

Original Article

The effect of solution temperature on the precipitates evolution and aging hardening response of Al-15%Mg₂Si(-1%Cu) alloys



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ABSTRACT

The effect of solution temperature on the aging hardening behavior of Al-15%Mg₂Si(-1%Cu) alloys was studied by characterizing the precipitation behaviors of nano-precipitates. After the solution temperature rises from 520 °C to 550 °C, more solute atoms are available for precipitation, and the formation activation energies of precipitates (β " and S) decrease. So the formation of β "/ β ' in Al-15%Mg₂Si alloy and S in Al-15%Mg₂Si-1%Cu alloy is accelerated at a solution temperature of 550 °C, which enhances the hardness and ultimate tensile strength (UTS) of the two alloys.

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1. Introduction

In recent years, the Al-Mg₂Si alloy, reinforced by intermetallic compound Mg₂Si, has an attractive application prospect in automotive manufacturing owing to the advantage of Mg₂Si (high melting point and hardness, low density and thermal expansion coefficient) [1–7]. Moreover, besides Mg₂Si, the intermetallics such as θ phase (Al₂Cu) and Q phase (Al₅Cu₂Mg₈. Si₆) are also important for strength and ductility of the Al-Mg₂Si alloys after alloyed with Cu [8–10]. These hard

intermetallics can not only directly strengthen the alloy, but also dissolve into the Al matrix to provide necessary solute atoms for the precipitation of nano-precipitates during aging heat treatment, thus further improving the strength of the Al-Mg₂Si alloys [9,11].

The $\beta^{\prime\prime}$ (Mg₅Si₆, a = 1.516 nm, b = 0.405 nm and c = 0.674 nm), β^{\prime} (Mg₉Si₅, a = 0.715 nm and c = 1.215 nm) and S (Al₂CuMg, a = 0.4 nm, b = 0.92 nm and c = 0.71 nm) phase (formed after low Cu alloying) are typical nano-precipitates in Al-Mg₂Si (-Cu) alloy system [9,11–13]. These precipitates are

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Table 1 — Actual chemical compositions of two alloys (wt.%).				
Alloys	Al	Mg	Si	Cu
Al-15%Mg ₂ Si	Bal.	9.7	5.5	_
Al-15%Mg ₂ Si-1%Cu	Bal.	9.8	5.4	1.2
Note: Chamical compositions were detected by industively coupled				

Note: Chemical compositions were detected by inductively coupled plasma mass spectrometry.

assembled by the solute atoms after the solution treatment and are essential for the mechanical properties of the alloys.

However, during solution treatment, the alloys are exposed to high temperatures [14]. The low solution temperature could result in the incomplete dissolution of intermetallic compounds and a decreased level of homogenization. But an excessive solution temperature leads to partial melting of eutectic microstructure. Hence, the solution temperature is an important factor for the strengthening effect. The increased solution temperatures are needed to ensure the solute supersaturation degree without destroying the properties of the alloys [9,15–20].

Therefore, the aging hardening behaviors of as-cast Al- Mg_2Si (1%Cu) alloys with different solution temperatures were studied in the current work by characterizing the formation and precipitation kinetics of nano-precipitates. And it can provide a reference to optimize the heat treatment process of the Al- Mg_2Si (1%Cu) alloys at different solution temperatures.

2. Materials and methods

The preparation of Al-15%Mg₂Si(-1%Cu) alloys (wt.% in this work) was mentioned in our previous paper [9]. The actual chemical compositions of the alloys were listed in Table 1.

The specimens (Φ 8 mm \times 6 mm) were solution treated for 6 h at 520 or 550 °C, then quenched in cold water and aged in an oil bath at 200 °C for varying periods of time. A macro Vickers hardness tester (ASTM E92-82) with a 200 gf load and a dwell time of 5 s was used to measure hardness value of the specimens with different aging time (the average of ten individual measurements).

The microstructures of as-cast and solution alloys were observed by field emission scanning electron microscope (Hitachi Model No. S4800). The precipitation kinetics of two alloys after quenching were analyzed using differential scanning calorimetry (DSC, Mettler Toledo) from 100 °C to 400 °C with a heating rate of 10 K/min in flowing high purity argon gas.

Twin-jet electropolishing 3 mm discs in a 30% nitric acid 70% methanol solution at -30 °C were used to prepare thin foils for transmission electron microscopy (TEM) and highresolution TEM (HRTEM). TEM (operated at 120 kV) and HRTEM observations (operated at 200 kV) of nano-precipitates were obtained using an FEI Tecnai F30 microscope. Image Pro plus was used to measure the volume fraction of Mg₂Si phase and the average size of precipitates. Mg₂Si and Al matrix are distinguished by different gray values. The volume fraction of Mg₂Si phase is represented by the average area fraction of Mg₂Si phase (measured more than 10 SEM pictures). The size and number of precipitates can be measured and counted by importing more than ten DM3 files corresponding to the TEM and HRTEM images. The measurement data of more than 50 precipitates are collected to reduce the measurement error. All line charts and histograms in the discussion section were plotted with Origin 8 software.

Tensile tests with a crosshead speed of 0.11 mm/min were performed on three samples (each data value) by using an INSTRON 1342/H1314 at 25 $^\circ$ C.

3. Results and discussion

3.1. Microstructure characterization

Fig. 1 shows the morphology of Al-15%Mg₂Si(-1%Cu) alloys with or without solution treatment. Fig. 1a (d), b (e) and c (f) are corresponding to as-cast, solution treated at 520 °C and 550 °C conditions, respectively. The primary Mg₂Si phases and binary eutectic microstructure exist in Al-15%Mg₂Si alloy



Fig. 1 – The morphology of (a), (b) and (c) Al-15%Mg₂Si and (d), (e) and (f) Al-15%Mg₂Si-1%Cu alloys at different conditions.



Fig. 2 – The volume fraction of Mg_2Si under different heat treatment conditions.

(Fig. 1a), and Cu-rich phases (θ -Al₂Cu and Q-Al₅Cu₂Mg₈Si₆) are formed after the addition of 1%Cu (Fig. 1d) [9]. After the solution treatment at 520 °C or 550 °C for 6 h, sharp corners of primary Mg₂Si and Cu-rich phases dissolve into the matrix, and eutectic Mg₂Si phases are broken into rod-like or spherical morphology, which is reported in the previous studies [21,22].

The volume fraction of Mg₂Si (primary and eutectic) under different heat treatment conditions is presented in Fig. 2. The reduced volume fraction of Mg₂Si with increasing solution temperature indicates that more Mg₂Si phases dissolve into the matrix. The elevated solution temperature causes the increased content of Mg, Si and Cu atoms in the matrix, which can significantly affect the aging process of the alloys.

3.2. Aging hardening behavior

After solution-aging treatment, the hardness curves with different solution temperatures are provided in Fig. 3 and corresponding peak hardness values for both alloys are summarized in Table 2. With the solution temperature increasing from 520 °C to 550 °C, the peak hardness increases from 85 HV to 95 HV for Al-15%Mg₂Si alloy and from 121 HV to 144 HV for Al-15%Mg₂Si-1%Cu alloy.

3.3. Precipitates evolution of $Al-15\%Mg_2Si(-1\%Cu)$ alloys

TEM and HRTEM images of the peak-aging condition are shown in Figs. 4 and 5, in order to better understand the agehardening behavior of the alloys with different solution temperatures.

Fig. 4a exhibits that the β " and β' phases are formed in Al-15%Mg₂Si alloy under the peak aging condition (solution at 520 °C followed by aging at 200 °C), and the HRTEM images of β " and β' phases are shown in Fig. 4b and c. For the Al-15% Mg₂Si alloy solution treated at 550 °C, more fine β " and β' phases are formed (Fig. 4d). The average diameters of β " (decreasing from 3.6 nm to 2.6 nm) and β' (decreasing from 8.4 nm to 5.8 nm) phases reduce significantly, compared with that solution treated at 520 °C (Fig. 6a).

After adding 1%Cu, the type, size and quantity of precipitates changed apparently (Fig. 5). The change of precipitates type (solution at 520 °C) in Al-15%Mg₂Si-1%Cu alloy was reported in our previous work [9]. The alloy exhibits lathlike S precipitates in peak-aging condition (solution at 520 °C) instead of β "/ β ' phases (Fig. 5a), owing to the stronger binding energy of Cu and Mg atoms. Fig. 5b shows an HRTEM image of S phase and its FFT spectrum. Because the structure of the S' phase was believed to be crystallographically similar to that of equilibrium S precipitate, no distinction was made in this work.

Moreover, as shown in Fig. 5a and c, the Al-15%Mg₂Si-1%Cu alloy solution-treated at 550 °C produced more S phases than that solution-treated at 520 °C. With the solution temperature increasing to 550 °C (Fig. 5c and d), the average diameter of S phase decreases from 4.3 nm to 3.5 nm, and the number density increases from 5.85×10^{21} m⁻³ to 7.45×10^{21} m⁻³ (Fig. 6b). The formation of more S phase is responsible for the advanced peak time and higher peak hardness (Fig. 3b).

3.4. The calculated formation activation energy of precipitates

Fig. 7 displays DSC curves obtained at a heating rate of 10 K/ min of the two alloys solution treated at 520 °C and 550 °C. For Al-15%Mg₂Si alloy, the exothermic peak A between 230 °C and 280 °C, reported as the precipitation of β " phase [23,24]. For Al-



Fig. 3 – Hardness curves of (a) Al-15%Mg₂Si and (b) Al-15%Mg₂Si-1%Cu alloys aging at 200 °C with different solution temperatures.

Table 2 – The peak hardness for both alloys with different solution temperatures.					
Alloys	Peak hardr	Peak hardness (HV)			
	520 °C	550 °C			
Al-15%Mg ₂ Si	85	121			
Al-15%Mg ₂ Si-1%Cu	95	144			
Note: Peak hardness value	es are obtained from ha	rdness curves			

(Fig. 3).

15%Mg₂Si-1%Cu alloy, exothermic peak B between 220 °C and 290 °C was considered as the formation of S phase [15,25–27]. It is essential to understand transformation kinetics of two alloys by evaluating the activation energy of precipitation reaction. According to the Johnson-Mehl-Avrami (JMA) model [28–30], the formation activation energy of β " and S phase can be determined as:

$$Y = 1 - \exp(-kt^{n}), \qquad (1)$$

$$k = k_0 \exp(-Q / RT)$$
, (2)

where k is the temperature correlation coefficient. k_0 and R are constants. n (a value of 1.5 used for aluminum [28]) is the nucleation growth coefficient. Q is the precipitation activation energy. Y (obtained from DSC curves) is the volume fraction of precipitates at T [28,31].

By derivation of Eq. (1) to t, the transformation rate of volume fraction is shown as:

$$dY / dt = k^{1/n} f(Y) , (3)$$

where f(Y) is a function of Y.

$$f(Y) = n(1 - Y)(-\ln(1 - Y))^{n-1/n}.$$
Based on Eqs. (2)-(4). (4)

$$ln[(dY / dT)(\Phi / f(Y))] = (1 / n)lnk_0 - Q / (nRT),$$
(5)

where Φ is heating rate (10 K/min). The variations of $\ln[(dY/dT)(\Phi/f(Y))]$ with 1/T are plotted at different solution temperatures to estimate the formation activation energy of precipitates. Based on the slop (Q/nR) of the fitted straight lines (found by least-square fitting in Fig. 8), the Q of precipitates can be calculated.

The formation activation energies of β " (decreasing from 102.5 kJ/mol to 98.4 kJ/mol) and S phases (decreasing from 81.7 kJ/mol to 76.1 kJ/mol) decrease with solution temperature increasing. The reduced formation activation energies of precipitates reflect the accelerated aging kinetics in two alloys. Nano-precipitates have high precipitation potential at elevated solution temperatures due to the increased supersaturation degree and decreased thermal diffusion activation energies of solute atoms [15], which promotes forming more precipitates with finer size (β ", β ' and S phases), as shown in Fig. 6.

In addition, mismatch strains are formed after quenching from the high temperature due to the large thermal expansion coefficient difference between the Al matrix (~26.6 \times 10⁻⁶/°C)



Fig. 4 – Bright-field TEM images with corresponding selected-area electron diffraction (SAED) patterns recorded near $<100>_{Al}$ and HRTEM images with fast Fourier transformation (FFT) spectrum of β '' and β ' phase in peak-aged Al-15%Mg₂Si alloy: at a solution temperature of (a) (b) (c) 520 °C and (d) (e) (f) 550 °C.



Fig. 5 – Bright-field TEM images with SAED patterns recorded near $<100>_{Al}$ and corresponding HRTEM image with FFT spectrum of S phase in peak-aged Al-15%Mg₂Si-1%Cu alloy: at a solution temperature of (a) (b) 520 °C and (c) (d) 550 °C.

and Mg₂Si phase (~7.5 × 10^{-6/°}C). These mismatch strains can promote the formation of dislocations and provide heterogeneous nucleation sites for nano-precipitates [32–34], as shown in Fig. 9. Moreover, the alloy with a higher solution temperature promotes more dislocations around Mg₂Si after quenching (Fig. 9b). This high-density dislocation is also the important reason for the finer precipitates and decreased formation activation energy.

3.5. Mechanical properties

Fig. 10 presents the ultimate tensile strength (UTS) of peakaging alloys with different solution temperatures. For two alloys, the strength of peak aging alloys increases with solution temperature increasing. Firstly, the modified morphology and reduced sharp corners (nucleation sites for cracks) of Mg₂Si after solution treatment lead to the improved strength of the



Fig. 6 – Average diameter and number density of (a) β''/β' and (b) S phase in Al-15%Mg₂Si(-1%Cu) alloys under peak-aging conditions.



Fig. 7 – DSC curves of solution (a) Al-15%Mg₂Si and (b) Al-15%Mg₂Si-1%Cu alloys quenched at 520 °C and 550 °C.



Fig. 8 – Fitting lines of calculated activation energies of (a) β '' phase in Al-15%Mg₂Si alloy and (b) S phase Al-15%Mg₂Si-1%Cu alloy.

alloy (Fig. 1). Secondly, mismatch strains and high-density dislocation around the Mg_2Si (large linear expansion coefficient difference with Al matrix) after quenching also promote the strengthening of the alloy (Fig. 9). Most importantly, for aging hardening alloy, the nano-precipitates formed during aging can hinder the dislocation movement and provide strengthening for the alloy [15,23,25]. The dispersed

precipitates (β''/β' and S phases in Figs. 4 and 5) uniformly distributed can significantly promote the age-hardening process and strengthening effect of the alloys. Therefore, as solution treatment temperature rises from 520 °C to 550 °C, the UTS is improved from 186 MPa to 249 MPa for Al-15%Mg₂Si alloy and from 283 MPa to 334 MPa for Al-15%Mg₂Si-1%Cu alloy.







Fig. 10 - Ultimate tensile strength of peak aging Al-15% $Mg_2Si(-1\%Cu)$ alloys with different solution temperatures at 25 $^\circ\text{C}.$

4. Conclusion

Solution temperature has an obvious effect on precipitates formation and age-hardening behavior of Al-15%Mg₂Si(-1% Cu) alloys. The increased solution temperature (from 520 °C to 550 °C) can reduce the formation activation energies of precipitates (β " and S). As a result, the formation of β "/ β ' phases in Al-15%Mg₂Si and S phase in Al-15%Mg₂Si-1%Cu is promoted. The fine size and high number density of β "/ β ' or S phase are mainly responsible for the improved hardness and ultimate tensile strength of two alloys at a solution temperature of 550 °C.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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