

# 3D Seepage under Hydraulic Structures Provided with Intermediate Filters

Ashraf Ahmed<sup>1</sup>, Shane McLoughlin<sup>2</sup>, and Harold Johnston<sup>3</sup>

<sup>1</sup> Lecturer, School of Planning, Architecture, and Civil Engineering, Queen's University Belfast, David Kier building, Stranmillis Road, Belfast BT95AG, UK

<sup>2</sup> Student, School of Planning, Architecture, and Civil Engineering, Queen's University Belfast, David Kier building, Stranmillis Road, Belfast BT95AG, UK

<sup>3</sup> Senior lecturer, School of Planning, Architecture, and Civil Engineering, Queen's University Belfast, David Kier building, Stranmillis Road, Belfast BT95AG, UK

## Abstract

Seepage flow under hydraulic structures provided with intermediate filters has been investigated. The flow through the banks of the canal has been included in the model. Different combinations of intermediate filter and canal width were studied. Different lengths of the floor, differential heads, and depths of the sheetpile driven beneath the floor were also investigated. It was found that the introduction of an intermediate filter to the floor of hydraulic structures reduced the uplift force acting on the downstream floor by up to 72%. The maximum uplift reduction occurred when the distance of filter location downstream the cutoff to the differential head ratio was 1. Introducing a second filter in the downstream side resulted in a further reduction in the exit hydraulic gradient and in the uplift force, which reached 90%. The optimum locations of the two filters occurred when the first filter was placed just downstream the cutoff wall and the second filter was placed nearly at the mid-distance between the cutoff and the end toe of the floor. The results showed significant differences between the three-dimensional (3D) and the two-dimensional (2D) analyses.

**Keywords:** Weirs; Regulators; Dams; Control structures; Mathematical modeling; Intermediate filters

## Introduction

Hydraulic structures are used to control the flow of water in rivers and canals. It is necessary to minimize the uplift pressures and hydraulic gradients beneath such structures to prevent

34 flotation, to ensure their structural stability, and to design against soil piping and consequent  
35 undermining of the structure. It is common to install cutoff walls beneath the floors of  
36 hydraulic strictures to reduce the seepage flow. In addition, intermediate filters are often  
37 provided in the floor of the structure as a further measure to reduce the uplift forces and exit  
38 hydraulic gradients. The effectiveness of these filters in reducing uplift forces has been  
39 analyzed using analytical methods.

40 Conformal mapping has been used to produce exact solutions for the problem of 2D seepage  
41 beneath a hydraulic structure with a flat floor having two end cutoffs and a filter located at  
42 various positions in the floor (Chawla 1975; Kumar et al. 1986). Elganainy (1986) presented  
43 a solution for the problem of seepage beneath two structures with intermediate filter built on  
44 two pervious strata. Hathoot (1986) used the Schwartz-Christoffel transformation to solve the  
45 problem of seepage beneath a concrete dam with a downstream filter.

46 The case of 2D seepage flow beneath a hydraulic structure provided with two intermediate  
47 filters was also studied using conformal mapping (Farouk and Smith 2000). Salem et al.  
48 (2001) used the Schwartz-Christoffel transformation to examine the stability of two  
49 consecutive floors with intermediate filter. The two consecutive floors represent a subsidiary  
50 weir constructed downstream of a barrage, a scheme which is equivalent to a physical  
51 situation resulting from the construction of subsidiary weirs downstream of barrages on the  
52 Nile river in Egypt.

53 Several studies conducted 3D numerical analysis to analyse the problem of seepage under  
54 hydraulic structures. Griffiths and Fenton (1997) studied 3D seepage through spatially  
55 random soil. The 3D results compared favorably with the 2D results for the same structure.  
56 More recently, Ahmed et al. (2007) studied the problem of 3D seepage under hydraulic  
57 structures with leakage through the sheetpiles. A limitation in these studies was that they  
58 have not considered the seepage flow through the canal banks. Studies carried out by Ahmed

59 and Bazaraa (2009) and Ahmed (2011) showed that neglecting the seepage flow through the  
60 banks of a canal resulted in errors in the seepage calculations.

61 The problem of 3D seepage beneath a hydraulic structure with a floor provided with an  
62 intermediate filter has not been investigated before. In this study, the effect of one and two  
63 intermediate filters on the development of uplift forces and exit hydraulic gradients at the  
64 downstream edge of a hydraulic structure has been analyzed. A number of analyses were  
65 carried out to investigate the effect of filter length, filter location and the introduction of a  
66 second filter on the development of uplift forces and exit hydraulic gradients. The analysis  
67 was carried out for various canal widths. Seepage through the canal banks was taken into  
68 account and the unsaturated flow above the free surface was considered.

### 69 **The Finite Element Model and the Analysis procedure**

70 The model deals with both confined and free surface flow problems. A detailed presentation  
71 of this computer program, and its validation and applications can be found in Ahmed (2008,  
72 2009). The program uses the model of van Genuchten (1980) to include the unsaturated  
73 flow.

74 Fig 1 illustrates an isometric view of the configuration studied; a hydraulic structure  
75 constructed upon a pervious homogeneous isotropic soil of depth 6m and hydraulic  
76 conductivity  $k=3 \times 10^{-5}$  m/s. The van Genuchten curve fitting parameters were taken  $\alpha = 14.5$   
77  $\text{m}^{-1}$  and  $n=2.68$ . The structure includes the floor, the side retaining walls and the structure  
78 built above the floor, all of which are considered to be impervious. A sheetpile cutoff driven  
79 to a depth of 4 m under the structure was represented. Different sheetpile depths were also  
80 investigated. The length of the modeled zone was 60 m and the upstream and downstream  
81 edges of the zone were considered to be impermeable. A differential head of  $H=1$  m between  
82 the upstream and downstream sides of the structure produced the seepage flow. The ratio of

83 the floor length to differential head  $L/H$  was 16. Other ratios of  $L/H=20$  and 24 were also  
84 investigated. The top of the banks was 2 m above the bed of the canal.

85 The finite element mesh used for the problem has a total of 10878 nodes and 9184 brick  
86 elements. Only one half of the problem was simulated because of its symmetry about the  
87 canal centerline. A 2D analysis was carried out on each case and the values of uplift forces  
88 and the exit hydraulic gradient acting on the downstream side of the structure were  
89 calculated. The problem was then studied in 3D for varying ratios of canal width to  
90 differential head  $W/H$  from 2 to 14. For each  $W/H$  ratio, scenarios of no filter, one filter, and  
91 two filters were analyzed. If  $x$  denotes the distance from the cutoff to the filter location (see  
92 Fig 1), the problem was studied for the ratio  $x/H$  varying from 1 to 6 for both the one and two  
93 filters scenarios. A comparison of the 2D and 3D results was carried out for each case.

## 94 **Results and Discussion of One Intermediate Filter**

### 95 **The Effect of the Filter Location**

96 Fig 2 presents different sections perpendicular to the canal centerline showing the free  
97 surface positions both upstream and downstream sides of the floor. As expected, the water  
98 flows out from the canal into the banks in the upstream side and then flows from the banks  
99 into the canal on the downstream side. It is therefore important to take the flow through the  
100 banks into consideration. Modelling this problem in 2D (e.g. Chawla 1975, Farouk and Smith  
101 2000) or in 3D without considering the flow through the banks has not provided accurate  
102 analysis that can be used in the design of the structure. The free surface at a distance of 10 m  
103 upstream and downstream of the structure was nearly flat.

104 Fig 3 presents the average uplift forces on the floor, when there was one filter, for different  
105 ratios of  $W/H$ . The filter location was measured from the sheet pile cutoff to the upstream  
106 edge of the filter. The uplift force shown in the figure is normalized relative to the case of no

107 filter in place. The introduction of a filter to the floor of the structure, regardless of its  
108 location, significantly reduced the uplift force developed under the floor. The smallest  
109 reduction in uplift force occurred when  $W/H=2$  where the reductions varied from 56% to  
110 33% as  $x/H$  varied from 1 to 6, respectively. As the ratio  $W/H$  increased, the potential for  
111 uplift reduction also increased. For  $W/H=14$ , the reduction in uplift force varied from 72% to  
112 35% as the ratio  $x/H$  varied from 1 to 6, respectively. For  $x/H=1$  to 2, only slight or no  
113 change was observed in the uplift force.

114 The greatest reduction in the uplift force occurred when  $x/H=1$ . This is because the uplift  
115 pressure is higher just downstream the cutoff than at any other point in the downstream side.  
116 The filter intercepts some of the streamlines and hence breaks the development of the uplift  
117 pressure. The above results in Fig 3 mean that placing a filter at this position will have a  
118 greater impact than at any other position.

119 Fig 4 presents the exit hydraulic gradients along the canal width for different filter locations.  
120 The exit hydraulic gradient calculated at the center of the canal was smaller than its value at  
121 the canal edge because of the water seepage through the banks. The water flows through the  
122 banks at a faster rate than below the structure. This is attributed to the existence of sheet pile  
123 below the floor that increases the travelling distance of the flowing water. Fig 4 shows again  
124 the importance of undertaking a 3D analysis of seepage problems since the exit hydraulic  
125 gradient obtained from the 2D analysis is that for the canal center. The 2D analysis also  
126 disregards seepage through the canal banks.

127 Fig 5 illustrates the impact the filter location had on the exit hydraulic gradient observed at  
128 the edge and at the centerline of the canal. All filter locations with  $x/H=1$  to 5 had little effect  
129 on the exit hydraulic gradient. A filter placed with  $x/H=6$  was found to further reduce the  
130 exit gradient. This happened both at the edge and at the center of the canal. However, the exit  
131 hydraulic gradient for all of these locations was reduced compared to the case of no filter in

132 place. The main reason for this reduction in exit gradient is because the filter intercepts some  
133 streamlines. Both the central and edge exit hydraulic gradients calculated using the 3D model  
134 were greater than the value obtained from the 2D model. As the W/H ratio increased from 2  
135 to 14, the central exit hydraulic gradient decreased and became comparable to the results of  
136 the 2D model.

### 137 **The Effect of Filter Length**

138 The effect of the filter length on the uplift pressure developed beneath the floor was analyzed  
139 using W/H ratios of 8 and 12. The filter length is taken as the dimension in the longitudinal  
140 direction of the canal. The results of this analysis are shown in Fig. 6. Increasing the length  
141 of the filter reduced the uplift force further; however the magnitude of this reduction was not  
142 significant when compared with the reduction produced from placing the filter in the  
143 downstream side.

144 Obviously, the existence of a filter, even with small length, is still able to break the  
145 development of the uplift pressure on the downstream floor. Hence, the increase in the filter  
146 length did not lead to a significant further reduction in the uplift force. These findings  
147 confirm those of Chawla (1975), and Farouk and Smith (2000). Increasing the filter length  
148 caused a small reduction in the exit hydraulic gradient at the edge and at the center of the  
149 canal.

### 150 **Different Depths of Sheetpile**

151 In addition to the 4 m deep sheetpile presented in Figs 3, and 5, a depth of the sheetpile cutoff  
152 of 2 m was tested for different locations of the intermediate filter. The percentage reductions  
153 in the exit gradient, and uplift force made by the filter for this case were similar to the  
154 percentage reductions made by the 4 m sheetpile. The only difference was that the absolute

155 values of the uplift force and the exit gradient obtained were slightly greater than the values  
156 obtained for 4 m deep sheetpile.

## 157 **Results and Discussion of Two Intermediate Filters**

158 The provision of a second filter to the floor of the structure reduced the uplift force beneath  
159 the floor significantly (Fig 7). The greatest reduction in the uplift force occurred when the  
160 two filters were located at  $x/H = 1$  and 4. For these two filter locations, the maximum  
161 reduction in the uplift force was 80% when  $W/H = 2$ . Increasing  $W/H$  to 14 led to reduction in  
162 the uplift force by 90%.

163 The optimum position of the filters downstream of the sheet pile cutoff changed as the floor  
164 length to differential head ratio  $L/H$  varied (Fig 8). When  $L/H$  was increased to 24, the  
165 optimum locations of the filters occurred at ratios of  $x/H$  of 1 and 5.

166 The downstream floor can be considered as three sections for analysis. Pore water pressure  
167 develops on the first section between the cutoff and the first filter. The first filter then  
168 intercepts some of the flow lines preventing the build-up of pore pressure along its length.  
169 Pore water pressure increases on the second section of the floor between the two filters. The  
170 second filter reduces the pore water pressure along its length and the pore water pressure  
171 increases again over the third section of the floor between the second filter and the  
172 downstream edge. The total pressure on the floor is less than the total pressure that is  
173 developed with either one or no filter in place.

## 174 **Comparison with 2D Results**

175 The uplift force calculated using the 3D model was comparable to its 2D value when  $W/H >$   
176 10 as shown in Fig 7. When  $W/H < 10$ , the uplift force resulting from the 3D model was  
177 greater than that obtained from the 2D solution. When  $W/H < 10$ , the seepage flow through  
178 the banks is significant compared to the flow beneath the floor, which is always reduced by

179 one or more rows of cutoff walls that are usually driven below the floor. This may be the  
180 reason behind the increased 3D uplift force for narrow canals.

181 In the 3D flow, the unsaturated flow through the banks may play a role in the difference  
182 between 2D and 3D results. For the 2D analysis of this problem, the flow is confined, and  
183 hence only saturated flow is considered. However, for the problem investigated in this  
184 research, the unsaturated flow was minimal. This may be attributed to the soil type used in  
185 the current analysis, or the fact that the free surface was only 1 m below the top level of the  
186 bank. The effect of unsaturated flow in 3D flow problems under hydraulic structures needs  
187 further investigations for different soil types, and different structures configurations.

#### 188 **Comparison between One- and Two-Intermediate Filters**

189 Table 1 shows the reduction in total uplift pressure for the one- and two-filters scenarios.  
190 When one filter was used, the total uplift force acting on the downstream floor was reduced  
191 by between 56% and 72% compared with the uplift experienced when no filter was provided.  
192 As the W/H ratio increased the potential for uplift reduction increased. The introduction of a  
193 second filter to the floor reduced the uplift forces further. When both filters were positioned  
194 at their optimum locations the total uplift force acting on the downstream side of the floor  
195 was reduced by between 80% and 90% of the uplift forces calculated in the ‘no-filter’  
196 scenario. This represents a further 25% decrease in uplift force when compared with the ‘one-  
197 filter’ scenario.

198 The edge and central exit hydraulic gradient from the one- and two-filters scenarios are  
199 compared in Fig 9. The maximum reduction in the exit hydraulic gradient occurred when the  
200 filters were located at  $x/H = 2$  and 6. When one filter was introduced, the exit gradient was  
201 reduced by between 41% and 45% at the canal edge, and by 50% to 65% at the center of  
202 canal for W/H ratios of 2 to 14, respectively. The introduction of a second filter reduced the



203 edge exit hydraulic gradient by 50% to 73% for  $W/H$  ratios of 2 to 14, respectively. The  
204 central exit hydraulic gradient was reduced by between 57% and 81% when two intermediate  
205 filters were introduced to the floor of the structure. The reduction in exit gradient at the canal  
206 center is greater than the reduction at the canal edge. This can be attributed to the flow  
207 through the canal banks that makes the exit gradient at the canal edge less sensitive to the  
208 provision of intermediate filter in the floor, particularly when the ratio  $W/H$  was small, i.e.  
209 for narrower canals.

## 210 **Differential Heads**

211 The previous results were based on the differential head  $H= 1$  m. A second value of the  
212 differential head  $H= 2$  m was tested for the case of ‘one-filter’ when  $W/H=10$ . The results are  
213 presented in Table 2, which shows both the uplift force and the exit hydraulic gradient at the  
214 canal edge. The effect of different filter locations for  $H=2$  m on uplift force and exit hydraulic  
215 gradient remained the same as in the case  $H=1$  m. A small increase of about 3% in the exit  
216 hydraulic gradient occurred when  $H=2$  m compared to when  $H=1$  m. This may be attributed  
217 to the nonlinearity of the problem caused by the unconfined flow through the banks.  
218 However, the influence of the filter location remained the same for different values of  $H$ .

## 219 **Conclusions**

220 2D and 3D analyses were carried out to study the effect of intermediate filters on the  
221 development of downstream uplift force and exit hydraulic gradient beneath floors of  
222 hydraulic structures. A number of variables were investigated including filter location, filter  
223 length, and the number of filters introduced to the floor of the structure. Results have been  
224 obtained for varying ratios of canal width to differential head, and different ratios of floor  
225 length to differential head.

226 The use of one filter reduced the uplift forces developed beneath the floor of the structure.  
227 The optimum location of the filter occurred when  $x/H=1$ , and reductions in uplift force of  
228 between 55% and 72% were recorded. The reduction in uplift force increased as the canal  
229 width increased. Increasing the length of the filter reduced the uplift force; however, this was  
230 small in comparison to the reduction experienced due to the introduction of an intermediate  
231 filter.

232 The introduction of a second intermediate filter in the floor of the structure decreased both  
233 the uplift pressure and exit hydraulic gradients. When the two filters were positioned such  
234 that  $x/H=1$  and 4, maximum reductions in uplift force of between 80% and 90% were  
235 obtained. It is recommended that to maximize the reduction of the uplift force, the first filter  
236 should be located just downstream of the cutoff and the second should be positioned half way  
237 between the cutoff and the downstream end of the floor.

238 The maximum reduction in exit hydraulic gradient occurred when the two filters were located  
239 at  $x/H =2$  and 6. The introduction of a second filter reduced the edge exit hydraulic gradient  
240 by 50% to 73% for W/H ratios of 2 to 14, respectively. The central exit hydraulic gradient  
241 was reduced by between 57% and 81% when two intermediate filters were introduced to the  
242 floor of the structure.

243 Differences between the results calculated using the 2D and 3D analyses were identified.  
244 These differences occur because the 2D analysis does not consider seepage flow through the  
245 canal banks. If the increases in uplift pressure and exit hydraulic gradients are neglected at  
246 the design stage, it may result in the structure being under-designed and unstable. Results of  
247 the 2D and 3D models were found to be comparable only when the canal width to differential  
248 head ratio was greater than 10.

249 **Acknowledgments**

250 The authors would like to thank the anonymous reviewers for their constructive comments  
251 that helped improve the manuscript of this paper.

## 252 **References**

- 253 1. Ahmed, A. A. (2008). "Saturated-unsaturated flow through leaky dams." *J. Geotech.*  
254 *Geoenviron. Eng.*, 134(10), 1564-1568.
- 255 2. Ahmed, A. A. (2009). "Stochastic analysis of free surface flow through earth dams."  
256 *Comput. Geotech.*, 36(7), 1186-1190.
- 257 3. Ahmed, A. A. (2011). "Design of hydraulic structures considering different sheetpile  
258 configurations and flow through canal banks." *Comput. Geotech.*, 38(4), 559-565.
- 259 4. Ahmed A A, Soliman A M, Bazaraa A S (2007) 3-D steady analysis of leaky hydraulic  
260 structures: 1. Leaky sheetpiles. *J of Eng. Appl. Sci.* 54(2): 141-157.
- 261 5. Ahmed, A. A., and Bazaraa, A. S. (2009). "Three-dimensional analysis of seepage  
262 below and around hydraulic structures." *J. of Hydrol. Eng.*, 14(3), 243-247.
- 263 6. Chawla, A S (1975). "Stability of structures with intermediate filters." *J Hydraul. Div.*,  
264 101(2), 223-241.
- 265 7. Elganainy M (1986). "Flow underneath a pair of structures with intermediate filters on  
266 a drained stratum." *Appl. Math. Model.*, 10(6), 394-400.
- 267 8. Farouk, M I, and Smith I M (2000). "Design of hydraulic structures with two  
268 intermediate filters." *Appl. Math. Model.*, 24, 779-794.
- 269 9. Griffiths, D. V., and Fenton, G. A. (1997). "Three-dimensional seepage through  
270 spatially random soil." *J. Geotech. Geoenviron. Eng.*, 123(2), 153-160.
- 271 10. Hathoot H M (1986) Seepage beneath a concrete dam with a downstream filter. *Appl.*  
272 *Math. Model.* 10(2), 129-132.
- 273 11. Kumar A, Singh B, and Chawla A S (1986). "Design of structures with intermediate  
274 filters." *J Hydraul. Eng.* 112(3), 206-219.
- 275 12. Salem, A S, and Ghazaw Y. (2001). "Stability of two consecutive floors with  
276 intermediate filters." *J Hydraul. Res.*, 39(5), 549-555.
- 277 13. van Genuchten M Th (1980). "A closed-form equation for predicting the hydraulic  
278 conductivity of unsaturated soils." *Soil Sci. Soc. Am. J.*, 1980, 44, 892-898.
- 279

280 **Figures Captions**

281

282 Fig 1. 3D view and cross section of the configuration studied

283 Fig 2. Free surface at different sections perpendicular to the canal centerline ( $W/H=10$ )

284 Fig 3. Effect of filter location on the downstream uplift force for different widths of the canal.  
285 The uplift force is normalized to the case of no filter in place.

286 Fig 4 Change of the exit gradient along the canal width. The exit hydraulic gradient is  
287 normalized to the case of no filter in place ( $W/H=10$ ).

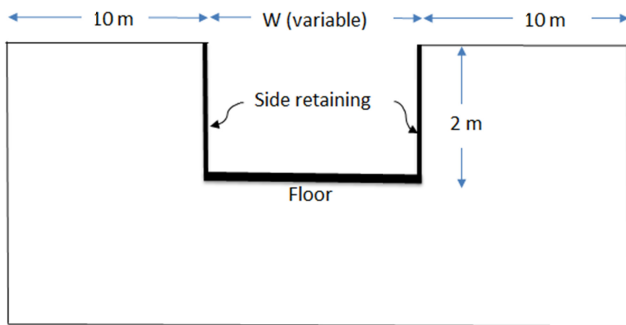
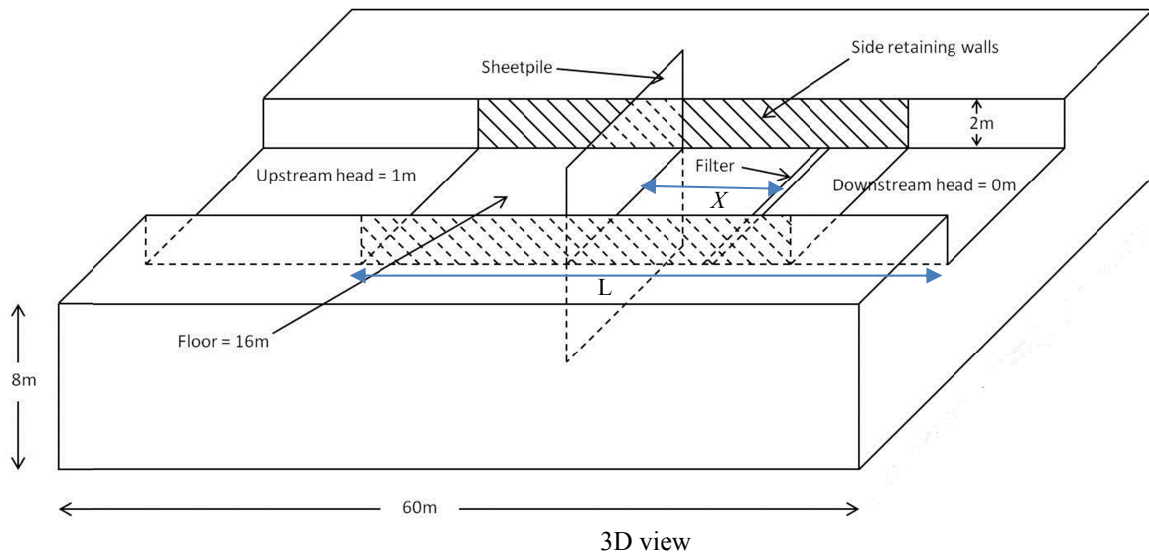
288 Fig. 5. Effect of filter location on the exit hydraulic gradient for different widths of the canal.  
289 The exit gradient is normalized to the case of no filter in place.

290 Fig. 6. Effect of filter length on uplift force. The uplift force is normalized to the case of no  
291 filter in place.

292 Fig. 7. Effect of introducing a second filter on uplift force developed beneath the floor of the  
293 structure.

294 Fig. 8. Reduction in uplift force for various filters locations and varying floor length.

295 Fig.9. Reduction in the exit hydraulic gradient for one- and two-filter scenarios (one filter  
296  $x/H=6$ ; two filters  $x/H= 2\& 6$ ).



Cross section through the canal

Fig 1

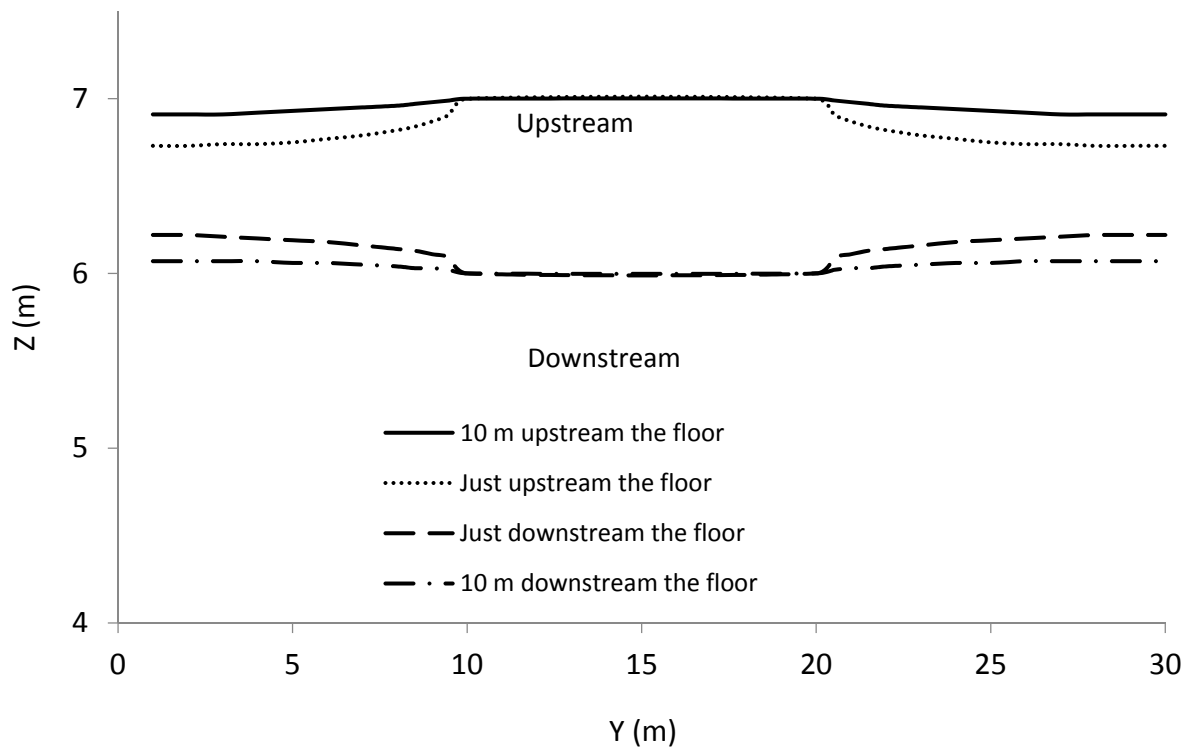


Fig 2

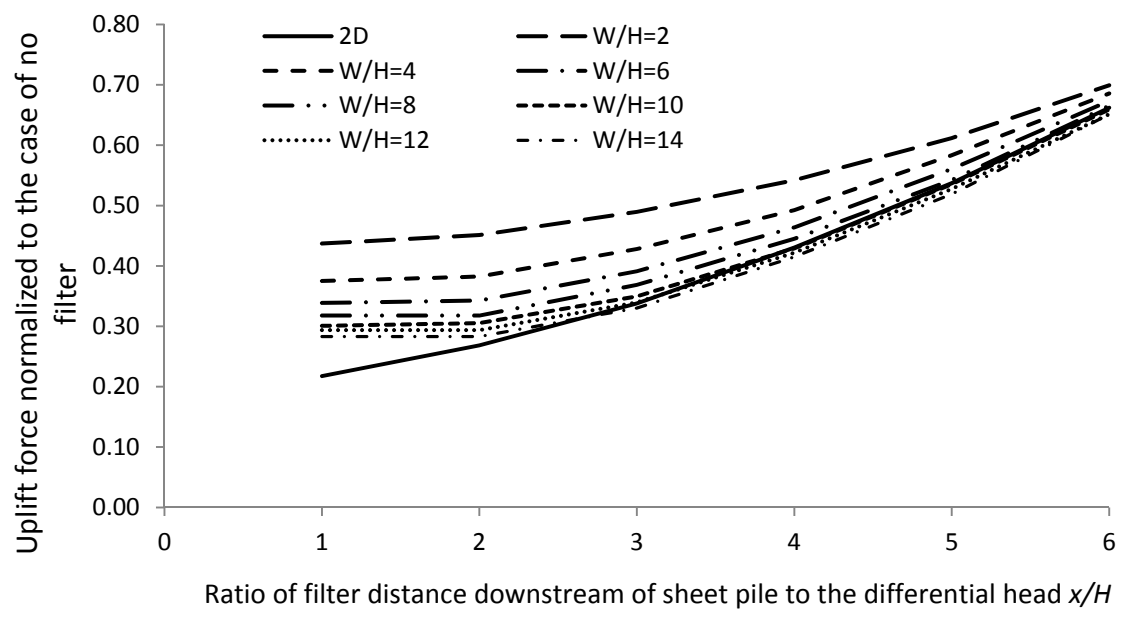


Fig 3

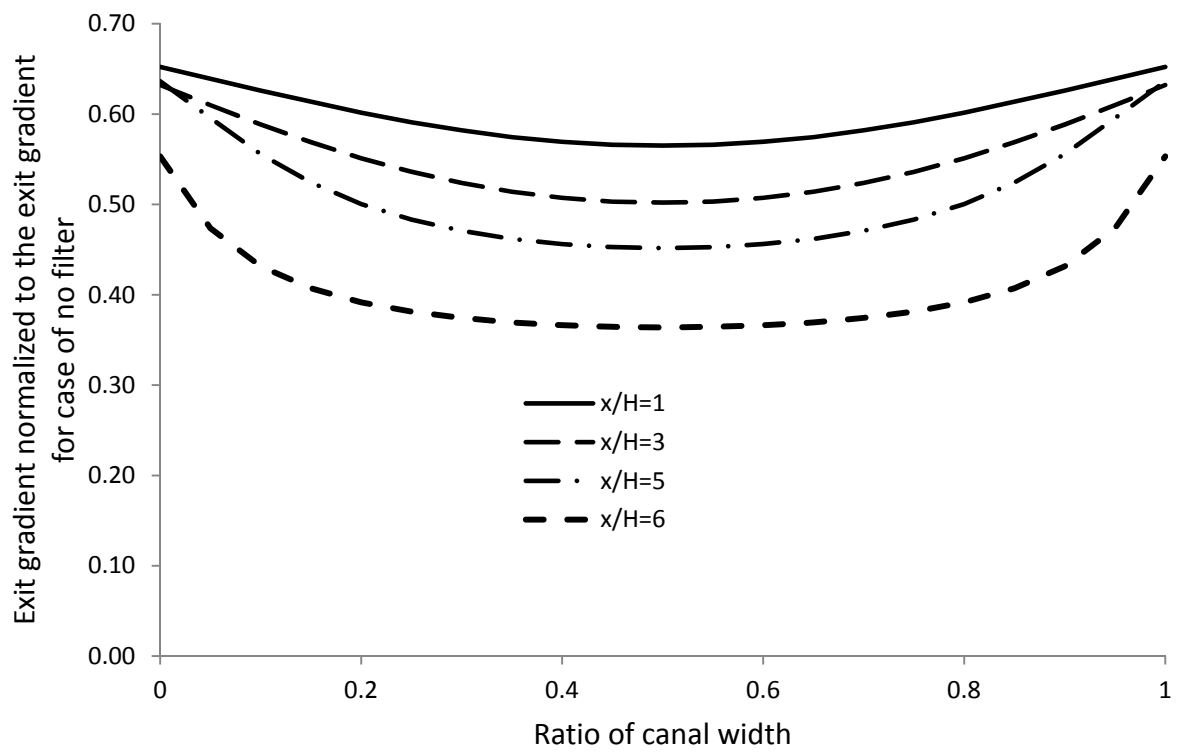


Fig 4



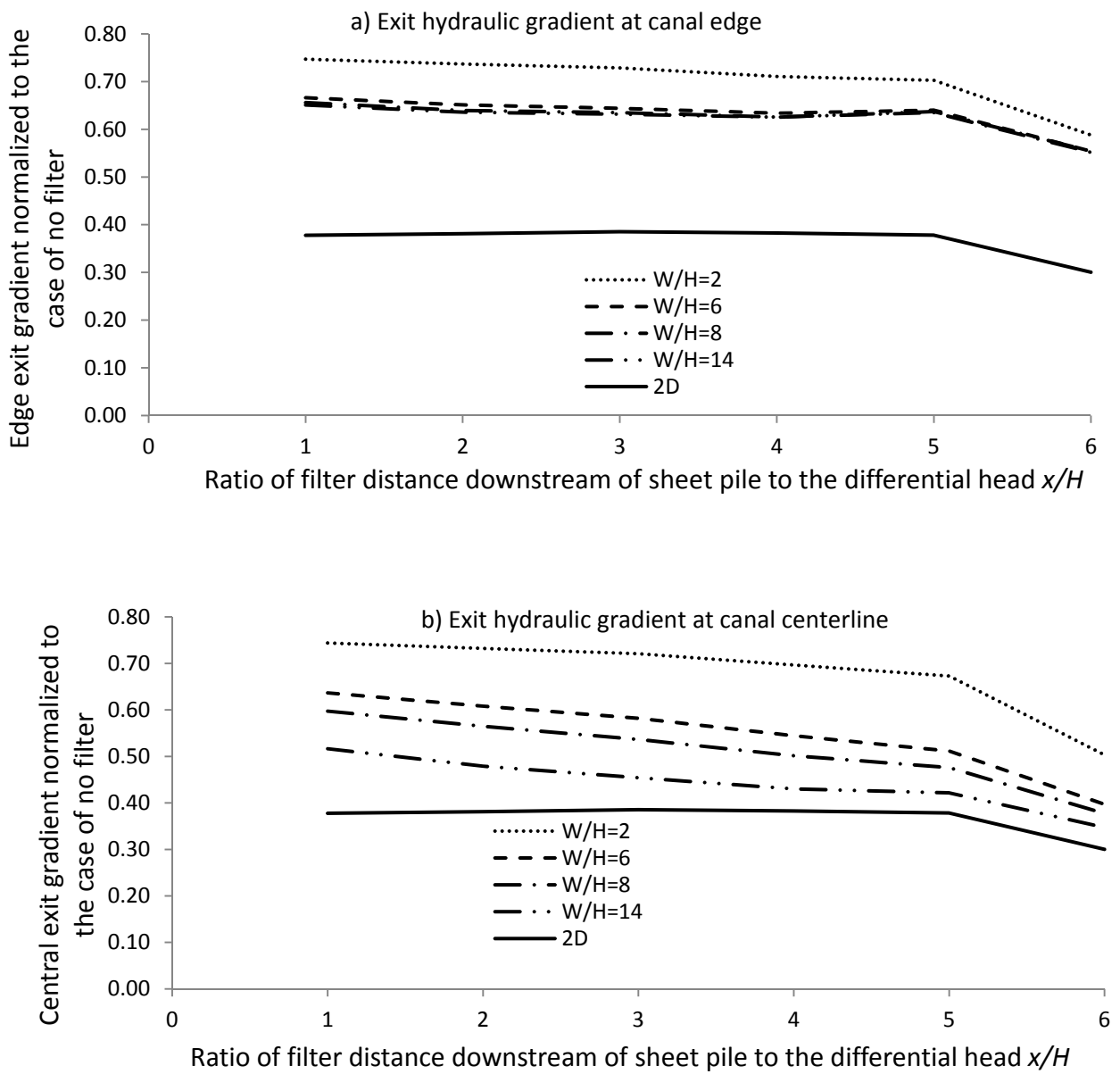


Fig 5



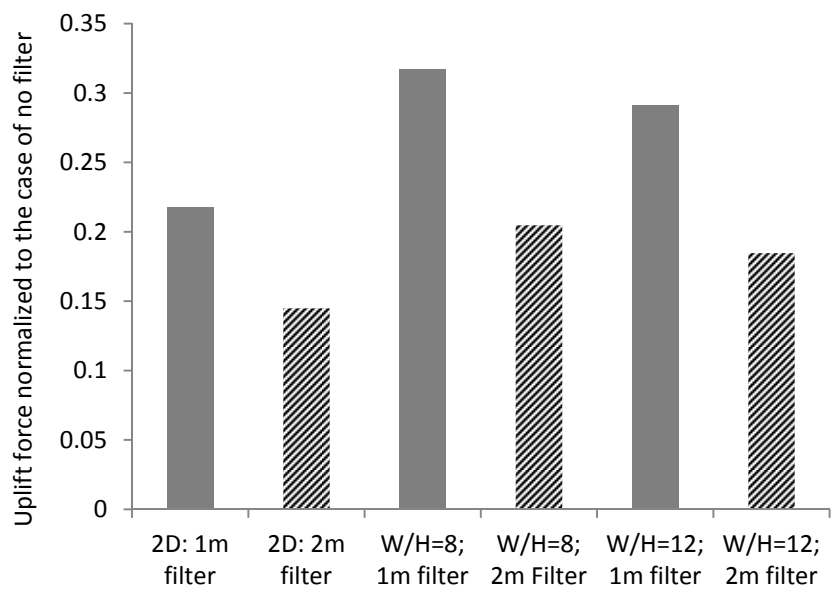


Fig 6

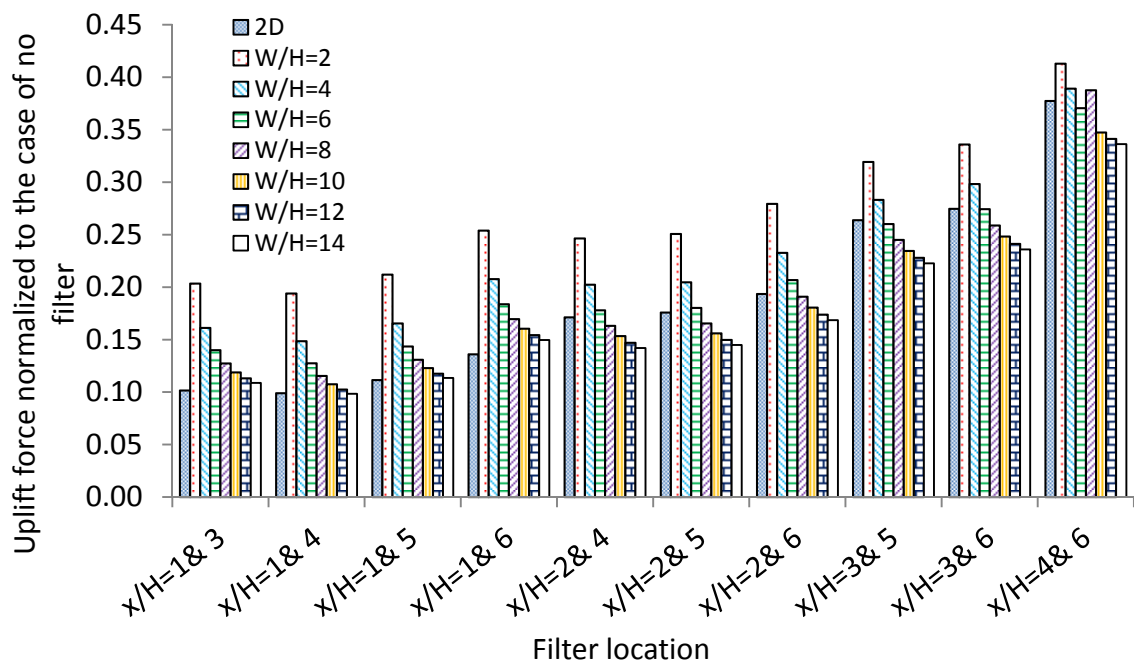


Fig. 7

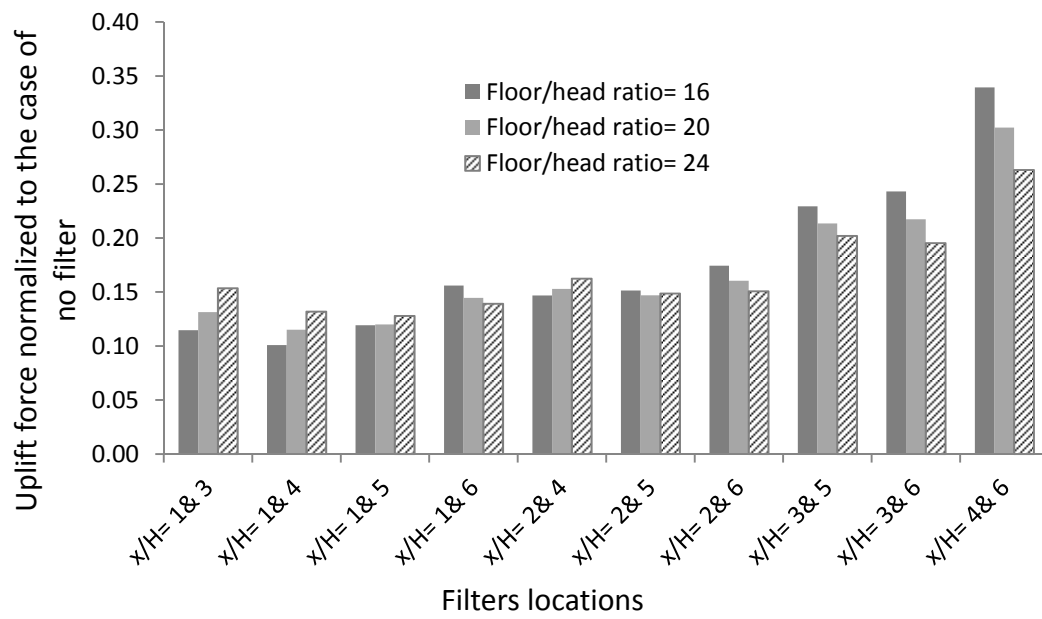
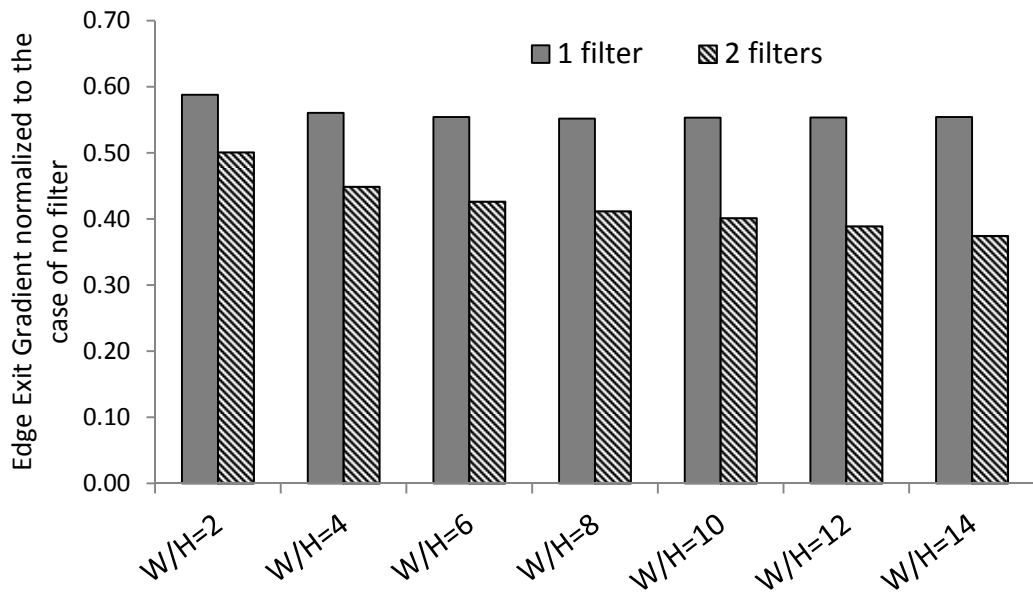
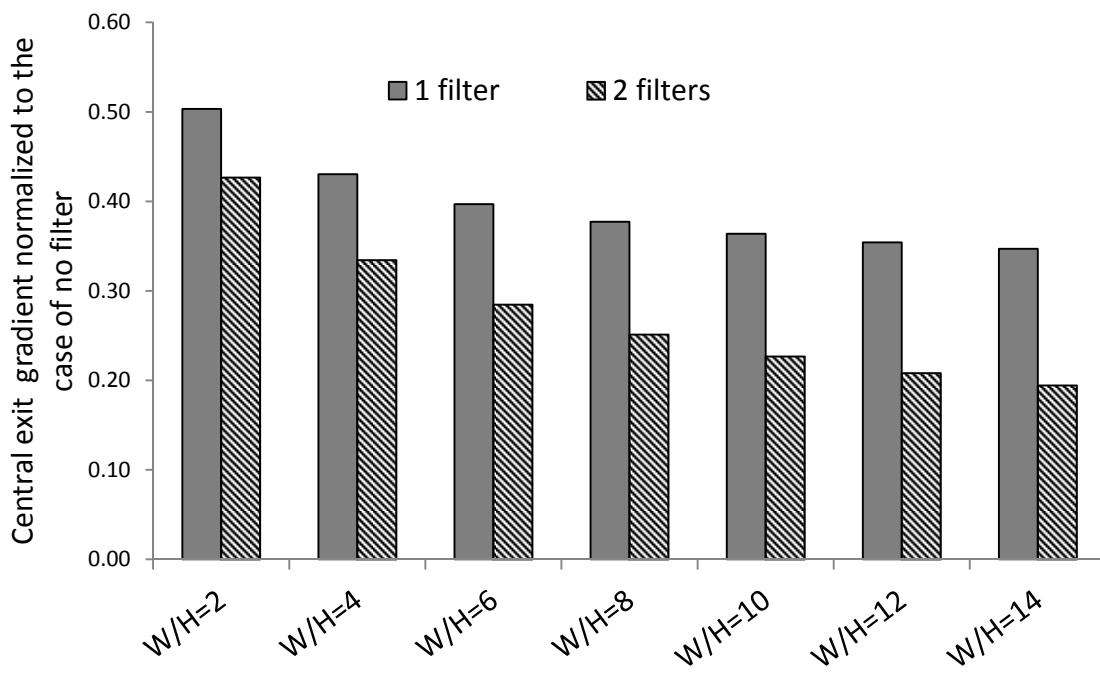


Fig. 8



a) At canal edge



b) At canal centerline

Fig 9

Table 1. Downstream uplift force for cases one filter located at  $x/H = 1$ , and two filters located at  $x/H = 1$  & 4 for different ratios of  $W/H$ .

Canal width/ differential head ratio	Downstream total uplift force normalized to the case of no filter		Percentage (%) total uplift reduction using one filter	Percentage (%) total uplift reduction using two filters
	1 filter	2 filters		
$W/H=2$	0.44	0.20	56.3	80.4
$W/H=4$	0.38	0.15	62.5	85.2
$W/H=6$	0.34	0.13	66.1	87.1
$W/H=8$	0.32	0.11	68.2	88.6
$W/H=10$	0.30	0.11	69.9	89.4
$W/H=12$	0.29	0.10	70.6	89.9
$W/H=14$	0.28	0.10	71.7	90.1

Table 2. Uplift Force and Exit gradient at the canal edge for different filter locations and two different differential head. The uplift force and exit gradient are normalised to the case of no filter in place.

Filter distance $x/H$	Uplift force		Exit gradient	
	H=1m	H=2m	H=1m	H=2m
1	0.30	0.30	0.64	0.67
2	0.31	0.30	0.64	0.67
3	0.35	0.35	0.64	0.67
4	0.43	0.43	0.64	0.67
5	0.54	0.53	0.64	0.67
6	0.66	0.66	0.55	0.58