



33 Iron (Fe) is inevitably picked up during the fabrication of primary Al, and it cannot be removed  
34 completely during recycling [1-2]. Due to the low solid solubility in aluminum especially at  
35 the low temperature, the Fe usually forms intermetallic phases in Al alloys, such as  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>,  
36  $\alpha$ -Al<sub>15</sub>(Fe, Mn)<sub>3</sub>Si<sub>2</sub>, and  $\beta$ -Al<sub>5</sub>FeSi, etc. [4-7]. These Fe-containing intermetallic compounds  
37 (FIMCs) usually form as large particles with different morphologies, such as plate-like, needle-  
38 like, Chinese script [7-11]. They deteriorate the mechanical properties dramatically, especially  
39 the ductility. In the last decades, much effort has been made to reduce the detrimental effect on  
40 the mechanical properties, such as removal of Fe, modification of FIMCs morphology, and  
41 refinement of FIMCs, etc. However, it is reported that [12] the removal Fe is very limited when  
42 Fe is lower than 0.7wt.%, which is still undesirable for the mechanical properties. The  
43 techniques or theories on direct removal of iron from aluminum has so far made no satisfactory  
44 progress. Some transition metal elements such as Mn, Co, and Cr were used to modify the  
45 morphology of FIMCs [13-17]. However, these elements will increase the total amount of  
46 FIMCs, which is also harmful to the mechanical properties of Al alloys. In recent years,  
47 research has focused to some extent on the development of grain refinement techniques for  
48 these FIMCs by applying the heterogeneous nucleation theory [10,18-20]. The bottlenecks in  
49 technology development are due to the lack of the fundamental understanding on the formation  
50 mechanism of FIMCs and the relationship between different types of FIMCs. In recent years,  
51 our group has worked on the understanding on the heterogeneous nucleation of FIMCs and  
52 phase relationship between different types of FIMCs by investigating different types of phase  
53 transformation among these FIMCs experimentally and using crystallographic methods [21-  
54 24].

55 Many different types of FIMCs were reported in various Al-alloys. In Al-Fe-Si casting alloys,  
56 the most commonly observed FIMCs are  $\theta$ -Al<sub>13</sub>M<sub>4</sub> (M= Fe, Ni, Cr, Cu, etc.) (monoclinic),  $\beta$ -  
57 Al<sub>5</sub>FeSi (monoclinic),  $\alpha$ -Al<sub>15</sub>(Fe, Mn)<sub>3</sub>Si<sub>2</sub> (complex body-centered cubic (BCC)) and  $\alpha'$ -  
58 Al<sub>8</sub>Fe<sub>2</sub>Si (complex hexagonal) [3-6, 25]. The formation of these FIMCs is very sensitive to the  
59 alloy composition. The composition and lattice parameters of these FIMCs change with the  
60 alloy composition and formation conditions. These FIMCs have a range of compositions and  
61 lattice parameters, and they act like the “solid solution compounds”. For example, atomic  
62 positions of Al in  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>,  $\alpha$ -Al<sub>15</sub>(Fe, Mn)<sub>3</sub>Si<sub>2</sub> can be replaced with Si, and the atomic  
63 positions of Fe are substituted by other transition elements such as Mn or Cr. This also the case  
64 for the other FIMCs such as  $\beta$ -Al<sub>5</sub>FeSi and  $\alpha'$ -Al<sub>8</sub>Fe<sub>2</sub>Si. The alloying elements incorporated  
65 into the parent FIMCs not only causes change in crystal structure but also induce phase  
66 transition, e.g., Mn doping in  $\beta$ -Al<sub>5</sub>FeSi (monoclinic) cause transformation into  $\alpha$ -Al<sub>15</sub>(Fe,  
67 Mn)<sub>3</sub>Si<sub>2</sub> (BCC). The modification achieves more desirable types of FIMCs in terms of retaining  
68 mechanical properties especially the ductility by modifying the morphology of the FIMCs.  
69 However, the modification result in complicated heterogeneous nucleation and phase  
70 transformation process among different types of FIMCs, which makes the microstructure  
71 control even more difficult.

72  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> as one of the most common FIMCs in as-cast Al alloys is reported a monoclinic  
73 crystal structure with lattice parameters:  $a = 15.447 \text{ \AA}$ ,  $b = 8.057 \text{ \AA}$ ,  $c = 12.429 \text{ \AA}$  and  $\beta =$   
74  $107.80^\circ$  [6]. It has a monoclinic lattice with space group C2/m (nr. 12) [13]. There are 20  
75 crystallographically different atomic sites (5 Fe and 15 Al) and 102 atoms in total in a unit cell.  
76 The Al atoms have 10 to 12 neighbours including 2 to 4 Fe, except the Al<sub>2</sub> atoms at the  
77 Wyckoff 4i sites which have only 6 neighbours including two Fe with Fe-Al bond-lengths  
78 below  $3.0 \text{ \AA}$  ( $1 \text{ \AA} = 0.1 \text{ nm} = 10^{-10} \text{ m}$ ).  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> is an extremely impurity tolerant intermetallic  
79 compound as both Al and Fe may be substituted with other elements, such as Si, Cr, Ni, Mn,  
80 etc. [26-31]. Experiments show that Si can easily incorporate into the  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> at impurity or  
81 solute concentration levels in Al alloys. The elemental solution and the composition changes  
82 in FIMCs not only can cause the lattice parameters variation, but also can lead to phase  
83 transformations [21-22, 32-34]. Research published recently [21] reported the multi-step phase  
84 transformation from  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> to the other types of FIMCs  $\alpha'$ -Al<sub>8</sub>Fe<sub>2</sub>Si,  $\beta$ -Al<sub>5</sub>FeSi and  $\delta$ -  
85 Al<sub>4</sub>FeSi<sub>2</sub>. The variation on the phase transformation among the FIMCs have been reported in  
86 literature to be dependent on the composition and cooling conditions. The experimental  
87 evidence shows that the multi-step phase transformation from  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> to the other types of  
88 FIMCs is a diffusion-controlled phase transformation which is mainly affected by the Si  
89 diffusion.

90 However, the understanding of the reasons behind the variable phase transformation among the  
91 FIMCs is very limited due to the lack of the fundamental research on the mechanisms of phase  
92 transformation, the phase relationships, and the changes in crystal structure during the  
93 experiment. Our research group focus on the fundamental research on formation and grain  
94 refinement of FIMCs in Al alloys recent years. In this paper, we summarized the findings on  
95 the phase transformation between  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and the other types of FIMCs in a number of Al  
96 alloys with different Si, Fe ratios. The effect of Si dissolution on the crystallography and the  
97 internal defects of the  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> crystals in different Al alloys were investigated. The phase  
98 relationship between  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and the other FIMCs were investigated using TEM and single  
99 crystal X-ray analysis. The Si solubility in multiple types of FIMCs were investigated through  
100 the development of the structural models of different types of FIMCs. Finally, a mechanism of  
101 phase transformation between  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and the other FIMCs is proposed.

102

## 103 2. Experimental

104 In this study, numbers of Al casting alloys containing  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> which phase transformed into  
105 other types of FIMCs were investigated. The phase diagrams of these Al alloys were calculated  
106 using Pandat software using PanAluminum 2020 database [48]. The alloy compositions of  
107 these Al alloys were listed in Table 1. The starting materials (in wt.%) used in this work were  
108 high purity (HP) Al (99.99%), commercial purity (CP) Al (>99.86%), Al-45Fe, Al-20Mn, Al-  
109 50Si and CP Mg (>99.8%) master alloys. The melting temperatures of these alloys were  
110 calculated with the Pandat software using Scheil solidification model, as shown in Table 1. The  
111 casting temperatures are about  $50^\circ\text{C}$  above the melting temperatures of these alloys. The alloys

112 were produced by melting HP Al or CP Al and the master alloys in an electric resistance  
113 furnace. The master alloys were added to the molten HP Al or CP Al melts in the sequence of  
114 Al-Fe, Al-Mn, Al-Si (as required for the alloy), following by a completely mixing and  
115 sufficiently long holding time to ensure chemical homogeneity of the melt. The preheated CP  
116 Mg (200°C) covered with Al foil (as required by some alloys) was inserted into the melt as the  
117 last addition. After sufficiently mixing and holding isothermally for 20 minutes, the slag in  
118 these Al alloys was removed and cast into TP-1 moulds preheated to 380 °C [35]. To achieve  
119 the samples with bigger particles for single crystal X-ray tests, the remainder of melt in the  
120 crucibles was cooled to 200°C in the furnace, with an average cooling rate of 0.01K/s.

121 In addition to experimental alloys, an Al-3.7Ti-1B master alloy which contains 1wt.% Si and  
122 1.5wt.% Fe was also investigated. This alloy was produced by adding Al-Fe and Al-Si master  
123 alloys into the Al-3.7Ti-1.5B master alloy melt, and casted at 1K/s in a steel mold into a flat  
124 sample with thickness of 1-5mm was achieved. The casting procedure in details will be  
125 reported in our other contributions [36]. In this alloy, TiB<sub>2</sub> particles formed in Al-Fe-Si alloy  
126 with 0.4wt.% free Ti. Therefore, to simplify, we refer this alloy containing Al-1.5Fe-1Si-3.7Ti-  
127 1B as Al-1Si-1Fe alloy. In this study, the focus is on the phase transformation between FIMCs.  
128 An AlFe intermetallic compound with B2-type (CsCl) was observed. The phase transformation  
129 between AlFe and  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> was examined with the aid of this alloy. A square sample was  
130 sectioned from the flat sample of Al-1Si-1Fe alloy. The microstructural characterization was  
131 carried out on the middle of the thickness by grinding and polishing both surface of the flat  
132 sample. Samples for microstructural characterisation were prepared from the cross section of  
133 TP1 samples at the 38mm height from the bottom which solidifies at 3.5K/s [35], with the  
134 exception of Al-1Si-1Fe alloy. Metallographic specimens were prepared using the standard  
135 procedures. To observe the 3-dimensional morphology of the structure, the samples were  
136 gently etched in 10vol.% HCl+H<sub>2</sub>O solution for a few minutes followed by cleaning in ethanol.  
137 The as-solidified microstructure characteristics of the samples were examined using a Zeiss  
138 optical microscope fitted with the Axio Vision 4.3 image analysis system and a Zeiss Supra 35,  
139 field emission gun scanning electron microscope (FEG-SEM), operated at an accelerating  
140 voltage between 5-20kV. Thin foils for high resolution transmission electron microscopy  
141 (TEM) examinations were prepared from samples which were mechanically ground and cut  
142 into 3mm diameter discs. The discs were then manually ground to a thickness of less than 50  
143  $\mu$ m, followed by ion-beam-thinning using a Gatan precision ion polishing system (PIPS) at an  
144 energy of 2.0-5.0kV and an incident angle of 3-5°. TEM examination was performed on a JEOL  
145 2100F transmission electron microscope equipped with EDX spectrometer operated at an  
146 accelerating voltage of 200kV. The 3-dimensional morphology of the FIMCs was examined  
147 on Zeiss X radial 410 Versa X-ray –microscope operating at 80kV with power set to 10W to  
148 achieve the clearest image of intermetallic particles.

149 To investigate the crystal structure variation of FIMCs, the FIMCs crystal from different  
150 samples were examined with a single crystal X-ray diffraction. The lattice parameters from the

151 literature and the casting conditions of samples examined are shown in Table 3. The slowly  
152 cooled samples were deep etched in 5-10% HCl+H<sub>2</sub>O solution for a few minutes followed by  
153 ultrasonic cleaning in ethanol. After deep cleaning and drying, the large crystals of intermetallic  
154 particles from desired microstructure was cut under optical microscope and transferred to a  
155 clean glass slide. The crystal samples were further cut into the desired size (<100 μm) for the  
156 single crystal analysis. Single crystal data were collected at 100K using a Rigaku SuperNova,  
157 Dualflex, AtlasS2 diffractometer with Cu-Kα radiation (λ=1.54184 Å). CrysAlis Pro software  
158 was used for data collection, absorption correction and data reduction.

159 In order to get reliable information about the effects of Si solution on the stability and structural  
160 information about the related FIMCs, we performed first-principles study on these compounds  
161 [24, 41]. We utilized a plane-wave approach which is implanted into the first-principles code  
162 VASP (Vienna Ab initio Simulation Package) [46]. The Generalized Gradient Approximation  
163 (GGA-PBE) [47] was used for the exchange and correlation energy terms. We used a cut-off  
164 energy of 550 eV for the wave functions and the cut-off energy of 700 eV for the augmentation  
165 functions. More details are included in [24, 41].

166

### 167 3. Results

#### 168 3.1 θ-Al<sub>13</sub>Fe<sub>4</sub> in Al-Fe alloys

169 Si as one of the major impurities in Al alloys is easily picked up during casting or from the  
170 master alloys. It is reported that Si can dope in θ-Al<sub>13</sub>Fe<sub>4</sub> by replacing the Al atoms. The effects  
171 of the Si on the crystal structure and the consequently phase transformation of θ-Al<sub>13</sub>Fe<sub>4</sub> will  
172 be investigated in this study. Firstly, the initial structure of the θ-Al<sub>13</sub>Fe<sub>4</sub> free of Si was  
173 investigated as the reference. To produce such high pure θ-Al<sub>13</sub>Fe<sub>4</sub> particles, the high pure Al  
174 and the Al-45Fe master alloy were used to minimize the effect of Si impurity. The high pure  
175 Al was previously melted at 900 °C, and then the Al-45Fe master alloy was added into the Al  
176 melt with completely stirring until fully molten. An Al-3Fe alloy actually containing 3.25±0.5  
177 wt.% Fe was produced.

178 To compare the effect of Si as impurity on the θ-Al<sub>13</sub>Fe<sub>4</sub> phase, the other Al-1Fe alloy was  
179 produced with commercial pure Al and same Al-45Fe master alloy. The commercial pure Al  
180 was previously melted at 750 °C, and then the Al-45Fe was added into the Al melt and stirred  
181 until fully molten. The final composition of these two alloys were list in Table 1. It shows that  
182 the Si content in Al-3Fe is negligible when HP Al was used. The measured EDX composition  
183 of θ-Al<sub>13</sub>Fe<sub>4</sub> phase (Table 2) show that the Si concentration in (HP) Al-3Fe is negligible, but  
184 0.3at. % Si can be detected in the (CP) Al-1Fe. The single crystal X-ray results are shown in  
185 Table 3. The lattice parameters *a*, *b*, and *c* in θ-Al<sub>13</sub>Fe<sub>4</sub> in (HP) Al-3Fe are larger than that of  
186 θ-Al<sub>13</sub>Fe<sub>4</sub> in (CP) Al-1Fe. Table 3 also indicates that the lattice parameters *a*, *b*, and *c* of θ-  
187 Al<sub>13</sub>Fe<sub>4</sub> decreased with the increase in Si concentration.

188 The as-cast microstructure of the (HP)Al-3Fe, Fig.1, shows the typical star-like primary  $\theta$ -  
189  $\text{Al}_{13}\text{Fe}_4$  phase and the needle-like  $\theta\text{-Al}_{13}\text{Fe}_4 + \alpha\text{-Al}$  eutectic structure (Fig 1a). The 3D  
190 morphology of these two structures were shown in Figs.1b-c, respectively. Fig.1b shows that  
191 the primary  $\theta\text{-Al}_{13}\text{Fe}_4$  phase has the multi-faceted star-like morphology in cross section. The  
192 eutectic  $\theta\text{-Al}_{13}\text{Fe}_4$  phase associated with the primary  $\theta$  has plate-like morphology, as shown in  
193 Fig.1b. Some eutectic  $\theta\text{-Al}_{13}\text{Fe}_4$  phase was observed as needle-like morphology which is away  
194 from primary  $\theta$ , as illustrated in Fig 1c. There is no appreciable difference in the morphology  
195 of  $\theta\text{-Al}_{13}\text{Fe}_4$  in HP Al-3Fe and CP Al-3Fe (Fig.1d) except the particle size.

196 Fig.2a shows the bright field TEM image presenting the needle-like morphology of eutectic  $\theta$ -  
197  $\text{Al}_{13}\text{Fe}_4$  phase in (CP)Al-1Fe alloy solidified from 720 °C at a cooling rate of 3.5 K/s. Two  
198 different types of faceted planes were observed on  $\theta\text{-Al}_{13}\text{Fe}_4$  phase, Figs.2b-c. The high  
199 resolution TEM (HRTEM) images show the faceted (010) planes and (102) planes of  $\theta\text{-Al}_{13}\text{Fe}_4$   
200 phase when viewed along the  $[\bar{2}01]$  zone direction.

201 As reported [37],  $\theta\text{-Al}_{13}\text{Fe}_4$  can be twinned easily. In as-cast Al-1Fe (CP Al) alloy, the twinning  
202 structure of  $\theta\text{-Al}_{13}\text{Fe}_4$  is readily observed. One example is shown in Fig.3. The HRTEM image  
203 (Fig.3a) and the corresponding selected area diffraction (SAED) patterns (Figs.3b-c) show that  
204 the  $\theta\text{-Al}_{13}\text{Fe}_4$  crystal has leaf-like symmetrical twinning. The SAED pattern, Fig.3d, contains  
205 two overlapping patterns with a  $36\pm 0.5^\circ$  rotation angle between the two sets of the SAED  
206 patterns. This provides for tenfold twins, as the orientation difference between neighbouring  
207 twins are very close to  $36^\circ$ . The higher magnification HRTEM image, Fig.3e, shows that in the  
208 very localised areas, there are multi-step twinning and some disordered regions.

209

### 210 3.2 $\theta\text{-Al}_{13}\text{Fe}_4$ in Al-4Fe-4Si alloy

211 Section 3.1 reported the result that Si can incorporate in  $\theta\text{-Al}_{13}\text{Fe}_4$  at impurity concentration  
212 level in Al alloys. Here, the effect of Si on the crystal structure of  $\theta\text{-Al}_{13}\text{Fe}_4$  in Al-Si-Fe alloys  
213 will be investigated. An Al-4Si-4Fe alloy with approximately equal concentration of Si and Fe  
214 (wt.%) was designed and cast. The Al alloy in this work had a composition of  $4.21\pm 0.5$  Si, and  
215  $4.10\pm 0.6$  Fe (in wt%) with Al balance. The phase diagram of the Al-4Fe-xSi system was  
216 calculated with the Pandat software and its associated Al-database as shown in Fig.12b. It  
217 shows that the  $\theta\text{-Al}_{13}\text{Fe}_4$  is calculated as the primary equilibrium phase. The melting  
218 temperature of Al-4Fe-4Si is calculated as  $715^\circ\text{C}$  with the Scheil solidification model. The  
219 microstructure of Al-4Si-4Fe alloy cast from  $770^\circ\text{C}$  at a cooling rate of 3.5K/s is shown in  
220 Fig.4. The microstructure consisted of multiple types of FIMCs which have star-like ( $\theta$ -  
221  $\text{Al}_{13}\text{Fe}_4$ ) and compacted morphology ( $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ ), and multiple FIMCs in eutectic structures  
222 which have Chinese script morphology ( $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ ) and needle-like morphology ( $\theta\text{-Al}_{13}\text{Fe}_4$ ).  
223 All the phases in this study were identified with SEM-EDX and subsequent TEM analysis. The  
224 details of primary star-like  $\theta\text{-Al}_{13}\text{Fe}_4$  was examined carefully with SEM, and the results are

225 shown in Figs.4b-c. Fig.4b shows the high magnification SEM-BSE (backscattered electron)  
226 image of a primary  $\text{Al}_{13}\text{Fe}_4$  particle with a brighter central phase ( $\theta\text{-Al}_{13}\text{Fe}_4$ ) and grey surface  
227 phase ( $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ ). The interface between  $\theta\text{-Al}_{13}\text{Fe}_4$  and  $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$  presents irregular under  
228 SEM-BSE observation. The morphology in Fig.4b indicates a reaction typical of a  
229 transformation:  $\text{L} + \theta\text{-Al}_{13}\text{Fe}_4 \rightarrow \alpha'\text{-Al}_8\text{Fe}_2\text{Si} + \alpha\text{-Al}$ .

230 It is noted that more than one type of phase transformation was observed on the surface of  
231 primary  $\theta\text{-Al}_{13}\text{Fe}_4$ . Fig.4c shows the primary  $\theta\text{-Al}_{13}\text{Fe}_4$  particle with bright white central region  
232 ( $\theta\text{-Al}_{13}\text{Fe}_4$ ) and sharp needle-like grey surface phase ( $\beta\text{-Al}_5\text{FeSi}$ ). The interface is irregular  
233 based on SEM observations. The morphology in Fig.4c also indicates a reaction:  $\text{L} + \theta\text{-Al}_{13}\text{Fe}_4$   
234  $\rightarrow \beta\text{-Al}_5\text{FeSi} + \alpha\text{-Al}$ .

235 The TEM-EDX compositions of  $\theta\text{-Al}_{13}\text{Fe}_4$ ,  $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$  and  $\beta\text{-Al}_5\text{FeSi}$  observed in this alloy  
236 are listed in Table 2. The  $\theta\text{-Al}_{13}\text{Fe}_4$  phase contains  $2.7 \pm 0.2$  at. %Si. However, the transformed  
237  $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$  and  $\beta\text{-Al}_5\text{FeSi}$  have much higher Si concentration at  $10.4 \pm 0.1$  at. % and  $16.9 \pm 0.1$  at.  
238 %, respectively.

239 To investigate the phase transformation mechanisms between  $\theta\text{-Al}_{13}\text{Fe}_4$  and the other FIMCs,  
240 the interface between  $\theta\text{-Al}_{13}\text{Fe}_4$ /FIMCs were observed under TEM. The orientation  
241 relationships between the parent  $\theta$  phase and the transformed FIMCs are examined from several  
242 different pairs of zone directions during the TEM analysis. Some examples with lower indexed  
243 zone directions will be presented here.

244 The HRTEM image, Fig.5a, shows the interface between  $\theta\text{-Al}_{13}\text{Fe}_4$  and  $\text{Al}_8\text{Fe}_2\text{Si}$  when viewed  
245 along the zone direction of  $[\bar{1}\bar{3}\bar{4}]$  of  $\theta\text{-Al}_{13}\text{Fe}_4$  and  $[\bar{3}2\bar{1}]$  of  $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$ . The interface is not  
246 sharp, and some transition area can be observed at the interface. The fast Fourier transformation  
247 (FFT) patterns of  $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$  phase and  $\theta\text{-Al}_{13}\text{Fe}_4$  phase are shown in Fig.5b-c. The FFT  
248 pattern (Fig.5d) containing both phases and its indexed pattern (Fig.5e) reveal an orientation  
249 relationship (OR) between  $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$  and  $\theta\text{-Al}_{13}\text{Fe}_4$ :  $(10\bar{3}) [\bar{3}2\bar{1}] \alpha'\text{-Al}_8\text{Fe}_2\text{Si} // (11\bar{1}) [\bar{1}\bar{3}\bar{4}]$   
250  $\theta\text{-Al}_{13}\text{Fe}_4$ .

251 The TEM-EDX composition of  $\theta\text{-Al}_{13}\text{Fe}_4$  in Al-4Fe-4Si contains  $2.7 \pm 0.2$  at.% Si, and  $20.6 \pm 0.5$   
252 at.% Fe, and the composition of  $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$  is  $10.4 \pm 0.1$  at.% Si, and  $15.3 \pm 0.1$  at.% Fe. The  
253 lattice parameters of  $\theta\text{-Al}_{13}\text{Fe}_4$  measured with single crystal X-ray was  $15.424 \text{ \AA}$  ( $a$ ),  $8.052 \text{ \AA}$   
254 ( $b$ ),  $12.404 \text{ \AA}$  ( $c$ ), with  $107.7^\circ$  ( $\beta$ ). The lattice parameters of  $\alpha'\text{-Al}_8\text{Fe}_2\text{Si}$  measured with TEM  
255 was  $12.13 \text{ \AA}$  ( $a$ ),  $12.13 \text{ \AA}$  ( $b$ ),  $26.68 \text{ \AA}$  ( $c$ ).

256 The HRTEM image, Fig.6a, shows the interface between  $\theta\text{-Al}_{13}\text{Fe}_4$  and  $\beta\text{-Al}_5\text{FeSi}$  when  
257 viewed along the zone direction of  $[001]$  of  $\theta\text{-Al}_{13}\text{Fe}_4$  and  $[100]$  of  $\beta\text{-Al}_5\text{FeSi}$ . The interface is  
258 again a diffuse interface, and a transition area can be observed at the interface, suggesting  
259 continuous incorporation of Si into the structure. The fast Fourier transformation (FFT) patterns  
260 of  $\beta\text{-Al}_5\text{FeSi}$  phase and  $\theta\text{-Al}_{13}\text{Fe}_4$  phase are shown in Figs.6b-c. The FFT patterns containing

261 both phases are shown in Fig.6d. The schematic diagram showing the indexed FFT of Fig.6d  
262 is in Fig.6e. These results indicate an OR between  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and  $\beta$ -Al<sub>5</sub>FeSi to be: (020) [100]  
263  $\beta$ -Al<sub>5</sub>FeSi // (010) [001]  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>. The TEM-EDX result, Table 2, shows that the  $\beta$ -Al<sub>5</sub>FeSi  
264 contains 16.9±0.1 at. % Si, which is higher than that of  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> (2.7±0.2 at. % Si) and  $\alpha'$ -  
265 Al<sub>8</sub>Fe<sub>2</sub>Si (10.4±0.1 at. % Si).

266

### 267 3.3 $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> in Al-1Fe-1Si (-3.7Ti-1.5B) alloy

268 The phase transformation between  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and AlFe in Al-1Fe-1Si alloy containing TiB<sub>2</sub>  
269 particles was investigated to understand the effect of heterogeneous sites for nucleation on the  
270 choice of FIMC. The SEM-SE (secondary electron) image, Fig.7, shows the microstructure of  
271 Al-1Si-1Fe(-3.7Ti-1.5B) alloy with 0.4wt.% free Ti solidified at 1K/s, indicating a  
272 microstructure with a mixture of FIMCs. The TiB<sub>2</sub> particles agglomerations distribute  
273 randomly in the Al grains or at the grain boundary. Some larger FIMC particles with long plate-  
274 like or needle-like morphology distribute in the Al grains, which can be considered as primary  
275 FIMCs. This FIMC was identified as AlFe which has B2-CsCl structure via TEM analysis. The  
276 AlFe phase observed here is not expected according to the Al-Fe phase diagram calculations.  
277 We expect localised inhomogeneities in the liquid composition and the presence of TiB<sub>2</sub>  
278 particles may promote this phase. The phase transformation from AlFe to  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> observed  
279 in this alloy illustrates the instability of this phase. Some smaller plate or needle-like FIMCs  
280 distribute at the grain boundaries, which are likely to be FIMCs in the eutectic structures. These  
281 FIMC in the eutectic structure was identified as  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> phase with TEM analysis. AlFe  
282 phase is rarely reported in cast Al alloys. In addition, a phase transformation was observed at  
283 the surface of AlFe with TEM, and a well-defined OR was identified and shown in Fig.8.

284 The bright field TEM image, Fig.8a, shows the needle-like central AlFe phase with the  $\theta$ -  
285 Al<sub>13</sub>Fe<sub>4</sub> phase at the surface. The TEM-EDX results, Table 2, show that the AlFe contains  
286 1.5±0.1 at. % Si, and the  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> contains 2.4±0.1 at. % Si. The Si is likely to be continuously  
287 incorporated into AlFe phase during the solidification progresses, and the phase transformation  
288 occurs from AlFe to  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> through a reaction: L + AlFe →  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> +  $\alpha$ -Al.

289 The SAED patterns from AlFe,  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and from a region containing both phases are shown  
290 in Figs.8b-d, when viewed along the [112] zone direction of AlFe and [100]  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>,  
291 respectively. Fig.8e shows the schematic illustration of the SAED in Fig.8d. The HRTEM  
292 image, Fig.8f, shows the interface between AlFe and  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>. Many planar defects can be  
293 observed on the  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> phase. The interface between the two phases reveals an orientation  
294 relationship of (1 $\bar{1}\bar{1}$ )AlFe// (001)  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>, and [112] AlFe// [100]  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>.

295

### 296 3.4 $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> in Al-Fe-Mn-Si-Mg alloys

297 The phase transformation between  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and the  $\alpha$ -Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub> was observed in Al-  
298 5Mg-2Si-0.7Mn-1.2Fe alloy. The Al alloy in this work had a composition of 5.1±0.5Mg,  
299 2.0±0.3 Si, 0.6±0.1 Mn and 1.3±0.05 Fe (in wt%) with Al balance. The phase diagram of the  
300 Al-5Mg-2Si-0.6Mn-xFe system was calculated with the Pandat software and its associated Al-  
301 database as shown in Fig.12c. It shows that the  $\alpha$ -Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub> is calculated as primary  
302 equilibrium phase. The as-cast microstructure of this alloy solidified at 3.5K/s is shown in  
303 Fig.9. The formation of FIMCs in this alloy is complicated and the details has been reported in  
304 pervious contribution [22]. The SEM-BSE image, Fig.9a, shows that in this sample, the FIMCs  
305 are mainly in plate-like and Chinese script morphologies. The high magnification SEM  
306 observation on the local area marked in Fig.9a is shown in Fig.9b. The compacted grey particles  
307 ( $\alpha$ -Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub>) which leading a Chinese script morphology FIMC connects and grows  
308 from the plate-like FIMC ( $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>). The calculated phase diagram, Fig.12c, shows that the  
309 equilibrium primary phase of Al-5Mg-2Si-0.7Mn-1.2Fe alloy supposed to be  $\alpha$ -  
310 Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub>, but not  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>. However, due to the smaller nucleation undercooling [20],  
311 the  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> nucleated firstly on the native MgAl<sub>2</sub>O<sub>4</sub> particles [22], and transformed into  $\alpha$ -  
312 Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub> via a reaction:  $L + \theta\text{-Al}_{13}\text{Fe}_4 \rightarrow \alpha\text{-Al}_{15}(\text{Fe,Mn})_3\text{Si}_2 + \alpha\text{-Al}$ .

313 The interface between  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and  $\alpha$ -Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub> was investigated with TEM, Fig.10. A  
314 well-defined OR between these two phases was identified. The dark field TEM image, Fig.10a,  
315 shows the interface between  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and  $\alpha$ -Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub> when viewed along the [010]  
316 zone direction of  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>. Some nano-scaled size  $\alpha$ -Al can be seen from the  $\alpha$ -  
317 Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub>, which indicates the alloy elements diffusion during the phase transformation.  
318 The HRTEM image containing both  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and  $\alpha$ -Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub> are shown in Fig.10b  
319 [22]. The corresponding schematic indexed FFT patterns is shown in Fig.10c [22]. The results  
320 reveal an orientation relationship between  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and  $\alpha$ -Al<sub>15</sub>(Fe, Mn)<sub>3</sub>Si<sub>2</sub>:  $(\bar{2}01) \theta\text{-Al}_{13}\text{Fe}_4$   
321  $// 2.3^\circ (0\bar{1}1)\alpha\text{-Al}_{15}(\text{Fe, Mn})_3\text{Si}_2$ , and  $[010] \theta\text{-Al}_{13}\text{Fe}_4 // [100] \alpha\text{-Al}_{15}(\text{Fe, Mn})_3\text{Si}_2$ . In addition,  
322 the TEM-EDX result, Table 2, shows that in this alloy, not only Si (1.8±0.1 at.%), but also Mn  
323 (6.4±0.1at.%) can incorporate into  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> phase in Al-5Mg-2Si-0.7Mn-1.2Fe alloy, which  
324 requires further investigation.

325

### 326 3.5 First principles calculation and related thermodynamics for the FIMCs

327 The experimental results revealed that the phase transformation between different types of  
328 FIMCs is a diffusion-controlled process. During the phase transformation, the vital element  
329 which determinate different phase transformation reactions is Si. Each FIMC has significant  
330 difference in Si concentration, Table 2. Therefore, the difference in crystal structure and the  
331 atomic sites of these FIMCs were investigated based on the reported structural models [3, 24-  
332 25, 38]. The solubility of Si in and phase stability of different FIMCs are compared based on  
333 the structural models in the literature, Table 4. Further to that, the solubility of Si using different

334 structural models were calculated and compared to the experimentally measured Si  
335 concentration.

336 The solubility of Si in different FIMCs based on the above crystal structural models were  
337 calculated and shown in Table 4. It shows that the Si solubility in FIMCs has a sequence as:  $\beta$ -  
338  $\text{Al}_5\text{FeSi}$  (15.38%) >  $\alpha'$ - $\text{Al}_8\text{Fe}_2\text{Si}$  (9.80%) >  $\alpha$ - $\text{Al}_{15}(\text{Fe}, \text{Mn})_3\text{Si}_2$  (7.68%) >  $\theta$ - $\text{Al}_{13}\text{Fe}_4$  (4.9%). The  
339 Si concentration in  $\theta$ - $\text{Al}_{13}\text{Fe}_4$  (4.9%) compound is based on the compound model calculated  
340 with DFT. As shown in Table 4, the Si concentrations in compounds  $\alpha'$ - $\text{Al}_8\text{Fe}_2\text{Si}$ ,  $\beta$ - $\text{Al}_{4.5}\text{FeSi\_I}$   
341 and  $\alpha$ - $\text{Al}_{15}(\text{Fe}, \text{Mn})_3\text{Si}_2$  are based on the compound models calculated from the literatures [25,  
342 38, 3] which based on the experimental compound compositions. The Si concentrations in  
343 compound  $\beta$ - $\text{Al}_{4.5}\text{FeSi\_II}$  and  $\beta$ - $\text{Al}_{4.375}\text{FeSi}_{1.125\_III}$  is based on the First-principles calculation  
344 done in this work. Our measured experimental Si concentrations in different types of FIMCs  
345 using TEM-EDX shows the same trend in the amount of Si incorporated into the structures as  
346 those of the calculated Si concentrations sequence. There is a significantly large gap between  
347 the maximum Si concentrations determined purely on DFT calculations and the experimentally  
348 measured Si solubility in FIMCs. Our experimental result shows that a 2.7 at.% Si is  
349 incorporated into  $\theta$ - $\text{Al}_{13}\text{Fe}_4$ , but the result from crystal structural model calculated with DFT is  
350 up to 4.9 at.% [24]. The DFT calculation reveals a theoretical possibility of Si concentration in  
351 compounds regardless of phase stability, which can provide some valuable information for the  
352 further investigation. Further studies are going to continue to build new crystal structural  
353 models for the other FIMCs using DFT calculations.

354 Both experimental and theoretical efforts have been made to obtain structural models for the  
355 FIMCs investigated. Experimental evidence revealed the complexity of crystal structures with  
356 partial occupation and/or multiple atomic species occupations at the Wyckoff sites in these  
357 FIMCs. This provides extra freedom for the crystals, Table 4. The primary FIMCs form at  
358 elevated temperatures during casting. At high temperature, the extra freedom at the atomic sites  
359 becomes an important factor in determining the relative stability of the FIMCs. To obtain a  
360 further insight into the crystal chemistry of the Fe-IMCs, parameters-free first-principles  
361 methods have been used [24, 39-41]. The first-principles calculations have been conducted to  
362 investigate the Si solution in FIMCs including  $\theta$ - $\text{Al}_{13}\text{Fe}_4$  [24] and  $\beta$ - $\text{Al}_{5.5}\text{Fe}$  [41]. The calculated  
363 results are summarized in Fig.11. The  $\beta$ - $\text{Al}_{5.5}\text{Fe}$  has higher formation energy compared with  $\theta$ -  
364  $\text{Al}_{13}\text{Fe}_4$ , in agreement with the experimental observations that the  $\theta$ -phase is the stable phase  
365 whereas the  $\beta$ -phase is not in the binary Fe-Al phase diagram. At low temperatures, the most  
366 stable configuration is  $\theta$ - $\text{Al}_{5.69}(\text{Si}^{\text{IX}})_{0.31}\text{Fe}_4$  containing 3.92 at. % of Si [24].

367 First-principles calculation, Fig.11b, reveals that a high concentration of Si goes into solution  
368 in  $\beta$ -phase and the configuration of the highest stability with respect to the elemental Al, Si and  
369 Fe is when Al11 sites ( $\beta$ - $\text{Al}_{4.5}\text{Si}^{\text{I}}\text{Fe}$ ) or Al6 site ( $\beta$ - $\text{Al}_{4.5}\text{Si}^{\text{VI}}\text{Fe}$ ) which contains 15.38 at% Si,  
370 are fully occupied by Si at the ambient conditions [39]. The first-principles calculations also  
371 showed that addition of more Si to the configurations of high stability at ambient condition,

372 e.g. ( $\beta$ -Al<sub>4.5</sub>Si<sup>1</sup>Fe) may increase the formation energy, but it also increases the number of  
373 configurations significantly. At 1000K the  $\beta$ -phase has 15.38at% to 21.15at % Si content [39],  
374 whereas the Si content in the  $\theta$ -phase is between 2.94 at% and 4.90at% due to the configuration  
375 entropy contributions [24]. This indicates that the Si concentration in the Fe-IMCs depends on  
376 the chemical compositions of the alloy and the casting process.

#### 377 4. Discussion

378

##### 379 4.1 Heterogeneous nucleation effects on phase transformation of $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>

380 In this study, 5 different Al-Fe alloys were investigated, where  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> phase formed during  
381 solidification as a primary intermetallic or as an intermetallic in the eutectic structure. Multiple  
382 types of phase transformation were observed in corresponding samples from  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> to the  
383 other types of FIMCs. The  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> in Al-1Fe-1Si, Al-4Fe-4Si alloys was calculated as  
384 equilibrium phase using Pandat software based on Scheil solidification model to illustrate the  
385 2D vertical-sections at given alloy chemistry with varying Si concentrations, Figs.12a-b. The  
386 Al<sub>13</sub>Fe<sub>4</sub> in other alloys such as Al-5Mg-2Si-0.7Mn-1.2Fe alloy was calculated to be a non-  
387 equilibrium phase, Fig.12c. However, during the casting process, the phase selection of the  
388 FIMCs can be different to that calculated phases due to the non-equilibrium phase selections  
389 [11, 21-22]. The changes to phase selection during the solidification process will cause the  
390 non-equilibrium phase transformation and solidification sequence. For example, the Al<sub>13</sub>Fe<sub>4</sub>  
391 formed in place of the equilibrium  $\alpha$ -Al<sub>15</sub>(Fe, Mn)<sub>3</sub>Si<sub>2</sub> phase in Al-5Mg-2Si-0.7Mn-1.2Fe alloy  
392 and then transformed into equilibrium  $\alpha$ -Al<sub>15</sub>(Fe, Mn)<sub>3</sub>Si<sub>2</sub> during further cooling. The AlFe  
393 formed first instead of the equilibrium  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> phase in Al-1Fe-1Si(-3.7Ti-1.5B) alloy and  
394 then transformed into the equilibrium  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>. The most complicated case is the FIMCs  
395 formation in the Al-4Fe-4Si alloy, Fig.12b. Multiple primary FIMCs such as  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and  $\alpha'$ -  
396 Al<sub>8</sub>Fe<sub>2</sub>Si formed (Fig.4a), and multiple types of phase transformation between  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and  
397 the other types of FIMCs such as  $\alpha'$ -Al<sub>8</sub>Fe<sub>2</sub>Si,  $\beta$ -Al<sub>5</sub>FeSi were observed. The solidification  
398 sequence and the complicated transformation sequence was presented in detail in a separate  
399 contribution [45].

400 The previous research [11, 21-22, 32-34] showed that the formation of FIMCs during the  
401 solidification is very sensitive to the alloy compositions, solidification conditions etc., which  
402 can easily be changed. Many types of phase transformation between different types of FIMCs  
403 have been reported in different alloys under different casting conditions. Recent research  
404 reported [20, 22] that the variations in phase selection among these FIMCs is due to the  
405 difficulties associated with nucleation which required multiple constitutive elements and large  
406 undercooling. It also shows that the  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> requires smaller number of elements and smaller  
407 nucleation undercooling compared to the other types of common FIMCs in as-cast Al alloys.  
408 This is likely why it is easier to form  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> in Al alloys such as Al-5Mg-2Si-0.7Mn-1.2Fe  
409 than the calculated equilibrium  $\alpha$ -Al<sub>15</sub>(Fe, Mn)<sub>3</sub>Si<sub>2</sub> phase. The other factors such as the TiB<sub>2</sub>

410 can also change the phase selection of FIMCs. In this study, the Al-1Fe-1Si alloy containing  
411 TiB<sub>2</sub> particles and 0.4% free Ti promoted a metastable AlFe phase formation in place of  $\theta$ -  
412 Al<sub>13</sub>Fe<sub>4</sub>. The non-equilibrium AlFe phase is not stable in the alloy and subsequently  
413 transformed into  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>. It is reported [20, 42-43] that the additional elements in the Al-Ti-  
414 B master alloys can change the interfacial segregation on the TiB<sub>2</sub> interface, which therefore  
415 changed the nucleation potency of these TiB<sub>2</sub> particles and promote the formation of one phase  
416 over another.

#### 417 4.2 Effects of Si on the crystal structural of $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> and $\beta$ -phase

418 Structurally,  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> has a large range of crystal chemistries due to Si and transition metal  
419 incorporation. It has a monoclinic lattice with space group C2/m [6, 44]. There are 20  
420 crystallographically distinct atomic sites (5 Fe and 15 Al) and 102 atoms in total in a unit cell  
421 [6]. A recent work [24] on the calculation of the Si solution in  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> phase using first-  
422 principles density-Functional Theory (DFT) showed that it is energetically favorable for Si to  
423 replace some Al in specific sites in  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>, but Si substitution into the Fe sites is very  
424 unlikely due to the high energy associated with this. It showed that the increased energy  
425 associated with Si substitution on 2 Al sites (Al8 and Al9) is negative, and on the other 2 sites  
426 (Al6 and Al4) is less favourable with but with very minor increase in energy. It also revealed  
427 that partial replacements of Al by Si at these sites break the local symmetry of the crystal,  
428 resulting in a localised triclinic structure compared with the global monoclinic structure.

429 In this study, the lattice parameters of  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> without and with Si incorporation in different  
430 Al alloys were measured and shown in Table 3, and the corresponding compositions of  $\theta$ -  
431 Al<sub>13</sub>Fe<sub>4</sub> particles were measured and listed in Table 2. The X-ray diffraction patterns for the  
432 single crystals revealed the lattice parameters:  $a = 15.4824(3)$  Å,  $b = 8.08146(15)$  Å,  $c =$   
433  $12.4689(3)$  Å and  $\beta = 107.689(2)$  ° for a single crystal without Si,  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>; and  $a =$   
434  $15.44239(11)$  Å,  $b = 8.0521(5)$  Å,  $c = 12.4040(8)$  Å and  $\beta = 107.649(7)$  ° for a single crystal  
435 with Si,  $\theta$ -(Al<sub>1-x</sub>Si<sub>x</sub>)<sub>13</sub>Fe<sub>4</sub> with  $x = 0.024$ . The results showed the crystal structure of  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>  
436 remains monoclinic, although the Si substitutes in  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> phase with a concentration is up  
437 to 2.7at. %. The experimental results in this work revealed that the lattice parameters and cell  
438 volume of  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> decreases with the increase of Si concentration. This is supported by the  
439 DFT calculation [24]. After increased amount of Si atoms diffused into  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> crystals, more  
440 Al sites were replaced with Si and the symmetry of  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> crystal was gradually changed  
441 and finally transformed into the other types of FIMCs.

442 Both the calculation and the experimental results indicated that Si can go into  $\theta$  phase but only  
443 up to a given concentration. Our calculation results shown in Fig.11 revealed that the FIMCs  
444 became unstable when the Si concentration reach their solubility. Therefore, the Si  
445 concentration of FIMCs at the interface that phase transformed to the other types of FIMCs can  
446 be considered as their maximum solubility. For example, during the multi-step phase  
447 transformation from  $\theta$  to  $\alpha'$ ,  $\alpha'$  to  $\beta$ , and  $\beta$  to  $\delta$ , the solubility of Si in these FIMCs can be

448 considered as 2.7at.% of  $\theta$ , 10.4at.% of  $\alpha'$ , and 16.9at.% of  $\beta$ , respectively. The solubility of Si  
449 in different FIMCs can change with the experimental conditions such as temperature at which  
450 the phases transformation can occur. Further investigation is required to understand the  
451 relationship between the alloy composition, concentration of Si in the FIMC and phase  
452 stability.

453 Recent research [21] showed that the phase transformation among different types of FIMCs  
454 are diffusion controlled. Therefore, which types of FIMCs form through phase transformation  
455 from  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> depends on many factors such as alloy composition, cooling rate. Additionally,  
456 a few pairs of ORs between  $\theta$  and the other FIMCs,  $\alpha'$ ,  $\beta$  were identified. These ORs contains  
457 some crystallographic information of the structure transition between these FIMCs. Further  
458 investigation is working.

459 The calculation results also revealed that the chemical composition of  $\beta$ -phase is Al<sub>4.5</sub>FeSi,  
460 which is similar as the experimental observation [38]. However, the Si distribution is different  
461 from that reported previously. The experimental model suggested a homogeneous distribution  
462 of Si at the Al sites, whereas the first-principles calculations predicted that the Si atoms are at  
463 either the Al1 or the Al6 site. Additionally, the DFT simulation also showed a high  
464 configurational entropy contribution for increased Si solution in the  $\beta$ -phase. This indicates  
465 that at high temperature (>700K), the  $\beta$ -phase may contain more Si than the configuration of  
466 stable structure at ambient conditions [41].

#### 467 4.3 Effects of thermodynamic on phase transformation of $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>

468 Naturally, the chemical composition has an impact on the formation of  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> phase in Al  
469 alloys. The concentration of Si in the  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> phase depending on the chemical composition  
470 in the Al alloys and casting conditions. The details of phase transformation mechanisms  
471 between different types of FIMCs have been reported in our recent contributions [21]. It is  
472 reported that these phase transformations between various FIMCs are diffusion-controlled. The  
473 phase transformation of FIMCs from  $\theta$ -(Al,Si)<sub>13</sub>Fe<sub>4</sub> with a low Si concentration to other  
474 FIMCs with a higher Si content (such as  $\alpha'$ -Al<sub>8</sub>Fe<sub>2</sub>Si,  $\alpha$ -Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub>,  $\beta$ -Al<sub>5</sub>FeSi) depends  
475 on the Fe and Si diffusion at high temperature and long holding times. The TEM-EDX results  
476 from various FIMCs observed in this study, Table 2, showed that the Fe content decreased, and  
477 the Si content increased in each of the FIMC as the phase transformation sequence progressed  
478 from  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub> to  $\alpha$ -Al<sub>15</sub>(Fe, Mn)<sub>3</sub>Si<sub>2</sub>,  $\alpha'$ -Al<sub>8</sub>Fe<sub>2</sub>Si and  $\beta$ -Al<sub>5</sub>FeSi. The experimentally  
479 measured Si concentration in Table 2 revealed a sequence among different types of FIMCs as:  
480  $C_{\theta}^{Si} < C_{\alpha}^{Si} < C_{\alpha'}^{Si} < C_{\beta}^{Si}$ . The experimental results in this study showed a complicated phase selection  
481 and the variable following phase transformations depending on the alloy composition, which  
482 illustrated that in high Si containing Al alloys, at certain casting conditions, especially at slow  
483 solidification process. The FIMCs such as  $\alpha'$ -Al<sub>8</sub>Fe<sub>2</sub>Si,  $\alpha$ -Al<sub>15</sub>(Fe,Mn)<sub>3</sub>Si<sub>2</sub>,  $\beta$ -Al<sub>5</sub>FeSi with  
484 higher Si content is more stable than those with a lower Si content FIMCs such as  $\theta$ -Al<sub>13</sub>Fe<sub>4</sub>,  
485 indicating the possible thermodynamic stability of these phases at the investigated alloys.

486 However, the final microstructure selection was resulted from the effects of multiple factors,  
487 such as thermodynamic, nucleation difficulty, etc.

488

## 489 5. Conclusions

490

491 (1) The experimental measured lattice parameters ( $a$ ,  $b$ ,  $c$ ) of  $\theta$ - $\text{Al}_{13}\text{Fe}_4$  decreases with the  
492 increasing Si concentration in  $\theta$ - $\text{Al}_{13}\text{Fe}_4$  particles formed in different Al alloys. However,  
493 the maximum Si concentration doped in  $\theta$ - $\text{Al}_{13}\text{Fe}_4$  measured from experimental results is  
494 lower than that of calculation.

495 (2) Multi types of phase transformation between  $\theta$ - $\text{Al}_{13}\text{Fe}_4$  and the other types of FIMCs were  
496 observed in Al-Fe-Si alloys.

497 1)  $\text{L} + \theta\text{-Al}_{13}\text{Fe}_4 \rightarrow \alpha'\text{-Al}_8\text{Fe}_2\text{Si} + \alpha\text{-Al}$

498 2)  $\text{L} + \theta\text{-Al}_{13}\text{Fe}_4 \rightarrow \beta\text{-Al}_5\text{FeSi} + \alpha\text{-Al}$

499 3)  $\text{L} + \text{AlFe} \rightarrow \theta\text{-Al}_{13}\text{Fe}_4 + \alpha\text{-Al}$

500 4)  $\text{L} + \theta\text{-Al}_{13}\text{Fe}_4 \rightarrow \alpha\text{-Al}_{15}(\text{Fe}, \text{Mn})_3\text{Si}_2 + \alpha\text{-Al}$

501 (3) The orientation relationships between  $\text{Al}_{13}\text{Fe}_4$  and the other types of FIMCs were well-  
502 defined.

503 A.  $(10\bar{3})\alpha'\text{-Al}_8\text{Fe}_2\text{Si} // (11\bar{1})\theta\text{-Al}_{13}\text{Fe}_4$ , and  $[\bar{3}2\bar{1}]\alpha'\text{-Al}_8\text{Fe}_2\text{Si} // [\bar{1}\bar{3}\bar{4}]\theta\text{-Al}_{13}\text{Fe}_4$

504 B.  $(020)\beta\text{-Al}_5\text{FeSi} // (010)\theta\text{-Al}_{13}\text{Fe}_4$ , and  $[100]\beta\text{-Al}_5\text{FeSi} // [001]\theta\text{-Al}_{13}\text{Fe}_4$

505 C.  $(1\bar{1}\bar{1})\text{AlFe} // (001)\theta\text{-Al}_{13}\text{Fe}_4$ , and  $[112]\text{AlFe} // [100]\theta\text{-Al}_{13}\text{Fe}_4$

506 D.  $(\bar{2}01)\theta\text{-Al}_{13}\text{Fe}_4 // 2.3^\circ (0\bar{1}1)\alpha\text{-Al}_{15}(\text{Fe}, \text{Mn})_3\text{Si}_2$ , and  $[010]\theta\text{-Al}_{13}\text{Fe}_4 // [100]\alpha\text{-}$   
507  $\text{Al}_{15}(\text{Fe}, \text{Mn})_3\text{Si}_2$

508 (4) The composition of different FIMCs solidified at different conditions are variable, which  
509 caused the corresponding lattice parameters changes. The Si concentration in different  
510 FIMCs has a sequence as:  $C_\theta^{\text{Si}} < C_\alpha^{\text{Si}} < C_{\alpha'}^{\text{Si}} < C_\beta^{\text{Si}}$ .

511

## 512 Acknowledgement

513 The Engineering and Physical Sciences Research Council (EPSRC) is gratefully acknowledged  
514 for providing financial support under Grant EP/N007638/1. Dr Lorna Auguilano, and Professor  
515 Chris Frampton is gratefully acknowledged for supporting in single crystal experiments.

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