

1 Article

# 2 **Deep Learning Methods for Fault Detection and** 3 **Classification in MMC-HVDC systems**

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15 **Abstract:** As there is not much literature about deep learning-based fault diagnosis for modular  
16 multilevel converters (MMCs) and comparison among deep learning methods used in fault  
17 diagnosis for MMC, two deep learning methods, namely, Convolutional Neural Networks (CNN)  
18 and Auto Encoder based Deep Neural networks (AE-based DNN) as well as stand-alone Softmax  
19 classifier are explored for the detection and classification of faults of MMC-based high voltage direct  
20 current converter (MMC-HVDC). Only AC-side three-phase current and the upper and lower  
21 bridges' currents of the MMCs are used directly by our proposed approaches without any explicit  
22 feature extraction or feature subset selection. The two-terminal MMC-HVDC system is established  
23 in PSCAD/EMTDC to verify and compare our methods. The simulation results indicate CNN, AE-  
24 based DNN, and Softmax classifier can detect and classify faults with high detection accuracy and  
25 classification accuracy. Compared with CNN and AE-based DNN, the Softmax classifier behaved  
26 better in detection and classification accuracy as well as testing speed. The detection accuracy of  
27 AE-based DNN is a little better than CNN, while CNN needs less training time than the AE-based  
28 DNN and Softmax classifier.

29 **Keywords:** MMC-HVDC; fault detection; fault classification; CNN; AE-based DNN; Softmax  
30 classifier; classification accuracy; speed  
31

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## 32 **1. Introduction**

33 With the increasing application of modular multilevel converter-based high-voltage direct  
34 current (MMC-HVDC) systems, the reliability of MMC is of major importance in ensuring power  
35 systems are safe and reliable. Topology configuration redundant strategies of fault-tolerant systems  
36 are useful methods to improve reliability which can be achieved by using more semiconductor  
37 devices as switches in an SM [1] or integrating redundant SMs into the arm submodule [2]. But, it is  
38 well to remember that, fault detection is a precondition for fault-tolerant operation which is needed  
39 to be as fast and accurate as possible to ensure converter continuous service. Therefore, Fault  
40 detection and classification are one of challenging tasks in MMC-HVDC systems to improve its  
41 reliability and thus reducing potential dangers in the power systems because there are a large number  
42 of power electronic sub-modules (SMs) in the MMC circuit and each SM is a potential failure point  
43 [3,4].

44 The research of fault detection and classification in MMC-HVDC systems applications can be  
45 broadly categorized into three basic approaches that are mechanism-based, signal processing-based,  
46 and artificial intelligence-based [5]. All the mechanism-based methods need many sensors  
47 monitoring the inner characteristics (circulating current, arm currents, capacitor voltages, etc.). Signal  
48 processing-based methods employ output characteristics rather than inner characteristics to detect a  
49 fault. Signal processing-based methods have been deemed reliable and fast by researchers [6-9] with  
50 the advancement of signal processing methods in recent years. But both of them need suitable  
51 methods to obtain expected inner characteristics or threshold of certain derived features, such as zero-  
52 crossing current slope or harmonic content which degrades the robustness of fault detection and  
53 classification. The artificial intelligent methods do not need any mathematical models of MMC  
54 functionality and any threshold setting, yet, they can improve the accuracy of fault diagnosis due to  
55 their advantage of nonlinear representations.

56 A neural network as the most basic artificial intelligence method is used by many researchers.  
57 Khomfoi and Tolbert [10] propose a fault diagnosis and reconfiguration technique for a cascaded H-  
58 bridge multilevel inverter drive using principal component analysis (PCA) and neural network (NN).  
59 In this method, the genetic algorithm is used to select valuable principal components. Simulation and  
60 experimental results showed that the proposed method is satisfactory to detect fault type, fault  
61 location, and reconfiguration. Wang et al. [11] propose an artificial NN-based robust DC fault  
62 protection algorithm for MMC high voltage direct current grid. In which, the discrete wavelet  
63 transform is used as an extractor of distinctive features at the input of the ANN. Furqan Asghar et al.  
64 [12] present NN-based fault detection and diagnosis system for three-phase inverter using several  
65 features extracted from the Clarke transformed output as an input of NNs. Merlin et al. [13] design  
66 thirteen artificial NNs for the voltage-source converter-HVDC systems to detect a fault condition in  
67 the whole HVDC system based only on voltage waveforms measured at the rectifier substation.

68 Although the NN based methods achieved some improvements in the diagnosis of failed  
69 converters and identification of defective switches [14,15], the prerequisite for the successful  
70 application of NNs is to have enough training data and long training time. Multi-class relevance  
71 vector machines (RVM) and support vector machine (SVM) replace a neural network to classify and  
72 locate the faults because of their rapid training speed and strongly regularized characteristic [5].  
73 Wang et al. [16] use a PCA and multiclass RVM approach for cascaded H-bridge multilevel inverter  
74 system fault diagnosis. Wang et al. [17] propose and analyze a fault-diagnosis technique to identify  
75 shorted switches based on features generated through the wavelet transform of the converter output  
76 and subsequent classification in SVMs. The multi-class SVM is trained with multiple recordings of  
77 the output of each fault condition as well as the converter under normal operation. Jiao et al. [18]  
78 used the three-phase AC output side voltage of MMC as the fault characteristic signal, combined with  
79 PCA data preprocessing and firefly algorithm optimized SVM (FA-SVM) for MMC fault diagnosis.  
80 Zhang and Wang [19] proposes a least-squares-based  $\epsilon$ -support vector regression scheme, which  
81 captures fault features via the Hilbert–Huang transform. Fault features are used as the inputs of  $\epsilon$ -  
82 support vector regression to obtain fault distance. Then, the least-squares method is utilized to  
83 optimize the parameters of the model so that it can meet the demand on fault location for MMC-  
84 MTDC transmission lines.

85 To build the aforementioned artificial intelligence machine, feature extraction techniques such  
86 as Fourier analysis [20,21], wavelet transform [14,15], Clarke transform [12] or feature subset selection  
87 techniques such as Principal component analysis (PCA) [10,22] and multidimensional scaling (MDS)  
88 plays an important role. Sometimes to select suitable sub-features, the Genetic Algorithm (GA)  
89 [10,22,23] or particle swarm optimization (PSO) [24] are employed. It is well known that feature  
90 extraction has always been a bottleneck in the field of fault diagnosis. Moreover, the feature extraction  
91 and all the following post-operation increase the computation burden.

92 Deep learning methods have been explored to learn the features from the data which can be  
93 generalized to different cases. Zhu et al. [25] proposed Convolutional Neural Networks (CNN) for  
94 fault classification and fault location in AC transmission lines with back-to-back MMC-HVDC, in  
95 which, two convolutional layers were used to extract the complex features of the voltage and the

96 current signals of only one terminal of transmission lines. Serkan Kiranyaz et al. [26] use 1-D CNN to  
97 detect and localize the switch open-circuit fault using four cell capacitor voltage, circulating current  
98 and load current signals. This method can achieve a detection probability of 0.989 and an average  
99 identification probability of 0.997 in less than 100ms. Qu et al. [27] propose CNN for MMC fault  
100 detection using each capacitor's voltage signal. Wang et al. [28] propose CNN for DC fault detection  
101 and classification using wavelet logarithmic energy entropy of transient current signal. In the past  
102 our research group proposed some related methods of NNs [29~31], AE-based DNN [32] and softmax  
103 classifier [33] for bearing fault detection and classification, but not for MMC-HVDC. Moreover, to the  
104 best of our knowledge, use of deep learning methods for MMC fault detection and classification have  
105 been very limited and there is no comparison of two deep learning methods. Furthermore, Afore-  
106 mentioned CNNs have achieved success, but their advantages have not been explored completely,  
107 e.g., the ability of feature extraction, the speed of processing, and its stability. In summary, up to now,  
108 there is still much room to further improve the performance of the open-circuit fault diagnosis of  
109 MMCs.

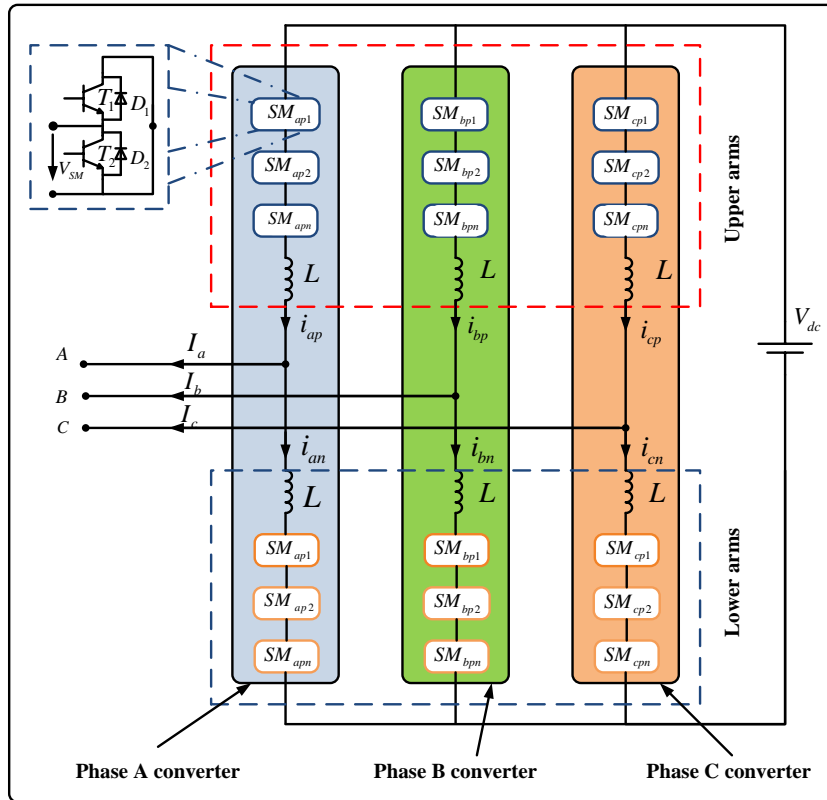
110 To shorten such a gap and achieve high fault classification accuracy with fewer sensors and  
111 reduced computational time for fault diagnosis of MMCs, we propose two deep learning methods  
112 and one stand-alone Softmax Classifier for MMCs faults detection and classification using raw data  
113 collected from current sensors to recognize automatically the open-circuit failures of IGBT in MMCs.  
114 The contributions of this paper are as follows:

- 115 a. Only current sensors data are used for fault diagnosis and achieved high accuracy of fault  
116 detection and classification.
- 117 b. Multichannel current signals are used instead of a single channel to improve reliability  
118 because the sensors may also cause some faults.
- 119 c. Excellent accuracy on fault detection and identification without data preprocessing or post-  
120 operation;
- 121 d. Two deep learning methods and a stand-alone Softmax Classifier are used with raw data  
122 collected by current sensors to achieve improved classification accuracy and reduced computation  
123 time.
- 124 e. Performance comparison of CNN, AE-based DNN, and Softmax Classifier in terms of fault  
125 diagnosis accuracy, stability and speed for MMC-HVDC fault diagnosis.

126 This paper is organized as follows. Section 2 introduces the topology and data acquisition from  
127 MMC. Section 3 proposes the framework of this paper and the design of CNN, AE-based DNN, and  
128 Softmax Classifier. The feasibility and performance of the proposed approaches are evaluated in  
129 Section 4. Section 5 compares the three deep learning methods. Conclusions are drawn in section 6.

## 130 2. MMC topology and data acquisition

131 The data for this study was simulated from a two-terminal model of the MMC-HVDC  
132 transmission power system using PSCAD/EMTDC [34]. It solves the differential equations of the  
133 entire power system and its controls. Figure 1 shows that each phase of the three-phase MMC consists  
134 of two arms (upper and lower) that are connected to two inductors L. Each arm contains a series of  
135 SMs, and each SM involves two IGBTs (i.e.,  $T_1$  and  $T_2$ ), two diodes D, and a DC storage capacitor.

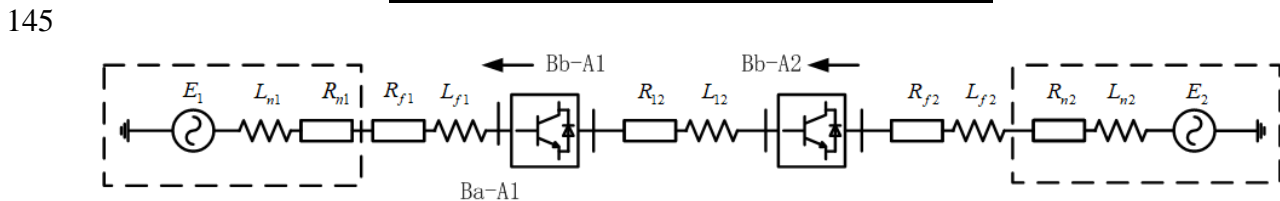


136 **Figure 1.** Structure of a three-phase MMC with half-bridge submodules

137 In our simulation (Table 1), we recorded 9 channels of data for normal and 6 different locations of IGBT break-circuit fault manually for each bridge (namely A-phase lower SMs, A-phase upper SMs, B-phase lower SMs, B-phase upper SMs, C-phase lower SMs, and C-phase upper SMs). There are 100 cases of IGBT break-circuit fault that happened at different IGBTs of the six bridges at different times. The power system is depicted in Figure 2. The type of SMs is half-bridge and the direction of the flow is shown as the arrow above. Ba-A1 and Ba-A2 are two AC bus bars. Bb-A1 and Bb-A2 are two DC bus bars. E1 is an equivalent voltage source for an AC network. E2 is a wind farm.

144 **Table 1.** Parameters of MMC.

Parameters	Value
number of SMs per arm	9
SM capacitor	1000uF
arm inductance	50mH
AC frequency	50Hz



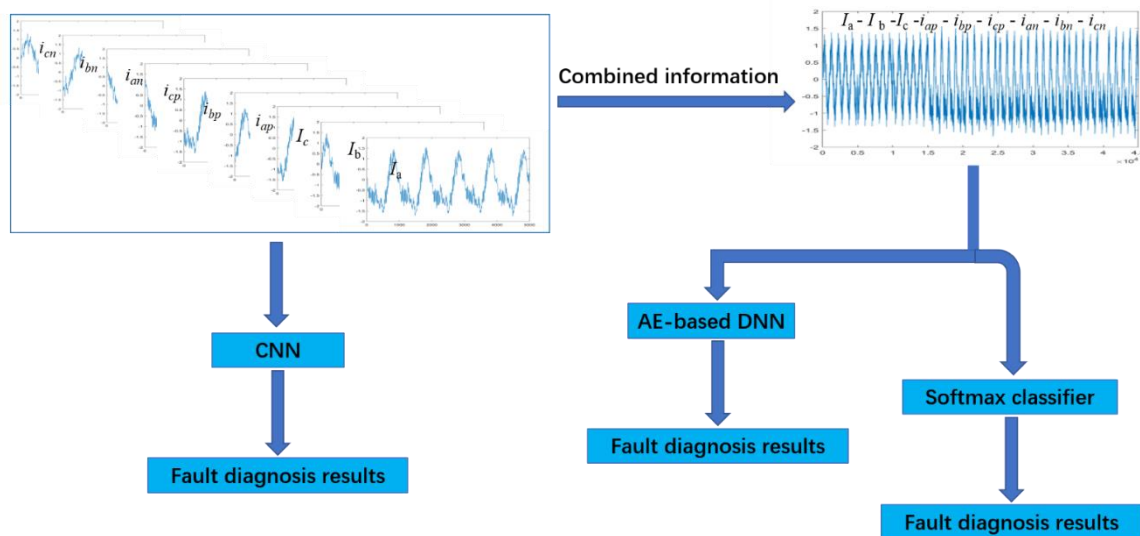
146 **Figure 2.** Structure of the HVDC

147 The whole time period used is 0.1s while the time for the IGBT open circuit fault duration is  
 148 varied from 0.03s to 0.07s. The simulation time step is 2μs and the sampling frequency is 20μs. The  
 149 acquired data channels for fault diagnosis are AC-side three-phase current ( $I_a, I_b, I_c$ ) and three-phase  
 150 circulation current ( $I_{diffa}, I_{diffb}, I_{diffc}$ ).

### 151 3. The framework of fault classification and design of deep learning methods

#### 152 3.1. The framework for fault detection and classification

153 This paper proposes three methods to complete both the fault detection and classification task  
 154 for MMC, as shown in Figure 3, which are CNN, AE-based DNN, and a stand-alone Softmax  
 155 classifier. CNN processes the raw sensors data which are nine current signals ( $I_a, I_b, I_c, i_{ap}, i_{bp}, i_{cp}, i_{an}, i_{bn},$   
 156 and  $i_{cn}$ ) and obtains the fault diagnosis results. AE-based DNN and Softmax process the combined  
 157 information which is concatenated the measurements of these nine parameters to form a vector of  
 158 samples that represent the current health condition of the MMCs, then obtain the fault diagnosis  
 159 results.



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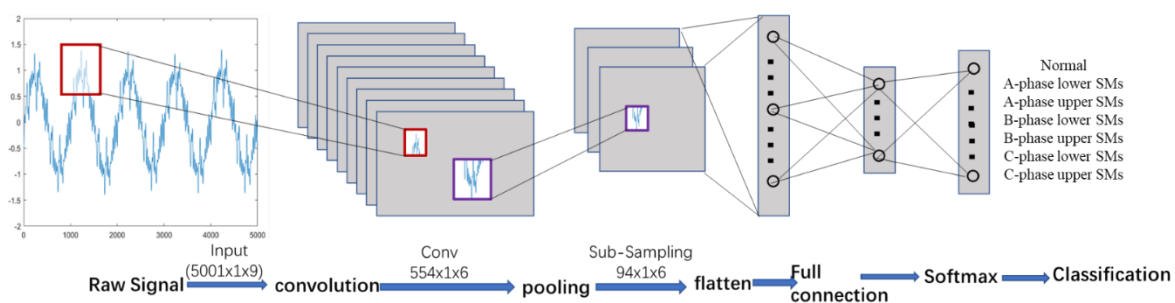
161

**Figure 3.** Framework for fault detection and classification for MMC

#### 162 3.2. Design of CNN

163 Convolutional neural networks (CNNs) are widely used tools for deep learning which is  
 164 different from the traditional feed-forward ANN because of its three architectural properties of the  
 165 visual cortex cell: local receptive regions, shared weights, and subsampling. The crucial advantage of  
 166 CNNs is that both feature extraction and classification operations are fused into a single Machine  
 167 learning body to be jointly optimized to maximize the classification performances [26].

168 CNN consists of multiple layers such as figure 4 which are the input layer, convolutional layer,  
 169 activation layer, pooling layer, full connect layer, softmax layer, and a classification layer. Among  
 170 these layers, there are two basic layers in CNN which are the convolutional layer and the pooling  
 171 layer. Convolution operation implements the first two properties that are local receptive regions and  
 172 shared weights. The pooling operation implements the subsampling property [35].



173

174

**Figure 4.** Architecture of the signal-level CNN classifier

175 A convolutional layer consists of neurons that connect to small regions of the input and operate  
 176 the convolution computation. The output feature map of the convolutional layer can be written as:

$$F_j = \varphi(\sum_{i=1}^N W_{i,j} \otimes I_i + b_j), \quad (1)$$

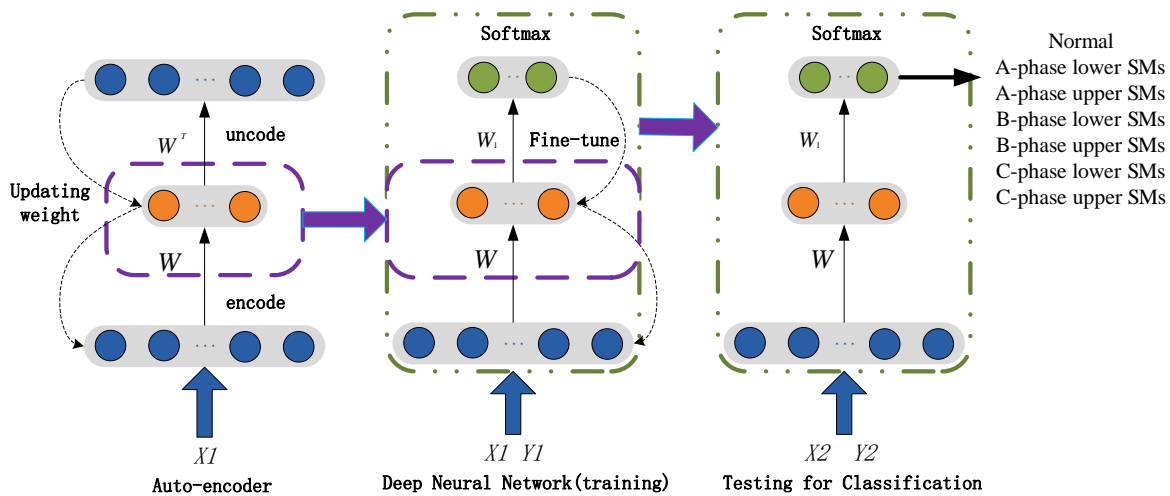
177 For the  $j$ th filter, the output is a new feature map  $F_j$ , Where  $W_{i,j}$  and  $b_j$  denote the  $j$ th filter kernel  
 178 and bias, respectively.  $I_i$  is the input matrix of the  $i$ th channel,  $\otimes$  represents the convolutional  
 179 operation, and  $I_i$  is convoluted with a corresponding filter kernel  $W_{i,j}$ . The sum of all convoluted  
 180 matrices is then obtained and a bias term  $b_j$  is added to each element of the resulting matrix. There  
 181 are many several choices we could make activation function  $\varphi$  be a non-linear. But in this paper, we  
 182 simply use a named leaky rectified linear unit (leaky ReLU). The function of leaky ReLU is given by:

$$\varphi(x) = \begin{cases} x, & x \geq 0 \\ scale * x, & x < 0 \end{cases} \quad (2)$$

183 It is a simple threshold that makes the negative value be zero. Then we can obtain the output feature  
 184 map  $F_j$ .

185 Pooling layers perform down-sampling operations. Pooling methods usually include max-  
 186 pooling and average-pooling. In this paper, the average-pooling function is applied which outputs  
 187 the average values of rectangular regions of its input. In a fully connected layer, neurons between  
 188 two adjacent layers are fully pairwise connected but neurons within the same layer share no  
 189 connections. Then the Softmax function is commonly adopted for classification tasks. The  
 190 introduction of Softmax will be presented in the following subsection 3.4.

### 191 3.3. Design of AE-based DNN



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193

Figure 5. Architecture of the AE-based DNN

194 An AE-based DNN (Deep Neural Network) is constructed by several autoencoders (AEs) stacked  
 195 with each other and a Softmax classifier on the output layer. In this paper, we stacked one AE with a  
 196 Softmax classifier as can be seen in figure 5. The AE needs to be pretrained by Greedy layer-wise  
 197 training algorithm. The simplest form of an AE includes three layers: the input layer, hidden layer,  
 198 and output layer. An AE network consists of an encoder and a decoder. The encoder maps the input  
 199 to a hidden representation and the decoder attempts to map this representation back to the original  
 200 input. given an unlabeled vector sample  $x$ , The encoder network can be explicitly defined as:

$$h = f(w_1x + b_1), \quad (3)$$

201 Similarly, the decoder network can be defined as:

$$\hat{x} = g(w_2x + b_2), \quad (4)$$

202 where  $\hat{x}$  are the approximate reconstruction of the inputs, and  $\theta = \{w, b\}$  are the reconstructing  
 203 parameters, and  $f$  and  $g$  are the activation function of the encoder and decoder, respectively. The  
 204 reconstruction error  $E$  between the inputs  $x$  and output  $\hat{x}$  are defined as:

$$E = \underbrace{\frac{1}{N} \sum_{i=1}^N (x_i - \hat{x}_i)^2}_{\text{mean squared error}} + \lambda * \underbrace{\Omega_{\text{weights}}}_{\text{regularization}} \quad (5)$$

205 Where the first part is the mean square variance used to measure the average discrepancy and  $N$  is  
 206 the number of neurons in the output layer, and the second part is the regularization term used to  
 207 prevent overfitting.  $\lambda$  is the coefficient for the [L<sub>2</sub> regularization term](#).

$$\Omega_{\text{weights}} = \frac{1}{2} \sum_l^L \sum_j^N (w_j^{(l)})^2 \quad (6)$$

208 Where  $L$  is the number of hidden layers. The following subsection introduces the softmax classifier.

### 209 3.4. Introduction of Softmax classifier

210 The Softmax function, also known as softargmax or normalized exponential function, is a  
 211 function that takes as input a vector of  $K$  real numbers and normalizes it into a probability  
 212 distribution consisting of  $K$  probabilities proportional to the exponentials of the input numbers. It is  
 213 calculated as:

$$y_r(x) = P(c_r | x, \theta) = \frac{\exp(a_r(x))}{\sum_{j=1}^k \exp(a_j(x))} \quad (7)$$

214 The loss function can use mean squared error function and the cross-entropy function. In this  
 215 paper, we used the cross-entropy function which is given by:

$$E = - \sum_{i=1}^N \sum_{j=1}^k t_{ij} \ln y_{ij}, \quad (8)$$

216 where  $t_{ij}$  is the indicator that the  $i$ th example belongs to the  $j$ th class,  $y_{ij}$  is the output for  
 217 example  $i$ , which here is the value from the softmax function.

## 218 4. Experimental study

219 Seven conditions of MMCs status have been recorded which include normal, A-phase lower  
 220 SMs, A-phase upper SMs, B-phase lower SMs, B-phase upper SMs, C-phase lower SMs, and C-phase  
 221 upper SMs faults. 100 examples were collected from each condition. So there are a total of 700 (100 x  
 222 7) raw data files to process with. All the nine parameters, i.e.,  $I_a, I_b, I_c, i_{ap}, i_{bp}, i_{cp}, i_{an}, i_{bn},$  and  $i_{cn}$ , were  
 223 recorded to obtain 5001-time samples.

224 Experiments were conducted for testing data rates from 0.1 to 0.9 and 20 run times for each  
 225 testing data rate. We need to point out that the detection and classification results in the following  
 226 paper are the average of 20 run results. In order not to be influenced by the difference in data used,  
 227 it is important to ensure that these methods work with the same data at each run. The following code  
 228 is pseudo-code which can explain this scenario.

```

229 For TestingDataRate=0.1:0.1:0.9
230   For i=1:20
231     [trainData testData]=split(RawData,TestingDataRate);
232     CNN=trainCNN (trainData);
233     ResultsCNN=CNN(testData);
234     [trainDataCI testDataCI]=combined Information( trainData, testData);
235     AE-basedDNN=trainAE-basedDNN(trainDataCI);
236     ResultsAE= AE-basedDNN(testDataCI);
237     Softmax=trainSoftmax(trainDataCI);
238     ResultsSoftmax =Softmax(testDataCI)
239   End
  
```

240 End

#### 241 4.1. Implementation details and results of CNN

##### 242 4.1.1. Implementation details of CNN

243 Figure 4 illustrates the architecture of CNN for fault detection and classification. The input data  
 244 is the raw sensor signals. Each channel denotes one sensor which records 5001-time samples. So the  
 245 size of input current signals is [5001x1x9], where the length is 5001 and the height is 1 as the signals  
 246 are one dimensional, and the depth is 9 as the signals come from 9 channels. The input is convolved  
 247 with 6 filters of size [30 1] with stride 9 and padding 3, then applied a leaky ReLU function, in which  
 248 the scalar multiplier for negative inputs is set as 0.01, resulting in a new feature map of size 554x1  
 249 and 6 channels. The sequence is pooling operation which is applied to each feature map separately.  
 250 Our pooling size is set 6x1 and stride is 6. Therefore, a convolution feature map is divided into several  
 251 disjoint patches and then the average value in each patch is selected to represent the patch and  
 252 transmit to the pooling layer, then the feature map is reduced to 94x1 by the pooling operation.

253 As stochastic gradient descent with momentum (SGDM) algorithm may reduce the oscillations  
 254 along the path of the steepest descent towards the optimum that is sometimes caused by stochastic  
 255 gradient descent algorithm [36], we use the SGDM algorithm to update the parameters of the deep  
 256 NN. The momentum is set at 0.95, the learning rate is 0.01 and the maximum number of epochs to  
 257 use for training is set at 30.

##### 258 4.1.2. Results of CNN

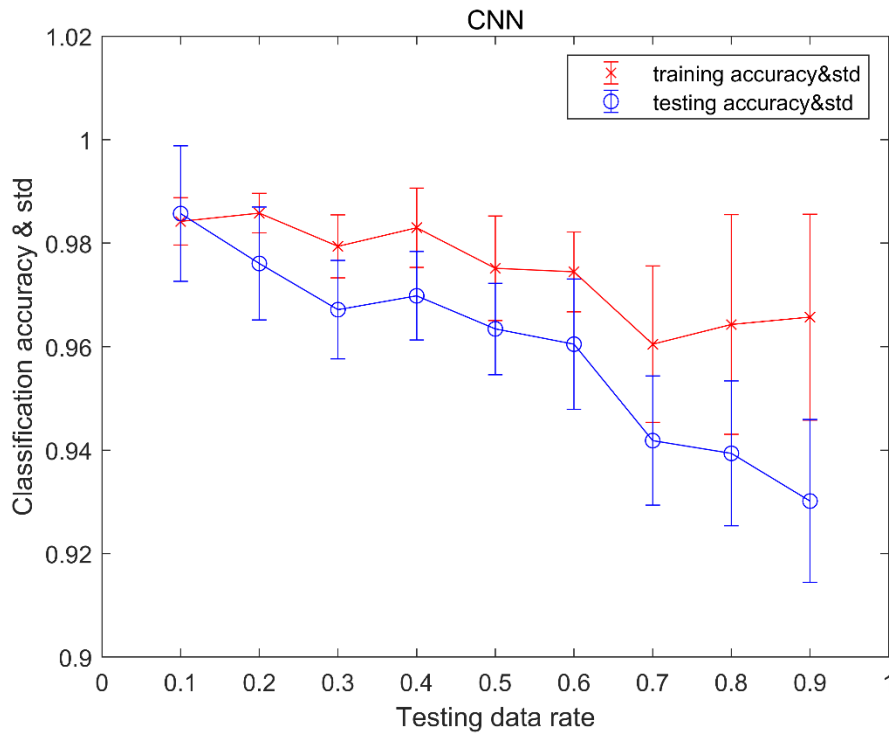
259 The accuracy of the CNN fault detection is shown in Table 2. For fault detection, the output  
 260 network is divided into two types: fault and normal. We can see from Table 2 when the testing rate  
 261 is 0.1~0.5 and 0.7, the detection accuracy is 100%. The min of the detection accuracy is 99.7% at the  
 262 testing rate of 0.9. In which, there are 0.3% fault cases are misclassified as normal cases.

263 **Table 2 Fault detection accuracy of CNN**

Testing data rate	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
Detection accuracy(%)	100	100	100	100	100	99.9	100	99.8	99.7

264 The classification results of training and testing data using convolutional NNs are shown in  
 265 figure 6. From the viewpoint of trending, we can see that with the testing data rate increases, both  
 266 classification accuracy for training data and testing data decline. For the training dataset, the standard  
 267 deviation of classification accuracy increases with the increase of the testing data rate. For testing data  
 268 set, the max of mean accuracy is 98.6% with testing data rate 0.1 and the min of the average accuracy  
 269 is 93.0% with testing data rate 0.9. The standard deviation of classification accuracy in the middle of  
 270 the testing data rate is smaller than both ends of the testing data rate. Moreover, for each testing data  
 271 rate, the standard deviation of classification accuracy for the training data set is less than the standard  
 272 deviation of classification accuracy for the testing data set.





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**Figure 6.** The classification accuracy and the standard deviation of CNN

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Table.3 provides a confusion matrix of the classification results for each condition with testing data rates of 0.2, 0.5 and 0.8. As can be seen from Table.3 that the recognition of the normal condition of the MMCs is 100% with 0.2, 0.5, and 0.8 testing data rates. With 0.2 testing data rate, our method misclassified 3.2% of testing examples of condition 4 as condition 2 and 2% of testing examples of condition 4 as condition 6; With 0.5 testing data rate, our method misclassified 1.6% of testing examples of condition 4 as condition 2 and 3.4% of testing examples of condition 4 as condition 6; Furthermore, with 0.8 testing data rate, our method misclassified 0.8% of testing examples of condition 4 as condition 2 and 6.4% of testing examples of condition 4 as condition 6.

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**Table.3** Sample confusion matrix of the classification results of CNN

Testing data rate=0.2							Testing data rate=0.5							Testing data rate=0.8						
100	0	0	0	0	0	0	100	0	0	0	0	0	0	100	0.2	0	0	0	0.5	1
0	97.8	0	3.2	0	0	0	0	95	0	1.6	0.2	0.7	1.3	0	91.6	0	0.8	0	0.9	2.3
0	0	97.3	0	0	0	0.8	0	0	97.2	0	0.9	0	1.1	0	0	94.4	0	2.5	0	2.2
0	0.7	0	94.8	0	2.2	0	0	1	0	95	0	1.9	0	0	3.8	0.4	92.8	0	0.6	0.2
0	0	2.2	0	99.8	0	3.2	0	0	1.9	0	96.1	0	3	0	0	3.2	0	90.8	0	2.5
0	0.7	0	2	0	97.8	0	0	3.6	0.2	3.4	0.3	96.9	0.4	0	4	0.3	6.4	0.6	97.1	0.9
0	0.2	0.5	0	0.2	0	96	0	0.4	0.7	0	2.5	0.5	94.2	0	0.4	1.7	0	6.1	0.9	90.9

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#### 4.2. Implementation details and results of AE-based DNN

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##### 4.2.1. Implementation details of AE-based DNN

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First, the measurements of nine current signals were concatenated to form a vector of samples that represent the current health condition of the MMCs. This gave a total of 45009 (5001 × 9) samples dimension for each vector of health condition. Second, we used the AE with three layers: the input layer, hidden layer, and output layer. In which, the number of neurons in the hidden layer is set as 250 which means the sample dimension will be reduced from 45009 to 250. An AE network consists of an encoder and a decoder. The transfer function for the encoder and the decoder is the Satlin

292 function and the logistic sigmoid function, respectively. Satlin function is a positive saturating linear  
 293 transfer function given as:

$$f(z) = \begin{cases} 0, & \text{if } z \leq 0 \\ z, & \text{if } 0 < z < 1, \\ 1, & \text{if } z \geq 1 \end{cases} \quad (9)$$

294 The algorithm to use for training the autoencoder applied scaled conjugate gradient descent  
 295 (SCGD). The maximum number of training epochs for this autoencoder is set as 10. Third, the 250  
 296 features achieved by trained AE are used as the input of the Softmax classifier. The maximum number  
 297 of training epochs for the Softmax classifier is set as 20. Next, we stacked the trained AE and Softmax  
 298 classifier into a deep NN. Finally, we trained this deep NN using the training data.

#### 299 4.2.2. Results of AE-based DNN

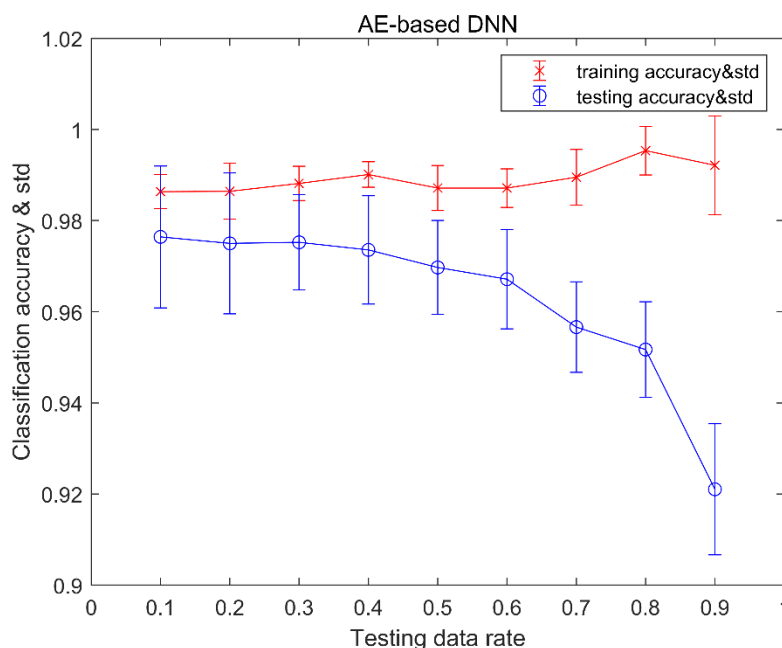
300 The fault detection results of the AE -based DNN are shown in table 4. When the testing rate  
 301 varies from 0.1 to 0.7, the detection accuracy is 100%. The lowest detection accuracy is 99.7% at the  
 302 testing rate of 0.9. In which, there are 0.3% fault cases are misclassified as normal cases. Compared  
 303 with Table 2 of CNN, AE-based DNN has better detection accuracy.

304

**Table 4.** Detection accuracy of AE -based DNN

Testing data rate	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
Detection accuracy	100	100	100	100	100	100	100	99.9	99.7

305 Figure 7 shows the classification results of training and testing data using AE-based DNN. From  
 306 the viewpoint of trending analysis, we can see that with the testing data rate increase, the  
 307 classification mean accuracy for testing data declines but the classification accuracy for training data  
 308 increases. For the training data set, the highest average accuracy is 99.5% with testing data rate 0.8  
 309 and the lowest is 98.6% with testing data rate 0.1. The standard deviation of classification accuracy  
 310 increases with the increase of the testing data rate. For the testing data set, the max of mean accuracy  
 311 is 97.6% with testing data rate 0.1 and the min of mean accuracy is 92.1% with testing data rate 0.9.  
 312 The standard deviation of classification accuracy in the middle of the testing data rate is smaller than  
 313 both ends of the testing data rate. We also can see that for each testing data rate the standard deviation  
 314 of classification accuracy for the training data set is less than the standard deviation of classification  
 315 accuracy for the testing data set.



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**Figure 7.** The classification accuracy and the standard deviation of AE-based DNN

318 Table 5 provides a confusion matrix of the classification results for each condition with testing  
 319 data rates of 0.2, 0.5 and 0.8. As can be seen from Table 5 that the recognition of the normal condition  
 320 of the MMCs is 100% with 0.2, 0.5, and 0.8 testing data rates. With 0.2 testing data rate, our method  
 321 misclassified 1.5% of testing examples of condition 3 as condition 5; With 0.5 testing data rate, our  
 322 method misclassified 1.8% of testing examples of condition 3 as condition 5 and 0.2% of testing  
 323 examples of condition 3 as condition 7. With 0.8 testing data rate, our method misclassified 0.7% of  
 324 testing examples of condition 3 as condition 4, 1.6% of testing examples of condition 3 as condition 5,  
 325 1% of testing examples of condition 3 as condition 6 and 1.9% of testing examples of condition 3 as  
 326 condition 7.

327 **Table 5.** Sample confusion matrix of the classification results of AE-based DNN

Testing data rate=0.2							Testing data rate=0.5							Testing data rate=0.8						
100	0	0	0	0	0	0	100	0	0	0	0	0	0	100	0.1	0	0	0	0.2	0.4
0	97	0	3.2	0	1.5	0.3	0	96.3	0	2	0.3	0.8	1.3	0	96.1	0	1.4	0.7	0.8	2.4
0	0	98.5	0	0	0	0	0	0	98	0	0.4	0	0.5	0	0	94.8	0	2.1	0.1	1.8
0	0.7	0	95.5	0	1	0.2	0	1.5	0	97	0	1.8	0.1	0	2.5	0.7	96.1	0	2	1.4
0	0	1.5	0	97	0	2.5	0	0	1.8	0	97.2	0	3.8	0	0.1	1.6	0	92.6	0	2.7
0	2.3	0	1.3	0.5	97.5	0	0	1.5	0	1	1.2	96	0	0	0.6	1	2.5	1.2	96.4	1
0	0	0	0	2.5	0	97	0	0.7	0.2	0	0.9	1.4	94.3	0	0.6	1.9	0	3.4	0.5	90.3

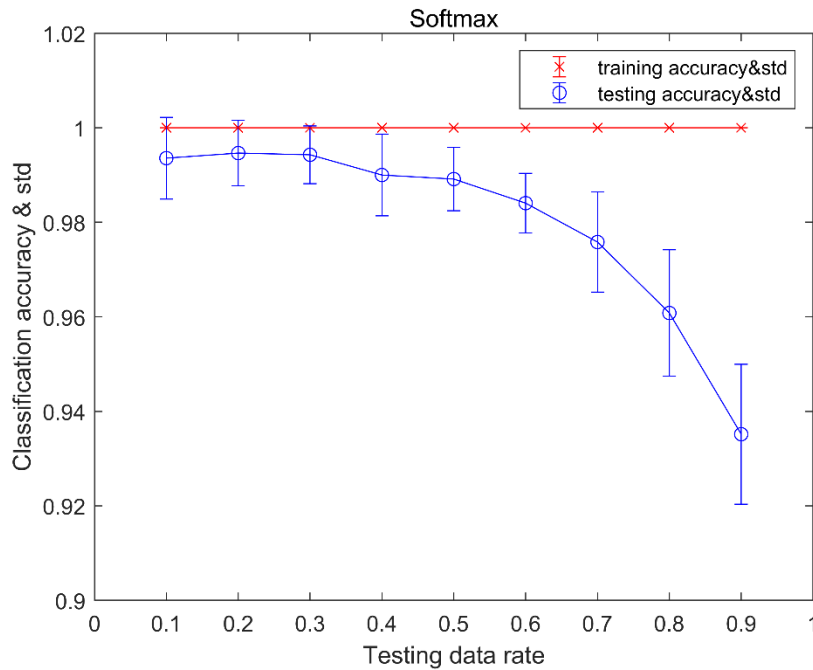
### 328 4.3. Results of Softmax classifier

329 The accuracy of Softmax Classifier fault detection is shown in Table 6. The detection accuracy is  
 330 100% at all testing rates.

331 **Table 6.** Detection accuracy of AE -based DNN

Testing data rate	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
Detection accuracy	100	100	100	100	100	100	100	100	100

332 Figure 8 shows the classification results of training and testing data using the Softmax classifier.  
 333 From the trending view, we can see that with the testing data rate increases, the classification average  
 334 accuracy for testing data declines but the classification average accuracy for training data keeps  
 335 steady which is 100%. The standard deviation of classification accuracy in the middle of the testing  
 336 data rate is smaller than both end of testing data rate for testing data set but the standard deviation  
 337 of classification accuracy keeps steady which is 0. For testing data set, the highest average accuracy  
 338 is 99.46% with testing data rate of 0.2 and the lowest average accuracy is 93.52% with testing data rate  
 339 of 0.9. It is obvious to see that for each testing data rate the standard deviation of classification  
 340 accuracy for training data set is less than the standard deviation of classification accuracy for testing  
 341 data set.



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**Figure 8.** The classification accuracy and the standard deviation of the stand-alone Softmax classifier

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Table 7 provides a confusion matrix of the classification results for each condition with testing data rates of 0.2, 0.5 and 0.8. As can be seen from Table 7 that the recognition of the normal condition of the MMCs is 100% with 0.2, 0.5, and 0.8 testing data rate. With 0.2 testing data rate, our method misclassified none of the testing examples of condition 4; With 0.5 testing data rate, our method misclassified 0.4% of testing examples of condition 4 as condition 2. With 0.8 testing data rate, our method misclassified 1.5% of testing examples of condition 4 as condition 2 and 1.88% of testing examples of condition 4 as condition 6.

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**Table 7.** Sample confusion matrix of the classification results of the stand-alone Softmax classifier

Testing data rate=0.2							Testing data rate=0.5							Testing data rate=0.8						
100	0	0	0	0	0	0	100	0	0	0	0	0	0	100	0	0	0	0	0	0
0	98.5	0	0	0	0.5	0.5	0	98.1	0	0.4	0.2	0.8	0.4	0	97.1	0	1.5	0.4	1.4	3.7
0	0	100	0	0.2	0	0	0	0	99.4	0	0.7	0	0.2	0	0	95.6	0	1.3	0	0.5
0	0	0	100	0	0.8	0	0	0.7	0	99.6	0	0.6	0	0	2.2	0.3	96.6	0	2.3	0
0	0	0	0	99.8	0	0	0	0	0.6	0	99.1	0	0.6	0	0	1.5	0	94.3	0	2
0	1.5	0	0	0	98.5	0	0	0.6	0	0	0	97.4	0	0	0.5	0.3	1.9	0.8	95.9	0.7
0	0	0	0	0	0.2	99.5	0	0.6	0	0	0	1.2	98.8	0	0.2	2.3	0	3.2	0.4	93.1

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Above all, for the training data set, with the increase of testing data rate, the average accuracy of Softmax keeps steady which is 100% and the average accuracy of CNN decreases but the average accuracy of AE-based increases. The standard deviation of accuracy for SoftMax keeps steady which is 0 and the standard deviation of accuracy for other methods increases with the increase of the testing data rate. For the testing data set, the average accuracy of all methods decreases with the increase of the testing data rate. And the standard deviation of accuracy in the middle is less than both ends of the testing data rate for all methods.

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## 5. Comparisons

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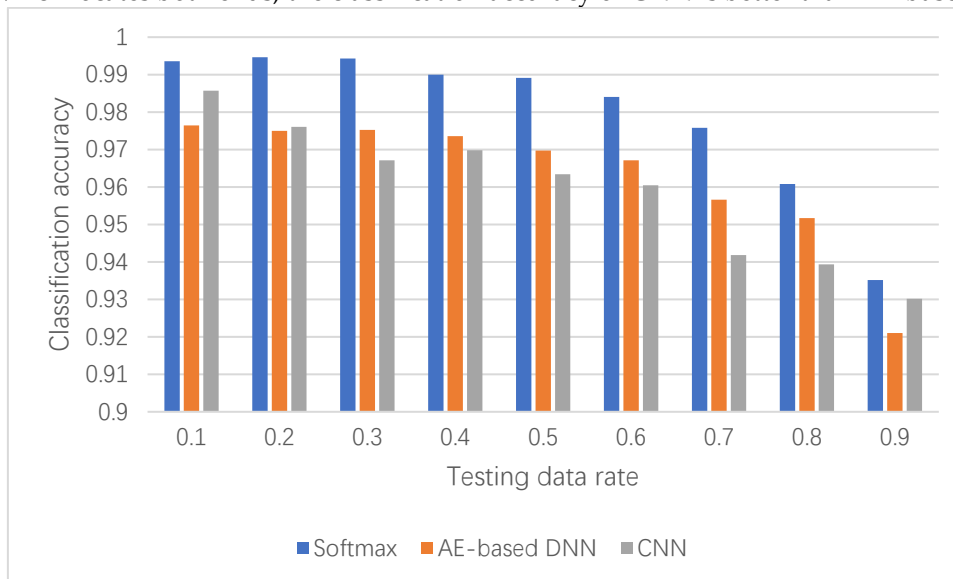
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We compared the three methods on the classification accuracy and the standard deviation of classification accuracy for the testing data with the testing data rate from 0.1 to 0.9 and compared the three methods from the viewpoint of training time spent and testing time spent which are presented in Figure 9~11 respectively.

## 364 5.1. Comparison of average accuracy

365 From figure 9, we can see that the Softmax classifier behaves outstandingly on the testing data  
 366 rate from 0.1 to 0.9 compared to CNN and AE-based DNN. When the testing data rate is 0.1, 0.2 and  
 367 0.9 which locates both ends, the classification accuracy of CNN is better than AE-based DNN.

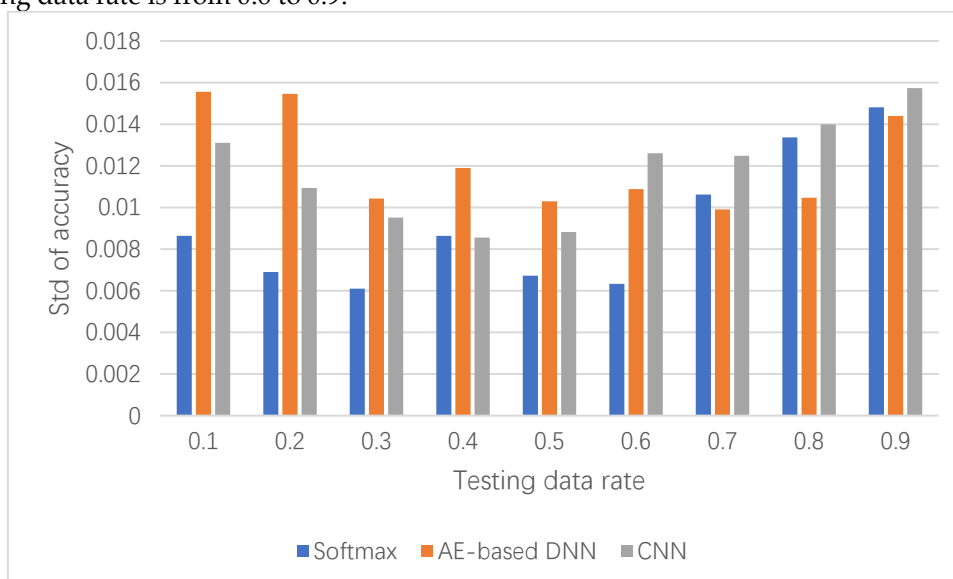


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**Figure 9.** Comparison of classification accuracy for the three methods

## 370 5.2. Comparison of Standard deviation

371 We know that in statistics, the standard deviation is a measure that is used to quantify the  
 372 amount of variation or dispersion of a set of data values. A low standard deviation indicates that the  
 373 values tend to be close to the expected value of set, while a high standard deviation indicates that the  
 374 values are spread out over a wider range. From figure 10, it is clear that the standard deviation of  
 375 accuracy of Softmax is lower than other methods when the testing data rate is 0.1 to 0.6, which means  
 376 that for every run for different training data set and testing data set, the classification accuracy of  
 377 Softmax is more stable and other methods are more spread out. When the testing data rate varies  
 378 from 0.7 to 0.9, the AE-based DNN has the lowest standard deviation. AE-based DNN is the most  
 379 spread out when the testing data rate is from 0.1 to 0.5 and CNN is the most spread out when the  
 380 testing data rate is from 0.6 to 0.9.

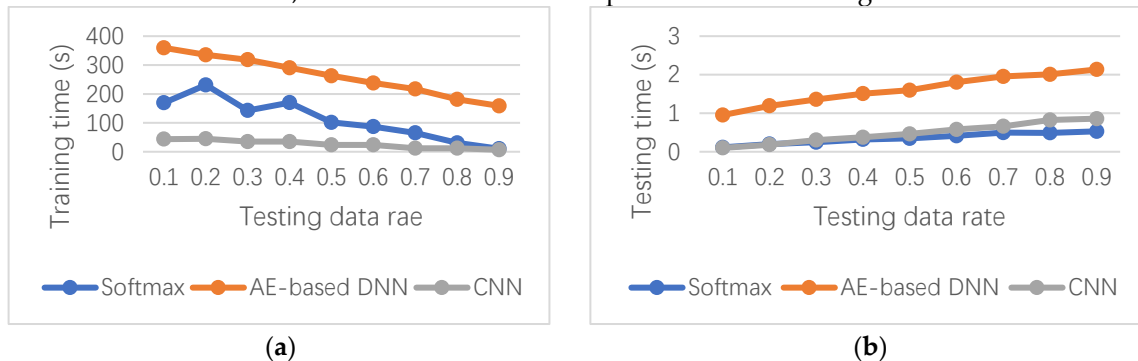


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**Figure 10.** Comparison of the standard deviation of classification accuracy for the three methods

### 383 5.3. Speed Comparison

384 Figure 11 describes the training time and testing time spent by three methods. It shows that for  
 385 each testing data rate, the AE-based DNN spends more training time than other methods, and the  
 386 CNN spends the least training time, and the Softmax takes the least testing time when the testing  
 387 data rate is from 0.3 to 0.9, and the AE-based DNN spends the most testing time.



388 **Figure 11.** Comparison of speed for the three methods. (a) Comparison of training time spent by the  
 389 three methods; (b) Comparison of testing time spent by the three methods.

390 Over all, the stand-alone Softmax Classifier provides better functionality, including fault  
 391 detection accuracy, classification accuracy, least standard deviation and speed, as well as its strong  
 392 ability to dealing with high dimensional data. The AE-based DNN has the second best classification  
 393 ability, but it needs more training time and testing time. CNN has enough classification accuracy and  
 394 it needs the least training time.

### 395 6. Conclusions

396 Fault detection and classification are two of the challenging tasks in MMC-HVDC systems. This  
 397 paper presented two deep learning methods (CNN and AE-based DNN) and a stand-alone Softmax  
 398 classifier for fault detection and classification. CNN and AE-based DNN can fuse both feature  
 399 extraction and classification operations into a single machine learning scheme for joint optimization  
 400 to maximize the classification performance, which avoided the design of handcrafted features. In this  
 401 paper, we only use raw current sensor data as input to our proposed approaches to detect and classify  
 402 faults of MMC-HVDC. The simulation results in PSCAD/EMTDC show that three methods all have  
 403 high detection accuracy more than 99.7%, in which the stand-alone Softmax classifier has 100%  
 404 detection accuracy, and AE-based DNN is a little better than of CNN. Three methods also have high  
 405 classification accuracy, small standard deviation, and high speed. Softmax classifier behaved better  
 406 than others in classification accuracy and testing speed, while CNN needs the least training time.

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 408 this paper. Yuexiao Yu performed the experiments and generated the raw data, Mohamed Darwish gave the  
 409 best suggestions about these experiments. Qinghua Wang analyzed the data and wrote a draft of the paper. All  
 410 authors contributed to discussing the results and revising the manuscript.

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