# Measurement of the $B \rightarrow X_{s} \ell^{+} \ell^{-}$Branching Fraction Using a Sum over Exclusive Modes 

The BABAR Collaboration

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#### Abstract

We present a measurement of the branching fraction for the flavor-changing neutral current process $B \rightarrow X_{s} \ell^{+} \ell^{-}$based on a sample of $88.9 \times 10^{6} \Upsilon(4 S) \rightarrow B \bar{B}$ events recorded with the BABAR detector at the PEP-II $e^{+} e^{-}$storage ring. The final state is reconstructed from pairs of electrons or muons and a hadronic system consisting of one $K^{ \pm}$or $K_{s}^{0}$ and up to two pions, with at most one $\pi^{0}$. Summing over both lepton flavors, we observe a signal of $41 \pm 10($ stat $) \pm 2$ (syst) events with a statistical significance of $4.6 \sigma$. The inclusive branching fraction is determined to be $\mathcal{B}\left(B \rightarrow X_{s} \ell^{+} \ell^{-}\right)=\left(6.3 \pm 1.6(\text { stat })_{-1.5}^{+1.8}(\right.$ syst $\left.)\right) \times 10^{-6}$ for $m\left(\ell^{+} \ell^{-}\right)>0.2 \mathrm{GeV} / c^{2}$. All results are preliminary.


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## 1 Introduction

The rare decay $B \rightarrow X_{s} \ell^{+} \ell^{-}$proceeds through a $b \rightarrow s \ell^{+} \ell^{-}$transition, which is forbidden at tree level in the Standard Model (SM). However, such a flavor-changing neutral current (FCNC) process can occur at higher order via electroweak penguin and $W^{+} W^{-}$box diagrams, as shown in Figure 1 The $b \rightarrow s \ell^{+} \ell^{-}$transition therefore allows deeper insight into the effective Hamiltonian describing FCNC processes and is sensitive to the effects of non-SM physics that may enter these loops; see, for example, Refs. [1, 2].

Recent calculations of the branching fractions for the exclusive decay modes predict $\mathcal{B}(B \rightarrow$ $\left.K e^{+} e^{-}\right)=\mathcal{B}\left(B \rightarrow K \mu^{+} \mu^{-}\right)=(0.35 \pm 0.12) \times 10^{-6}, \mathcal{B}\left(B \rightarrow K^{*} e^{+} e^{-}\right)=(1.58 \pm 0.49) \times 10^{-6}$ and $\mathcal{B}\left(B \rightarrow K^{*} \mu^{+} \mu^{-}\right)=(1.19 \pm 0.39) \times 10^{-6}$, and for the inclusive processes $\mathcal{B}\left(B \rightarrow X_{s} e^{+} e^{-}\right)=$ $(6.9 \pm 1.0) \times 10^{-6}$ and $\mathcal{B}\left(B \rightarrow X_{s} \mu^{+} \mu^{-}\right)=(4.2 \pm 0.7) \times 10^{-6}[1]$. In the electron channel, the branching fraction is predicted to be $\mathcal{B}\left(B \rightarrow X_{s} e^{+} e^{-}\right)=(4.2 \pm 0.7) \times 10^{-6}$ [3] for $m\left(e^{+} e^{-}\right)>0.2 \mathrm{GeV} / c^{2}$. Measurements of the inclusive branching fractions are motivated by the smaller theoretical uncertainties, as compared with predictions for exclusive decays. Both the Belle and BABAR Collaborations have observed the $B \rightarrow K \ell^{+} \ell^{-}(\ell=e, \mu)$ decay [4, 5], BABAR has found evidence for the $B \rightarrow K^{*} \ell^{+} \ell^{-}$decay [6], and Belle has measured the inclusive $B \rightarrow X_{s} \ell^{+} \ell^{-}$decay [7].

In the present analysis, we study the $B \rightarrow X_{s} \ell^{+} \ell^{-}$process by reconstructing the final state from pairs of electrons or muons and a hadronic system consisting of one $K^{ \pm}$or $K_{s}^{0}$ and up to two pions, with at most one $\pi^{0}$. The choice of maximum number of pions is motivated by the fact that the signal-to-background ratio drops significantly with increasing multiplicity. This approach [8], which sums over exclusive modes, allows approximately half of the full inclusive rate to be reconstructed. If the fraction of modes containing a $K_{L}^{0}$ is taken to be equal to that containing a $K_{S}^{0}$, the missing states that remain unaccounted for represent $\sim 25 \%$ of the total rate. We require the hadronic mass for the selected final states to be less than $1.8 \mathrm{GeV} / c^{2}$ to reduce combinatorial background. This cut retains approximately $94 \%$ of the signal in the reconstructed modes. We correct for the missing modes and the effect of the hadronic mass cut to extract the inclusive $B \rightarrow X_{s} \ell^{+} \ell^{-}$decay rate for $m\left(\ell^{+} \ell^{-}\right)>0.2 \mathrm{GeV} / c^{2}$.


Figure 1: Feynman diagrams for $b \rightarrow s \ell^{+} \ell^{-}$transitions.

## 2 The BABAR Detector and Data Sample

The data sample used in this analysis was collected with the BABAR detector during 1999-2002 at the PEP-II asymmetric-energy $e^{+} e^{-}$storage ring at the Stanford Linear Accelerator Center. It consists of $81.9 \mathrm{fb}^{-1}$ recorded at the $\Upsilon(4 S)$ resonance, corresponding to $88.9 \times 10^{6} \Upsilon(4 S) \rightarrow B \bar{B}$ events, as well as an additional $9.6 \mathrm{fb}^{-1}$ recorded 40 MeV below the $\Upsilon(4 S)$ resonance. The offresonance data provide a clean sample of $e^{+} e^{-} \rightarrow q \bar{q}$ (with $q=u, d, s, c$ ) continuum events for
background studies.
This analysis relies on the charged-particle tracking systems and particle identification systems of the BABAR detector [9. A 5-layer silicon vertex tracker (SVT) and a 40-layer drift chamber ( DCH ) provide tracking and particle identification for charged particles. The DIRC, a Cherenkov ring-imaging system, is primarily used for charged hadron ( $\pi, K, p$ ) identification. The electromagnetic calorimeter (EMC), consisting of Tl-doped CsI crystals, provides electron identification and photon reconstruction. These detectors are located inside a $1.5-\mathrm{T}$ solenoidal superconducting magnet. Muons are identified in the instrumented flux return (IFR) with resistive plate chambers interleaved with iron plates.

Clean particle identification for the final state particles $e^{ \pm}, \mu^{ \pm}, K^{ \pm}, K_{s}^{0}, \pi^{ \pm}$and $\pi^{0}$ is important for this analysis. Electrons and muons are required to have lab-frame momenta greater than $0.5 \mathrm{GeV} / c$ and $1.0 \mathrm{GeV} / c$, respectively. Bremsstrahlung photons from electrons are recovered by combining an electron with up to three photons within a small angular region around the electron direction [10]. $K_{s}^{0}$ candidates are reconstructed from pairs of oppositely-charged tracks with $\left|m\left(\pi^{+} \pi^{-}\right)-m\left(K_{s}^{0}\right)\right|<11.2 \mathrm{MeV} / c^{2}$, decay length greater than 2 mm , and angle between the $K_{s}^{0}$ momentum vector and the line between the primary vertex and the $K_{s}^{0}$ vertex satisfying $\cos \delta>0.99$. Charged pions are selected from tracks after rejection of cleanly identified $e^{ \pm}$and $K^{ \pm}$ candidates. Neutral pions are required to have lab-frame energy greater than 400 MeV , photon daughter energies greater than 50 MeV , and a $\gamma \gamma$ invariant mass that satisfies $\left|m(\gamma \gamma)-m\left(\pi^{0}\right)\right|<$ $10 \mathrm{MeV} / c^{2}$.

## 3 Analysis overview

We use a technique that sums over exclusive modes to measure the inclusive branching fraction $\mathcal{B}\left(B \rightarrow X_{s} \ell^{+} \ell^{-}\right)$. Compared to a fully inclusive approach, this method has the advantage of being able to exploit the strong kinematical discrimination provided by $m_{E S}=\sqrt{E_{b e a m}^{2}-\vec{p}_{B}^{2}}$ and $\Delta E=E_{B}-E_{\text {beam }}$, where $E_{\text {beam }}$ is the beam energy and $E_{B}\left(\vec{p}_{B}\right)$ is the reconstructed $B$ meson energy ( 3 -momentum). All quantities are evaluated in the $e^{+} e^{-}$center-of-mass system (CM). This analysis approach is needed to suppress large backgrounds from $B \bar{B}$ and continuum events, and to extract the expected small signal yield.

The main contribution to the combinatorial background is from semileptonic decays in $B \bar{B}$ events. In these events, $B \rightarrow X_{s} \ell^{+} \ell^{-}$candidates contain decay products from both $B$ mesons (i.e., the daughters of the $B \rightarrow X_{s} \ell^{+} \ell^{-}$candidate do not originate from the same point) and there is a significant amount of missing energy due to neutrinos. Another contribution to the combinatorial background is due to continuum events, which are effectively suppressed with event-shape variables.

The dominant peaking backgrounds, which are from $B \rightarrow J / \psi X$ and $B \rightarrow \psi(2 S) X$ decays with $J / \psi(\psi(2 S)) \rightarrow \ell^{+} \ell^{-}$, mimic the signal and need to be efficiently removed with cuts on the dilepton mass $m\left(\ell^{+} \ell^{-}\right)$. The resulting veto sample provides a large control sample of decays with a signature identical to that of the signal, albeit in a restricted range of $m\left(\ell^{+} \ell^{-}\right) . B \rightarrow D^{(*)} n \pi(n>0)$ decays with misidentification of two charged pions as leptons present an additional source of peaking background.

Simulated $B \rightarrow X_{s} \ell^{+} \ell^{-}$events are produced with a combination of exclusive and inclusive models. In the hadronic mass region of $m\left(X_{s}\right)<1.1 \mathrm{GeV} / c^{2}$, exclusive $B \rightarrow K^{(*)} \ell^{+} \ell^{-}$decays are generated according to 1, 11, where the relevant form factors are computed using light-cone QCD sum rules. The remaining decays, in the region $m\left(X_{s}\right)>1.1 \mathrm{GeV} / c^{2}$, are generated with
a nonresonant model following [1, 12] and using the Fermi motion model of [13]. JETSET [14] is then used to hadronize the system consisting of a strange quark and a spectator quark.

## 4 Event selection

Events are required to have a well determined primary vertex, be tagged as multi-hadron events, have a ratio of the second to zeroth-order Fox-Wolfram moments [15] (calculated using charged tracks and neutral calorimeter clusters) of $R_{2}<0.5$, have at least four charged tracks, and contain at least two leptons (either electrons or muons) satisfying loose particle identification criteria and having lab-frame momenta greater than $0.5 \mathrm{GeV} / c$ for electrons and $0.8 \mathrm{GeV} / c$ for muons.

In the next step, $B$ candidates are reconstructed. A dilepton is selected by choosing the $e^{+} e^{-}$ or $\mu^{+} \mu^{-}$pair with the largest value of $\left|p\left(\ell^{+}\right)\right|+\left|p\left(\ell^{-}\right)\right|$, using lab-frame momenta. The dilepton candidate is required to form a good vertex. Using this $\ell^{+} \ell^{-}$pair, $B \rightarrow X_{s} \ell^{+} \ell^{-}$candidates are formed by adding either a $K^{ \pm}$or a $K_{s}^{0}$ and up to two pions, but no more than one $\pi^{0}$. In this manner, ten different hadronic topologies are considered: $K^{+}, K^{+} \pi^{0}, K^{+} \pi^{-}, K^{+} \pi^{-} \pi^{0}, K^{+} \pi^{-} \pi^{+}$, $K_{S}^{0}, K_{S}^{0} \pi^{0}, K_{S}^{0} \pi^{+}, K_{S}^{0} \pi^{+} \pi^{0}$, and $K_{S}^{0} \pi^{+} \pi^{-}$.

The resulting $B$ candidates are required to have an $\ell^{+} \ell^{-}$vertex fit probability $\log \left(P_{l l v t x}\right)>-10$, a $B$ vertex constructed from charged daughter particles with fit probability $\log \left(P_{B v t x}\right)>-10$, $m\left(X_{s}\right)<2.5 \mathrm{GeV} / c^{2}, 5.0<m_{E S}<5.29 \mathrm{GeV} / c^{2}$, and $|\Delta E|<0.3 \mathrm{GeV}$.

At this stage, there is an average of five $B$ candidates per event in the signal simulation. Only the $B$ candidate with the largest signal likelihood value is retained. The signal likelihood function is constructed based on the simulated distributions of $\Delta E, \log \left(P_{B v t x}\right)$, and $\cos \theta_{B}$ for the signal, where $\theta_{B}$ is the angle between the momentum vector of the $B$ candidate and the beam axis in the CM frame. We select the best candidate before further selection cuts are applied. This approach entails a small cost in signal efficiency, which is more than compensated by an improved background suppression in the final sample.

After selecting the best candidate, combinatorial backgrounds are suppressed by tightening some of the earlier requirements: $m\left(X_{s}\right)<1.8 \mathrm{GeV} / c^{2}, 5.20<m_{E S}<5.29 \mathrm{GeV} / c^{2}$, and $-0.2<$ $\Delta E<0.1 \mathrm{GeV}$. In addition, we require the separation between the two leptons along the beam direction to satisfy $|\Delta z|<0.15 \mathrm{~cm}$, where the $z$-coordinate of each lepton is determined at the point of closest approach to the beam axis. We also require the rest of the event, formed by combining all charged tracks and neutral calorimeter clusters not included in the $B$ candidate, to satisfy $-5.0<\Delta E^{R O E}<2.0 \mathrm{GeV}$ and $m_{E S}^{R O E}>4.9 \mathrm{GeV} / c^{2}$.

Charmonium backgrounds are reduced by removing $B$ candidates with dilepton mass in the ranges $2.70<m\left(e^{+} e^{-}\right)<3.25 \mathrm{GeV} / c^{2}, 2.80<m\left(\mu^{+} \mu^{-}\right)<3.20 \mathrm{GeV} / c^{2}, 3.45<m\left(e^{+} e^{-}\right)<$ $3.80 \mathrm{GeV} / c^{2}$, and $3.55<m\left(\mu^{+} \mu^{-}\right)<3.80 \mathrm{GeV} / c^{2}$. If one of the electrons from a $J / \psi$ or $\psi(2 S)$ decay erroneously picks up a random photon in the Bremsstrahlung-recovery process, the dilepton mass can increase sufficiently to evade the above cuts. Therefore the charmonium veto is applied to the dilepton mass before and after Bremsstrahlung recovery. Using the simulation, we estimate the remaining peaking charmonium background to be $0.6 \pm 0.3$ events and $0.3 \pm 0.2$ events for $e^{+} e^{-}$ modes and $\mu^{+} \mu^{-}$modes, respectively.

The potential peaking background from $B \rightarrow X_{s} \gamma$ decays, followed by conversion of the photon into an $e^{+} e^{-}$pair in the detector material, is a concern for the $e^{+} e^{-}$modes only. After observing an excess of events in data over the simulation for low $e^{+} e^{-}$mass in the $m_{E S}<5.27 \mathrm{GeV} / c^{2}$ sideband distribution, we completely remove this background by requiring $m\left(e^{+} e^{-}\right)>0.2 \mathrm{GeV} / c^{2}$.

The final suppression of the combinatorial background is achieved with a likelihood ratio $\mathcal{L}_{R}$
based on nine variables: $\Delta E, \Delta E^{R O E}, m_{E S}^{R O E}, \Delta z, \log \left(P_{B v t x}\right), \cos \theta_{\text {miss }}$, where $\theta_{\text {miss }}$ is the angle between the missing momentum vector for the whole event and the $z$ axis in the CM frame, $\cos \theta_{B}$, $\left|\cos \theta_{T}\right|$, where $\theta_{T}$ is the angle between the thrust axes of the $B$ candidate and the rest of the event in the CM frame, and $R_{2}$. The variables $\Delta E, \Delta E^{R O E}$, and $m_{E S}^{R O E}$ are most effective at rejecting $B \bar{B}$ background, especially for events with two semileptonic decays, which have large missing energy. For continuum suppression, the event-shape variables $\left|\cos \theta_{T}\right|$ and $R_{2}$ are most useful. The distribution for the background-discrimination variable $i$ is parameterized by a PDF $\eta_{i}^{j}$ for each component $j$ of the sample: $j=1$ for signal, $j=2$ for $B \bar{B}$ background, and $j=3$ for continuum background. A likelihood is then computed for each sample component as the product of the individual PDFs for that component: $\mathcal{L}^{j}=\prod_{i} \eta_{i}^{j}$. The ratio between the likelihood for the signal component and the sum of the signal and background likelihoods then provides the final discriminating variable, the likelihood ratio $\mathcal{L}_{R}=\mathcal{L}^{\text {signal }} /\left(\mathcal{L}^{\text {signal }}+\mathcal{L}^{B \bar{B}}+\mathcal{L}^{\text {cont }}\right)$.

Using the simulation, the cut on $\mathcal{L}_{R}$ is optimized to maximize the statistical significance of the signal. This optimization is performed separately for $e^{+} e^{-}$modes and $\mu^{+} \mu^{-}$modes in the three $m\left(X_{s}\right)$ regions $m\left(X_{s}\right)<0.6 \mathrm{GeV} / c^{2}, 0.6<m\left(X_{s}\right)<1.1 \mathrm{GeV} / c^{2}$, and $1.1<m\left(X_{s}\right)<1.8 \mathrm{GeV} / c^{2}$, resulting in the cuts $\mathcal{L}_{R}>0.3,0.4$, and 0.9 for the $e^{+} e^{-}$modes and $\mathcal{L}_{R}>0.2,0.6$, and 0.9 for the $\mu^{+} \mu^{-}$modes.

After applying all selection criteria, a sample of $349 B \rightarrow X_{s} e^{+} e^{-}$and $222 B \rightarrow X_{s} \mu^{+} \mu^{-}$ candidates remains. According to the simulation, the background left at this stage of the analysis consists mostly of $B \bar{B}$ events ( $86 \%$ and $72 \%$ of the total background in the electron and muon channels, respectively).

## 5 Maximum likelihood fit

We perform an extended, unbinned maximum likelihood fit to the $m_{E S}$ distribution in the region $m_{E S}>5.2 \mathrm{GeV} / c^{2}$ to extract the signal yield as well as the shape and yield of the combinatorial background. The likelihood function $\mathcal{L}$ consists of four components:

$$
\begin{equation*}
\mathcal{L}=\frac{e^{-\left(N_{s i g}+N_{c-p e a k}+N_{h-p e a k}+N_{\text {comb }}\right)}}{N!} \prod_{k=1}^{N}\left[\left(N_{\text {sig }}+N_{c-p e a k}\right) \mathcal{P}_{k}^{c-p e a k}+N_{h-p e a k} \mathcal{P}_{k}^{h-p e a k}+N_{c o m b} \mathcal{P}_{k}^{c o m b}\right] \tag{1}
\end{equation*}
$$

where $N$ and $k$ denote the total number and index of candidate events, respectively. $N_{s i g}, N_{c-p e a k}$, $N_{h-p e a k}$, and $N_{\text {comb }}$ represent the yields of the signal, charmonium peaking background, hadronic peaking background, and combinatorial background, respectively, with corresponding PDFs given by $\mathcal{P}_{k}^{c-\text { peak }}, \mathcal{P}_{k}^{h-\text { peak }}$, and $\mathcal{P}_{k}^{c o m b}$. The signal PDF is the same as that for the charmonium peaking background since it is extracted from the charmonium-veto data sample.

The signal PDF $\mathcal{P}_{k}^{c-p e a k}$ is described by a Gaussian for $\mu^{+} \mu^{-}$modes as well as for $e^{+} e^{-}$modes, since the Bremsstrahlung recovery and selection procedure for $e^{+} e^{-}$modes lead to a negligible radiative tail in the $m_{E S}$ distribution. The Gaussian shape parameters are determined from fits to the sum of a Gaussian and Argus [16] function for the charmonium-veto data sample. The fits yield signal $m_{E S}$ peak positions and resolutions of $m_{\text {sig }}=5280.04 \pm 0.05 \mathrm{MeV} / c^{2}$ and $\sigma_{\text {sig }}=$ $2.80 \pm 0.05 \mathrm{MeV} / c^{2}$ for the $e^{+} e^{-}$modes, and $m_{\text {sig }}=5280.05 \pm 0.07 \mathrm{MeV} / c^{2}$ and $\sigma_{\text {sig }}=2.61 \pm$ $0.06 \mathrm{MeV} / c^{2}$ for the $\mu^{+} \mu^{-}$modes, respectively. In the simulation, the Gaussian fit results for the $m_{E S}$ distributions for correctly reconstructed signal are in agreement with the shape parameters extracted from the fits to the charmonium-veto sample. The signal yield $N_{s i g}$ is a free parameter in the likelihood fit.

The charmonium peaking background is estimated from the simulation to contribute $N_{c-\text { peak }}=$ $0.6 \pm 0.3$ events in the electron modes and $N_{c-p e a k}=0.3 \pm 0.2$ events in the muon modes. In the likelihood fit, $N_{c-p e a k}$ is fixed to these values.

The size and shape of the hadronic peaking $B \bar{B}$ background component arising from $B \rightarrow$ $D^{(*)} n \pi(n>0)$ decays with misidentification of two charged pions as leptons are derived directly from data by performing the analysis without the lepton identification requirements. Parameters for the PDF $\mathcal{P}_{k}^{h-p e a k}$ are taken from a fit to the sum of a Gaussian and Argus function, with $m_{E S}$ peak positions and resolutions of $m_{\text {peak }}=5280.13 \pm 0.06 \mathrm{MeV} / c^{2}$ and $\sigma_{\text {peak }}=2.99 \pm 0.07 \mathrm{MeV} / c^{2}$. Taking the $\pi$ to $\ell$ misidentification rates into account, the remaining hadronic peaking backgrounds are estimated to be $N_{h-p e a k}=2.4 \pm 0.8$ events for the $\mu^{+} \mu^{-}$modes and are negligible for the $e^{+} e^{-}$ modes. In the likelihood fit, $N_{h-p e a k}$ is fixed to the estimated values.

The combinatorial background PDF, $\mathcal{P}_{k}^{c o m b}$, is given by an Argus shape, which describes the combinatorial contribution from continuum events and $B \bar{B}$ events. The Argus cutoff is determined by the beam energy in the $\Upsilon(4 S)$ rest frame, $E_{\text {beam }}=5.290 \mathrm{GeV}$, whereas the Argus shape parameter and the yield $N_{\text {comb }}$ are free parameters in the likelihood fit.

## 6 Results

Using the fit parameterizations described above, we fit the $m_{E S}$ distributions for the selected $B \rightarrow$ $X_{s} e^{+} e^{-}$and $B \rightarrow X_{s} \mu^{+} \mu^{-}$candidates separately and obtain the results shown in Figure 2. The fit results are summarized in Table $\square$ The statistical significance is $\mathcal{S}=\sqrt{2\left(\ln \mathcal{L}_{\text {max }}-\ln \mathcal{L}_{\text {max }}^{0}\right)}$, where $\mathcal{L}_{\text {max }}$ represents the maximum likelihood for the fit and $\mathcal{L}_{\text {max }}^{0}$ denotes the maximum likelihood for a different fit when the signal yield is fixed at $N_{\text {sig }}=0$. The significance does not incorporate effects due to systematic uncertainties in the signal shape or in the contribution from peaking background. However, these have been found to be small. The $B \rightarrow X_{s} \ell^{+} \ell^{-}$signal yield presented in Table 1 is the sum of the $B \rightarrow X_{s} e^{+} e^{-}$and $B \rightarrow X_{s} \mu^{+} \mu^{-}$signal yields. A separate fit to the combined electron and muon channels gives a very similar result.

Figure [2(d) shows the distribution of $m_{E S}$ for $B \rightarrow X_{s} e^{ \pm} \mu^{\mp}$ candidates selected using the nominal selection criteria but requiring that the two leptons have different flavor. This sample provides a cross-check for the parameterization of the combinatorial background. Figure 2(d) shows an Argus fit to the $m_{E S}$ distribution and, as expected, there is no evidence for peaking background. The Argus shape and yield parameters for the combinatorial background are free in the nominal fit to data.

Figure 3 shows the distribution of $m\left(X_{s}\right)$ for electron and muon channels combined. This distribution is obtained by performing the nominal likelihood fit in separate $m\left(X_{s}\right)$ regions. Figure3 indicates that the observed signal receives contributions from final states across a range of hadronic mass, including hadronic systems with mass above that of the $K^{*}$ (892).

The branching fraction $\mathcal{B}$ for the signal is calculated from

$$
\begin{equation*}
\mathcal{B}=\frac{N_{\text {sig }}}{2 N_{B \bar{B}} \epsilon}, \tag{2}
\end{equation*}
$$

where $N_{B \bar{B}}=(88.9 \pm 1.0) \times 10^{6}$ is the number of $B \bar{B}$ pairs produced in $81.9 \mathrm{fb}^{-1}$ and $\epsilon$ is the signal efficiency. The fitted signal yield $N_{s i g}$ contains a contribution from misreconstructed $B \rightarrow X_{s} \ell^{+} \ell^{-}$ decays (cross-feed events) of $1.8 \pm 1.8$ events in the electron channel and $0.9 \pm 0.9$ events in the muon channel. The central values are derived from fits to data in which the nominal fit function is changed to include a cross-feed PDF whose shape and normalization with respect to that for the correctly


Figure 2: Distributions of $m_{E S}$ for selected (a) $B \rightarrow X_{s} e^{+} e^{-}$, (b) $B \rightarrow X_{s} \mu^{+} \mu^{-}$, (c) $B \rightarrow X_{s} \ell^{+} \ell^{-}$ ( $\ell=e, \mu$ ), and (d) $B \rightarrow X_{s} e^{ \pm} \mu^{\mp}$ candidates. The solid lines represent the result of the fits and the dashed lines represent the background component under the signal peaks.
reconstructed $B \rightarrow X_{s} \ell^{+} \ell^{-}$decays are taken from the simulation. The corresponding uncertainties are estimated from Monte Carlo studies using a large number of data-sized experiments. The signal efficiency $\epsilon$ is adjusted to reflect the contribution from cross-feed events.

## $7 \quad$ Systematic uncertainties

Systematic uncertainties are of two different types: those that affect the extraction of the number of signal decays and those that affect the calculation of the branching fraction. The systematic uncertainties are summarized in Table 2

Uncertainties affecting the extraction of the signal yield are evaluated by varying the signal Gaussian parameters (mean and width) and the signal shape (using asymmetric signal shapes) within the constraints allowed by the charmonium veto data. The small amount of peaking background from $B \rightarrow J / \psi X$ and $B \rightarrow \psi(2 S) X$ decays is varied according to the estimated number of such decays: $0.6 \pm 0.3$ and $0.3 \pm 0.2$ in the electron and muon channels, respectively. The peaking background in the muon channel due to $B \rightarrow X_{s} \pi^{+} \pi^{-}$decays is varied according to the estimated number of such events: $2.4 \pm 0.8$, where the uncertainty is dominated by the uncertainty in the

Table 1: Results of the fit to data: signal yield, charmonium and hadronic peaking backgrounds (fixed in the fit), combinatorial background yield, and statistical significance.

| Sample | $N_{\text {sig }}$ | $N_{c-\text { peak }}$ | $N_{h-\text { peak }}$ | $N_{\text {comb }}$ | Signif. |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $X_{s} e^{+} e^{-}$ | $29.0 \pm 8.3$ | 0.6 | 0.0 | $319.4 \pm 18.9$ | 4.0 |
| $X_{s} \mu^{+} \mu^{-}$ | $12.4 \pm 6.2$ | 0.3 | 2.4 | $207.0 \pm 15.2$ | 2.2 |
| $X_{s} \ell^{+} \ell^{-}$ | $41.4 \pm 10.3$ | 0.9 | 2.4 | $526.4 \pm 24.3$ | 4.6 |



Figure 3: Distribution of number of signal events as a function of hadronic mass for electron and muon channels combined for data (points) and Monte Carlo signal (histogram). The vertical error bars represent statistical uncertainties only.
$\pi$ to $\mu$ misidentification rates determined from control samples in the data. The shape of this background is also varied according to the data sample selected without lepton identification. The largest variations in the signal yield are observed for changes in the signal shape and in the amount of peaking background.

Uncertainties affecting the signal efficiency originate from the detector modeling, from the simulation of signal decays, and from the estimate of the number of $B$ mesons in the sample. By far the dominant component is that due to the simulation of signal decays, discussed in detail below.

The detector modeling uncertainty is sensitive to the following uncertainties determined from the data: the uncertainty in the tracking efficiency of $1.3 \%$ per track ( $2.0 \%$ per charged pion); the uncertainty in the charged-particle identification efficiency of $0.7 \%$ per electron, $1.6 \%$ per muon, $1.0 \%$ per kaon and $2.0 \%$ per pion; and the uncertainty in the reconstruction efficiency of $10 \%$ per
$K_{S}^{0}$ and $5 \%$ per $\pi^{0}$. The efficiency of the likelihood ratio cut to suppress combinatorial background is checked with the charmonium-veto sample and the level of discrepancy with the simulation is taken as the corresponding uncertainty. The fraction of signal cross-feed included in the signal Gaussian is studied with a parameterized Monte Carlo simulation technique and the uncertainty is set to correspond to the R.M.S. obtained for a large number of data-sized experiments (the uncertainty amounts to a variation of $\pm 100 \%$ of the number of signal cross-feed events included in the Gaussian).

The dominant source of uncertainty arises from modeling signal decays. Parameters of the Fermi motion model are varied in accordance with measurements of hadronic moments in semileptonic $B$ decays 17] and the photon spectrum in inclusive $B \rightarrow X_{s} \gamma$ decays [18. The fraction of exclusive $B \rightarrow K \ell^{+} \ell^{-}$and $B \rightarrow K^{*} \ell^{+} \ell^{-}$decays is varied according to theoretical uncertainties [1] and the corresponding systematic uncertainties are added linearly (i.e., we assume the uncertainties in the branching fraction for these two modes are fully correlated). The transition point in $m\left(X_{s}\right)$ between pure $K^{*} \ell^{+} \ell^{-}$and nonresonant $X_{s} \ell^{+} \ell^{-}$final states is varied by $\pm 0.1 \mathrm{GeV} / c^{2}$.

The nonresonant Monte Carlo event generator relies on JETSET to fragment and hadronize the system consisting of a final state $s$ quark and a spectator quark from the $B$ meson. Since the signal efficiencies depend strongly on the particle content of the final state, uncertainties in the number of charged and neutral pions and in the number of charged and neutral kaons translate into a significant uncertainty in the signal efficiency (for $m\left(X_{s}\right)>1.1 \mathrm{GeV} / c^{2}$ ).

The ratio between the generator yield for decay modes containing a $K_{S}^{0}$ and that for modes containing a charged kaon is varied according to $0.50 \pm 0.05$, to allow for isospin violation in the decay chain. The ratio between the generator yield for decay modes containing one $\pi^{0}$ and that for modes containing none is varied according to $1.0 \pm 0.5$. The ratio between the generator yield for decay modes into two-body hadronic systems and that into three-body hadronic systems is varied according to $0.5 \pm 0.3$. Uncertainties in the last two ratios are set by the level of discrepancy between data and Monte Carlo as measured in the BABAR semi-inclusive $B \rightarrow X_{s} \gamma$ analysis [19]. (Both $B \rightarrow X_{s} \gamma$ and present analyses use the same hadronization model.)

The ten modes selected in this analysis only capture about $50 \%$ of the full set of final states. Approximately half of the missing modes is due to final states with a $K_{L}^{0}$ meson and their contribution can be determined from the $K_{S}^{0}$ modes. However, we need to account for the uncertainty in the fraction of modes with too many pions or kaons (two extra kaons may be produced via $s \bar{s}$ popping), as well as for modes with photons that do not originate from $\pi^{0}$ decays but rather from $\eta, \eta^{\prime}, \omega$, etc. For final states with $m\left(X_{s}\right)>1.1 \mathrm{GeV} / c^{2}$, we vary these different fractions by $\pm 50 \%$.

Including systematic uncertainties, the measured branching fractions for $m\left(\ell^{+} \ell^{-}\right)>0.2 \mathrm{GeV} / c^{2}$ are

$$
\begin{align*}
\mathcal{B}\left(B \rightarrow X_{s} e^{+} e^{-}\right) & =\left(6.6 \pm 1.9_{-1.6}^{+1.9}\right) \times 10^{-6}  \tag{3}\\
\mathcal{B}\left(B \rightarrow X_{s} \mu^{+} \mu^{-}\right) & =\left(5.7 \pm 2.8_{-1.4}^{+1.7}\right) \times 10^{-6},  \tag{4}\\
\mathcal{B}\left(B \rightarrow X_{s} \ell^{+} \ell^{-}\right) & =\left(6.3 \pm 1.6_{-1.5}^{+1.8}\right) \times 10^{-6} \tag{5}
\end{align*}
$$

where the first error is statistical and the second error is systematic. The combined $B \rightarrow X_{s} \ell^{+} \ell^{-}$ branching fraction is the weighted average of the branching fractions for the electron and muon channels, where we assume the individual branching fractions to be equal for $m\left(\ell^{+} \ell^{-}\right)>0.2 \mathrm{GeV} / c^{2}$. Table 3 summarizes the results of the analysis and lists both the statistical and systematic errors in the signal yields, the signal efficiencies and the branching fractions.

Table 2: Summary of fractional systematic uncertainties (in \%). The uncertainties in extracting the signal are presented first and those related to the signal efficiency and $B \bar{B}$ counting are presented second.

| Source | $X_{s} e^{+} e^{-}$ | $X_{s} \mu^{+} \mu^{-}$ |
| :--- | ---: | ---: |
| Signal shape | $\pm 4.3$ | $\pm 2.5$ |
| Peaking background | $\pm 1.0$ | $\pm 5.8$ |
| Signal yield total | $\pm 4.4$ | $\pm 6.3$ |
| Tracking efficiency | $\pm 5.0$ | $\pm 4.8$ |
| Lepton identification efficiency | $\pm 1.3$ | $\pm 3.2$ |
| Kaon identification efficiency | $\pm 0.8$ | $\pm 0.8$ |
| $\pi^{ \pm}$identification efficiency | $\pm 1.5$ | $\pm 1.3$ |
| $K_{S}^{0}$ efficiency | $\pm 2.2$ | $\pm 1.9$ |
| $\pi^{0}$ efficiency | $\pm 0.8$ | $\pm 0.5$ |
| LR cut efficiency | $\pm 3.7$ | $\pm 3.3$ |
| Cross-feed efficiency | $\pm 6.7$ | $\pm 7.4$ |
| $\quad$ Detector model subtotal | $\pm 9.7$ | $\pm 10.2$ |
| Fermi motion model | ${ }_{-4.0}^{+10.2}$ | ${ }_{-3.6}^{+10.8}$ |
| $\mathcal{B}\left(B \rightarrow K \ell^{+} \ell^{-}\right)$ | $\pm 9.6$ | $\pm 12.6$ |
| $\mathcal{B}\left(B \rightarrow K^{*} \ell^{+} \ell^{-}\right)$ | $\pm 6.2$ | $\pm 6.8$ |
| $K^{*}-X_{s}$ transition | $\pm 3.3$ | $\pm 4.1$ |
| Hadronization | $\pm 11.1$ | $\pm 7.5$ |
| Missing modes | $\pm 10.6$ | $\pm 8.9$ |
| $\quad$ Signal model subtotal | ${ }_{-22.6}^{+24.5}$ | ${ }_{-23.3}^{+25.4}$ |
| Monte Carlo statistics | $\pm 2.5$ | $\pm 3.0$ |
| $B \bar{B}$ counting | $\pm 1.1$ | $\pm 1.1$ |
| Efficiency and $N_{B \bar{B}}$ total | ${ }_{-24.8}^{+26.5}$ | ${ }_{-25.6}^{+27.6}$ |

## 8 Summary

Using a sample of $88.9 \times 10^{6} \Upsilon(4 S) \rightarrow B \bar{B}$ events, we measure the branching fraction for the rare decay $B \rightarrow X_{s} \ell^{+} \ell^{-}$, where $\ell=e$ or $\mu$, with a sum over ten different hadronic states (with up to two pions). For $m\left(\ell^{+} \ell^{-}\right)>0.2 \mathrm{GeV} / c^{2}$, we observe a signal of $41 \pm 10$ (stat) $\pm 2$ (syst) events and obtain a branching fraction of

$$
\begin{equation*}
\mathcal{B}\left(B \rightarrow X_{s} \ell^{+} \ell^{-}\right)=\left(6.3 \pm 1.6(\text { stat })_{-1.5}^{+1.8}(\text { syst })\right) \times 10^{-6} \tag{6}
\end{equation*}
$$

with a statistical significance of $4.6 \sigma$. This preliminary measurement agrees well with the recent prediction by Ali et al. [1] and the measurement performed by the Belle Collaboration, $\mathcal{B}(B \rightarrow$ $\left.X_{s} \ell^{+} \ell^{-}\right)=\left(6.1 \pm 1.4(\right.$ stat $) \pm_{1.1}^{1.4}($ syst $\left.)\right) \times 10^{-6}$ for $m\left(\ell^{+} \ell^{-}\right)>0.2 \mathrm{GeV} / c^{2}[7]$.

Table 3: Summary of results: signal yield, statistical significance, efficiency and branching fraction. In the case of the signal yield and the branching fraction, the first error is statistical and the second error is systematic. In the case of the signal efficiency, the first error corresponds to uncertainties in detector modeling, $B \bar{B}$ counting, and Monte Carlo statistics, whereas the second error corresponds to the uncertainties in the signal model.

| Sample | $N_{\text {sig }}$ | Signif. | $\epsilon(\%)$ | $\mathcal{B}\left(\times 10^{-6}\right)$ |
| :--- | :---: | :---: | :---: | :---: |
| $X_{s} e^{+} e^{-}$ | $29.0 \pm 8.3 \pm 1.3$ | 4.0 | $2.46 \pm 0.25_{-0.56}^{+0.60}$ | $6.6 \pm 1.9_{-1.6}^{+1.9}$ |
| $X_{s} \mu^{+} \mu^{-}$ | $12.4 \pm 6.2 \pm 0.8$ | 2.2 | $1.23 \pm 0.13_{-0.29}^{+0.31}$ | $5.7 \pm 2.8_{-1.4}^{+1.7}$ |
| $X_{s} \ell^{+} \ell^{-}$ | $41.4 \pm 10.3 \pm 1.5$ | 4.6 | - | $6.3 \pm 1.6_{-1.5}^{+1.8}$ |

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