For example, during the multi-step phase
447 transformation from θ to α' , α' to β , and β to δ , the solubility of Si in these FIMCs can be

448 considered as 2.7at.% of θ , 10.4at.% of α' , and 16.9at.% of β , respectively. The solubility of Si
449 in different FIMCs can change with the experimental conditions such as temperature at which
450 the phases transformation can occur. Further investigation is required to understand the
451 relationship between the alloy composition, concentration of Si in the FIMC and phase
452 stability.

453 Recent research [21] showed that the phase transformation among different types of FIMCs
454 are diffusion controlled. Therefore, which types of FIMCs form through phase transformation
455 from θ -Al₁₃Fe₄ depends on many factors such as alloy composition, cooling rate. Additionally,
456 a few pairs of ORs between θ and the other FIMCs, α' , β were identified. These ORs contains
457 some crystallographic information of the structure transition between these FIMCs. Further
458 investigation is working.

459 The calculation results also revealed that the chemical composition of β -phase is Al_{4.5}FeSi,
460 which is similar as the experimental observation [38]. However, the Si distribution is different
461 from that reported previously. The experimental model suggested a homogeneous distribution
462 of Si at the Al sites, whereas the first-principles calculations predicted that the Si atoms are at
463 either the Al1 or the Al6 site. Additionally, the DFT simulation also showed a high
464 configurational entropy contribution for increased Si solution in the β -phase. This indicates
465 that at high temperature (>700K), the β -phase may contain more Si than the configuration of
466 stable structure at ambient conditions [41].

467 4.3 Effects of thermodynamic on phase transformation of θ -Al₁₃Fe₄

468 Naturally, the chemical composition has an impact on the formation of θ -Al₁₃Fe₄ phase in Al
469 alloys. The concentration of Si in the θ -Al₁₃Fe₄ phase depending on the chemical composition
470 in the Al alloys and casting conditions. The details of phase transformation mechanisms
471 between different types of FIMCs have been reported in our recent contributions [21]. It is
472 reported that these phase transformations between various FIMCs are diffusion-controlled. The
473 phase transformation of FIMCs from θ -(Al,Si)₁₃Fe₄ with a low Si concentration to other
474 FIMCs with a higher Si content (such as α' -Al₈Fe₂Si, α -Al₁₅(Fe,Mn)₃Si₂, β -Al₅FeSi) depends
475 on the Fe and Si diffusion at high temperature and long holding times. The TEM-EDX results
476 from various FIMCs observed in this study, Table 2, showed that the Fe content decreased, and
477 the Si content increased in each of the FIMC as the phase transformation sequence progressed
478 from θ -Al₁₃Fe₄ to α -Al₁₅(Fe, Mn)₃Si₂, α' -Al₈Fe₂Si and β -Al₅FeSi. The experimentally
479 measured Si concentration in Table 2 revealed a sequence among different types of FIMCs as:
480 $C_{\theta}^{Si} < C_{\alpha}^{Si} < C_{\alpha'}^{Si} < C_{\beta}^{Si}$. The experimental results in this study showed a complicated phase selection
481 and the variable following phase transformations depending on the alloy composition, which
482 illustrated that in high Si containing Al alloys, at certain casting conditions, especially at slow
483 solidification process. The FIMCs such as α' -Al₈Fe₂Si, α -Al₁₅(Fe,Mn)₃Si₂, β -Al₅FeSi with
484 higher Si content is more stable than those with a lower Si content FIMCs such as θ -Al₁₃Fe₄,
485 indicating the possible thermodynamic stability of these phases at the investigated alloys.

486 However, the final microstructure selection was resulted from the effects of multiple factors,
487 such as thermodynamic, nucleation difficulty, etc.

488

489 5. Conclusions

490

491 (1) The experimental measured lattice parameters (a , b , c) of θ - $\text{Al}_{13}\text{Fe}_4$ decreases with the
492 increasing Si concentration in θ - $\text{Al}_{13}\text{Fe}_4$ particles formed in different Al alloys. However,
493 the maximum Si concentration doped in θ - $\text{Al}_{13}\text{Fe}_4$ measured from experimental results is
494 lower than that of calculation.

495 (2) Multi types of phase transformation between θ - $\text{Al}_{13}\text{Fe}_4$ and the other types of FIMCs were
496 observed in Al-Fe-Si alloys.

497 1) $\text{L} + \theta\text{-Al}_{13}\text{Fe}_4 \rightarrow \alpha'\text{-Al}_8\text{Fe}_2\text{Si} + \alpha\text{-Al}$

498 2) $\text{L} + \theta\text{-Al}_{13}\text{Fe}_4 \rightarrow \beta\text{-Al}_5\text{FeSi} + \alpha\text{-Al}$

499 3) $\text{L} + \text{AlFe} \rightarrow \theta\text{-Al}_{13}\text{Fe}_4 + \alpha\text{-Al}$

500 4) $\text{L} + \theta\text{-Al}_{13}\text{Fe}_4 \rightarrow \alpha\text{-Al}_{15}(\text{Fe}, \text{Mn})_3\text{Si}_2 + \alpha\text{-Al}$

501 (3) The orientation relationships between $\text{Al}_{13}\text{Fe}_4$ and the other types of FIMCs were well-
502 defined.

503 A. $(10\bar{3})\alpha'\text{-Al}_8\text{Fe}_2\text{Si} // (11\bar{1})\theta\text{-Al}_{13}\text{Fe}_4$, and $[\bar{3}2\bar{1}]\alpha'\text{-Al}_8\text{Fe}_2\text{Si} // [\bar{1}\bar{3}\bar{4}]\theta\text{-Al}_{13}\text{Fe}_4$

504 B. $(020)\beta\text{-Al}_5\text{FeSi} // (010)\theta\text{-Al}_{13}\text{Fe}_4$, and $[100]\beta\text{-Al}_5\text{FeSi} // [001]\theta\text{-Al}_{13}\text{Fe}_4$

505 C. $(1\bar{1}\bar{1})\text{AlFe} // (001)\theta\text{-Al}_{13}\text{Fe}_4$, and $[112]\text{AlFe} // [100]\theta\text{-Al}_{13}\text{Fe}_4$

506 D. $(\bar{2}01)\theta\text{-Al}_{13}\text{Fe}_4 // 2.3^\circ (0\bar{1}1)\alpha\text{-Al}_{15}(\text{Fe}, \text{Mn})_3\text{Si}_2$, and $[010]\theta\text{-Al}_{13}\text{Fe}_4 // [100]\alpha\text{-}$
507 $\text{Al}_{15}(\text{Fe}, \text{Mn})_3\text{Si}_2$

508 (4) The composition of different FIMCs solidified at different conditions are variable, which
509 caused the corresponding lattice parameters changes. The Si concentration in different
510 FIMCs has a sequence as: $C_\theta^{\text{Si}} < C_\alpha^{\text{Si}} < C_{\alpha'}^{\text{Si}} < C_\beta^{\text{Si}}$.

511

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