# Impact of Hybrid Distributed Generation Allocation on Short Circuit Currents in Distribution Systems 

# A thesis submitted for the degree of Doctor of Philosophy 

## By

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#### Abstract

The rapid development in renewable generation technologies and flexible distribution networks requires current infrastructure to be modified and developed to adapt high penetration levels of distributed generation. Existing distribution networks were not initially designed and anticipated to accommodate generators on large scale. Short circuit studies ensure the effectiveness of protection equipment settings and coordination is maintained in case of short circuit, despite any additional distributed generation is connected to the distribution network. This research aims to study and compare the different network fault situations for wind energy systems with induction generators, photovoltaic energy systems, and diesel generators connected to distribution networks. The simulation study will be conducted on the existing IEEE case study systems including 13 bus and 30 bus distribution test systems, using ETAP software. Short circuit analysis will be performed twice to include the ANSI/IEEE and the IEC methods for short circuit currents calculation. Simulated results showed that the wind energy systems have significant impact on the short circuit currents, whereas the photovoltaic energy systems are found to have inconsequential effect. The most moderate solution is found to be a distributed generation mix.


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## Declaration of Authorship

The work described in this thesis has not been previously submitted for a degree in this or any other university and unless otherwise referenced it is the author's own work.

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## List of Abbreviations

|  |  |
| :--- | :--- |
| 3-PH/3-ph | Three-Phase |
| AC | Alternating Current |
| ANSI | American National Standard Institute |
| DC | Direct Current |
| DFIG | Doubly Fed Asynchronous Generators |
| DG | Distributed Generation |
| DR | Distributed Resources |
| EPS | Electrical Power Systems |
| ETAP | Electrical Power System Analysis |
| HV | High Voltage |
| IEC | International Electrotechnical Commission |
| IEEE | Institute of Electrical and Electronics Engineers |
| LG | Line to Ground |
| LL | Line-to-Line |
| LLG | Line-to-Line to Ground |
| LV | Low Voltage |
| MCFC | Molten Carbonate Fuel Cell |
| MV | Medium Voltage |
| OC | Over Current |
| PAFC | Phosphoric Acid Fuel Cell |
| PCC | Point of Common Coupling |
| PEMFC | Proton Exchange Membrane Fuel Cell |
| PV | Photovoltaic |
| R/X | Shoristance to Reactance ratio |
| SCC | Squirrel-Cage Induction Generator Turrent |
| SCIG | Verband Deutscher Electrotechniker Generators |
| SOFC |  |
| VDE |  |

## Chapter One

## 1 Introduction

### 1.1 Background

With BREXIT and new global political agenda's coming in place, countries will begin to change their energy policies to ensure energy security. Energy security implies diversified energy supply and independency. This means that countries should rely on their own resources and harvest their energy potentials. At the same time, the environmental target of reducing carbon dioxide emissions still exists. This would be considered as an extra burden for energy policy makers and decision makers to determine new solutions and set new legislations to inhabit the new policies. This implies countries to generate more energy to meet the increase in demand from their own resources either renewable or non-renewable. Though, the uptake for renewable energy should be more than non-renewable to meet the reduction in carbon dioxide emissions target. This will increase the uptake of renewable energy systems and encourage the deployment of variable renewable energy mix such as wind, photovoltaics, and hydro on a large scale. In the EU, it is expected that the renewable energy generation mix will be almost double the current generation capacity by 2020 and will reach around $30 \%$ in 2030 [1], [2]. This raises a significant question, apart from the economical and energy markets capabilities; are the technologies technically (such as mechanical, electrical, and civil) mature and available to accommodate this boost [2]. Electrical power systems have three major consequential pillars generation, transmission, and distribution. As renewable sources are not always available to be centralised to generate bulk capacities of electricity, therefore, the interest in decentralised generation is becoming more enviable. The traditional concept of generating electricity from one centralised power station to be transmitted miles away to distribution network and then to customer is no longer the single arrangement of electricity production and transfer.

Currently, the electrical power is generated at the consumer side or distribution level. This type of generation is known as Distributed Generation (DG).

### 1.2 Distributed generation definition

Distributed generation is considered as a new approach did not exceed the two decades. Initially, there are several terms used to describe this initiative in literature and in different countries. These terms are Embedded Generation commonly used in Anglo-American countries; dispersed generation in North American countries; and decentralised generation in Europe and parts of Asia [5].

The most common general definition used in the literature for Distributed Generation is proposed by [5]: "DG is an electric power source connected directly to the distribution network or the consumer side of the meter" [5]. The type of power source may include both, renewable and non-renewable energy sources such as Wind, solar, and diesel generators. DG rating has no maximum permissible limit; it may vary from few watts up to hundreds of megawatts, depending on distribution network capacity, which is correlated to the voltage level within the distribution system [2], [5]. Different DG ratings range as follows [5] :

Micro distributed generation $\sim 1$ Watt -5 kW
Small distributed generation $\sim 5 \mathrm{KW}-5 \mathrm{MW}$
Medium distributed generation $\sim 5$ MW-50 MW
Large distributed generation ~ 50 MW - 300 MW

### 1.2.1 Motivations for DG integration

According to International Energy Agency (IEA), there are five main factors significantly increased distributed generation importance, which are as follows [4]:

1. Development in DG technologies
2. Constraints on construction of new transmission lines
3. Increased load demand for highly reliable electricity
4. Electricity market liberalization.
5. Climate change mitigation.

### 1.2.2 Advantages of distributed generation

1. Provides electrical supply to remote areas, where it may be more economical than establishing a new transmission and distribution systems [91]
2. Regulates the voltage profile of distribution networks that suffered poor voltage levels before the penetration of DG at peak loads scenarios [91]
3. Improves the distribution network losses, which in return benefits the Distribution Network Operators costs [91]
4. Reduces the loading on the main feeder [91]
5. Acts as a backup power supply in case of main supply failure, especially for the sensitive loads such as hospitals
6. DG based on renewable energy sources mitigates climate change [74].
7. In some developing countries, DG may improve population economy, such as in Pakistan, where consumers are encouraged to install DG to meet their load demands and to reduce their electricity bills by selling that electricity to utility [74]
1.2.3 Disadvantages of distributed generation
8. DG integration causes the change of power flow from being uni-directional to bi-directional. This feature interferes with the normal operation of distribution networks.
9. DG alters the short circuit level when it is connected to a network, which affects the network protection scheme.
10. Improper allocation and penetration level of DG may lead to increased power losses; undesirable voltage profile; and stability issues [92], [93]
11. In renewable energy-based DG such as PV and wind, the output power is intermittent due to the variable nature of the renewable energy source sun and wind [92].
12. Some DG sources may cause voltage flicker such as in Wind [92].
13. DG may inject harmonics into the distribution system [89].
14. In DG integration, islanding may occur. This is a condition in which a portion of the utility system that contains both load and DG remains energized while isolated from the remainder of the utility system. Meanwhile, a DG may be feeding a short circuit [92].

DG is classified by the type of technology that interfaces with the distribution system such as power electronics inverters, and rotating machines including induction generators, squirrel cage generator, and synchronous generators. The characteristics of different types of interface are distinguished by their impact on the distribution system short circuit current, voltage control, and potential contribution to harmonic distortion [3].

The presence of DG in distribution systems alters the conventional theory of the flow of power in one-direction. Some existing distribution networks are not designed to accommodate more DG [5]. The connection of DG to the distribution systems remains a constraint in the power distribution planning. The DG capacity limits; total DG capacity penetration level; DG capacity reserve; and short circuit current limit are considered from the major factors affecting the power distribution planning, when it comes to DG integration [6]. Moreover, there are technical aspects inhibiting the implementation of DG on a large scale such as voltage control; fault level; grid protection; power quality; and power losses [7], [8].

It is essential to perform a technical evaluation study to evaluate the impact of the interconnection of a particular DG in order to determine the most efficient DG to be connected, to avoid unnecessary implications. The evaluation study requires understanding the type and size of DG under consideration, system limitations at the proposed location of the DG, and the expected mode of operation and monitoring techniques that will be available to distribution networks operators [3].

DG may interfere with protection coordination if it contributed more than 10\% [3] of the circuit's maximum fault current at the primary voltage at the point of common coupling. Increased fault currents may exceed existing equipment ratings, interrupting current ratings, which may lead to potential mis-coordination of existing protective devices. Therefore, further system protection studies should be performed [3].

The main objective of system protection studies is to ensure that the reliability of electrical system and the effectiveness of the protection devices settings and coordination are maintained during fault conditions despite the interconnection of additional generation sources to the distribution system [3].

Protection studies require comprehensive advanced studies involving load flow and short circuit studies to provide the fundamental essential data for analysing the impact of DG on the distribution system considered under different fault considerations and pre-fault conditions. This implies the modelling of the distribution circuit with proposed DG in a short circuit study computer program and different short circuit simulations to be performed in order to determine the short circuit current levels for appropriate protection coordination and relay settings [3].

The increasing exploitation of DG units has a significant impact on the short circuit currents and the short circuit level of the distributed systems. Therefore, the introduction of DG will to lead to a change in the short circuit current. Consequently, this will affect the existing overcurrent protection scheme, which in return may have a significant influence on the power system reliability. Hence, a redesign to the fault protection system will be needed [5], [7], [9]. The impact of DG depends on several factors such as DG size, penetration level, DG location, the technology of DG used, its operation mode, interface of the DG (type of generator connected), system voltage prior fault, location of fault, and type of fault. Therefore, it is essential and recommended to examine the contribution of each DG unit installed [9]. The safest way to assess the impact of DG on fault current level and the relay protection scheme of the distribution network is to model the grid with DG and to simulate different scenarios with different operating conditions [7].

The short circuit study should provide accurate results for reliable analysis and consistent coordination of relay settings. It requires very detailed models representing the system components dynamic behaviour. International committees as ANSI/IEEE and IEC provide simplified procedures as reference methods for short circuit calculations. Electrical power systems simulation software's have adopted these authorized methods to precisely simulate short circuit currents [10]. However, there is lack of evidence of which procedure could be adopted to examine the impact of DG on short circuit currents.

Wind and solar PV are the renewable energy sources that will be examined in this study. The wind and PV are the fastest growing sources of electricity generation worldwide, meeting more than $90 \%$ of incremental demand for electricity in 2015. Also, their average land cost is decreasing. Between 2008 and 2015, the average cost
of land for wind decreased by $35 \%$ and that of PV by approximately $80 \%$ [11]. These two technologies have been shifted from the phase where main priorities are technology learning and cost reduction to the phase of technologically mature and economically liable [11].

The future trend in electricity generation is deploying a mix of technologies. It is found to have several valuable synergies such as the current technology mix (wind and PV ) in Germany that is able to provide an overall more stable generation profile. Also, the variable output of wind and PV can be used in conjunction with other renewable resources and energy storage to offer integrated packages [11].

The fast-growing deployment of wind and PV has created significant challenges to the power systems planning, operation, and stability. The variable availability of daylight and wind leads to non-continuous generation, in which the system may not be flexible enough to adopt fluctuated output power. This affects the system stability and reliability. Furthermore, the interface of power converters technology between the grid and wind and PV is still uncertain [11]. Therefore, further investigations are still needed to determine the influence of deploying high penetration levels of wind and PV on the power systems operation in particular distributed systems.

### 1.3 Aim and objectives

The main aim of this research is to investigate the impact of wind, PV , and their mix including diesel generators on the short circuit current in electrical distribution network using different calculation methods such as IEEE/ANSI and IEC.

The objectives are:
a- To simulate and analyse a short circuit study for the IEEE 13-bus and IEEE 30-bus distribution test systems.
b- To investigate the impact of DG type on the short circuit current.
c- To investigate the impact of DG location on the short circuit current.
d- To investigate the impact of DG penetration level on the short circuit current.
e- To perform a load flow study to investigate the proper locations of DG to determine the key scenarios under study.
f- To investigate the key difference in short circuit calculations using IEEE/ANSI and IEC methods.

### 1.4 Methodology

The methodology applied in this research is simulation and analysis. The IEEE 13bus distribution test system and 30 -bus system are the two distribution systems selected to investigate the impact of DG penetration on their short circuit currents respectively. The choice for selecting a distribution system to study was not a straightforward task. The most appropriate preference is usually a real existing network. However, for this research, this opportunity was not available. Therefore, the most viable accessible data for approved distribution system models which are based on actual distribution circuits that were found are the IEEE distribution test systems.

The IEEE PES distribution system analysis subcommittee has several radial test feeders and common set of data available. The main purposes of these test feeders are to evaluate and benchmark algorithms in solving unbalanced three-phase radial systems [12].

The test feeders are classified by number of buses available in the circuit. The range of test feeders starts from the smallest as 4 buses up to 132 buses and even more for low voltage networks. The criteria for selecting the test distribution systems to study came from the prospect of examining the impact of DG on small system and large system so as to have substantial results and analyses for reliable conclusion. The two systems selected were the 13 bus and the 30 bus systems. Further details of different scenarios considered will be presented.

The computer software used for simulation in this research is Electrical Power System Analysis (EATP). ETAP is advanced software used by reputable research institutes and industry corporations for power system modelling, design, analysis, optimization, control, and automation. ETAP provides the most comprehensive unbalanced short circuit module for unbalanced fault simulation based on ANSI, IEC and GOST standards. Furthermore, the software includes comprehensive renewable energy models that are fully integrated with power system analysis calculations including load flow, short circuit, transient stability, and ETAP Real-Time solutions, for accurate simulation, predictive analysis, and equipment sizing.

Different types of photovoltaic array elements and wind turbine models are included in the ETAP renewable energy models. For the photovoltaic modelling, unlimited number of solar panels individually or in groups could be modelled in series and/or parallel connection combinations to form the required solar array with built-in inverter model. The effect of variable performance coefficients such as solar irradiance and cell temperature is considered and capable of automatically recalculating the power output from the photovoltaic array [13]. However, in this study this feature is not considered. A constant solar irradiance and cell temperature are assumed. Similarly, for wind turbine modelling, detailed modelling of turbine dynamics including aerodynamics and power coefficients is included with the option of simulating transient wind conditions with ramp, gust, and noise disturbances. Though, the aerodynamics and power coefficients for this study are assumed to be constant.

The distribution systems are modelled and modified by integration of different scenarios for wind, PV, Wind and PV, and Wind, PV, and diesel generators in ETAP. The short circuit study is run twice to consider ANSI and IEC methods respectively. Simulation results from short circuit studies are collected and entered into Microsoft Excel for generation of figures and further calculations of percentages. These results are then analysed in depth and presented in chapters five and six, where discussion and conclusions are provided.

### 1.5 List of publications conducted from this PhD

The research conducted in this PhD has resulted in the publication of a list of refereed publications as follows:

International Conferences publications

- S. N. Afifi, and M. K. Darwish, "Impact of PV/Wind/Diesel Hybrid System on the Distribution Networks - Fault Currents," in International Conference of Renewable Energy and Power Quality, ICREPQ 2016, Madrid, Spain, May 4-6, 2016.
- S. N. Afifi, and M. K. Darwish," Impact of Hybrid Renewable Energy Systems On Short Circuit Levels in Distribution Networks," 2014 49th International Universities Power Engineering Conference, UPEC2014, Cluj-Napoca, Romania, September 2-5, 2014.
- S. N. Afifi, M. K. Darwish, and G. A. Taylor. "Impact of Photovoltaic Penetration on Short Circuit Levels in Distribution Networks," in International Conference of Renewable Energy and Power Quality, ICREPQ 2014, Cordoba, Spain, April 8-10, 2014.
- S. Afifi, H. Wang, G. Taylor and M. Irving, "Impact of DFIG Wind Turbines on Short Circuit Levels in Distribution Networks Using ETAP," 2013 48th International Universities Power Engineering Conference, UPEC2014, Dublin, Ireland, September 2-5, 2013.

Book editing:
"Sustainable Energy: Technological Issues, Applications and Case Studies" ed. by Ahmed F. Zobaa, Sara N. Afifi and Ioana Pisica

### 1.6 Thesis outline

Chapter One - Introduction

This chapter provides a background to the research problem and motivations for conducting this research. The main objectives and aims are defined. The thesis outline is presented.

Chapter Two - Literature Review

This chapter provides an overview of the previous research conducted about the impact of distributed generation on distributed networks. Comprehensive technical challenges of DG implementation are presented. A review of the simulation studies carried out by previous research considering different power system parameters including short circuit analysis are provided. The research gap is highlighted where motivation of this research is based on.

## Chapter Three - Technology and Short Circuit Overview

This chapter is divided into two main sections. First section outlines the arrangement of electrical power systems focusing on the distributed systems and its major difference with transmission systems. The importance of DG integration into distributed systems is presented. A detailed description of distributed generation technologies and its interface are provided. The second section presents the fundamental theories of short circuit analysis and its importance on power systems reliability.

## Chapter Four - Short Circuit Calculations

This chapter presents the main techniques and detailed equations applied in short circuit calculations according to the chosen standards for this research which are IEC and ANSI standards. Also, the differences between these two standards are demonstrated. The major factors that influence the short circuit calculation for each method are given in details.

## Chapter Five - IEEE 13 Bus Distribution Test System

In this chapter, the simulation work carried out by this research using ETAP 12.0 software is presented. Simulation results for ANSI and IEC methods are exploited and presented in figures to demonstrate the impact of DG type, location and penetration level on the short circuit current of the IEEE 13 Bus distribution test system, for both methods. Each section is followed by a discussion, and last section a comparison between the IEC and ANSI simulated results is drawn and discussed.

Chapter Six - IEEE 30 Bus System

This chapter is similar to chapter five in terms of layout and objective. It presents the simulation results carried out using advanced version of ETAP (ETAP 14) on the IEEE 30 bus. However, in chapter six, increased DG capacity and more scenarios have been examined for the system under study. Detailed short circuit analysis is presented for ANSI standard simulation. Main IEC simulated results are presented. Detailed comparison between the IEC and ANSI simulated results are provided and discussed.

Chapter Seven - Conclusions and Future Work

In the final chapter, a summary of this research outcome is presented. The research main contributions are discussed. Furthermore, a recommendation of future work is outlined and proposed.

## Chapter Two

## 2 Literature Review

### 2.1 Introduction

In this chapter, a general review of the impact of distributed generation on distributed networks is presented. Detailed technical challenges of increased DG and its impact on distribution networks will be presented. Moreover, a review of simulation studies performed on various distribution systems addressing the technical impacts of distributed generation on different power system parameters focusing on short circuit analysis will also be presented.

### 2.1.1 Impact of distributed generation on distributed networks

In most of the literature, the introduction for the research usually describes the new era happening in the electrical power systems, in particular the distribution systems. This is the altering of the traditional concepts and theories of power flow, as a consequence of connecting the electrical generation sources at the customer side or to the distribution network, and the impact of this on the system operations, reliability and control. Several authors described a general impact of distributed generation on distribution networks as follows:

The traditional radial distribution system with unique generation source is becoming a multi-source system by the integration of DG [14]. In ref. [15], the authors stated that the connection of distributed generation invalidated the original traditional assumption for the design of the distribution networks, where the primary substation will not be the only source of power and short-circuit capacity. In [16] argued that the penetration of DG changed the historic operation of passive distribution networks that originally used to deliver the power at lower voltages from transmission networks to consumers, with limited control. Furthermore, Ref.[17]- [19] agreed that the distribution networks performance have been altered due to the connection of DG, in which the existence of a radial system with unidirectional power flow pattern is diminished. The distributed networks gained more and modified characteristics to be active with power flows and voltages identified by the generation [20]. Ref. [8]
described it in its simplest form where the current nature of distribution systems is changing from passive to active.

### 2.2 Challenges of increased penetration of DG in distribution network

The challenges that may occur due to increased penetration of DGs in distribution networks can be classified into three categories [16].

### 2.2.1 Commercial challenges

Ref. [16] mentioned that there are number of studies have showed that active management of distribution networks could enhance the implementation of largescale of DG that could be connected to the existing networks. Despite that the cost of active management of distribution networks is still uncertain, though the benefits of connecting DG are expected to exceed the cost of its implementation. Ref. [16] recommended that in order to encourage the development of active distribution networks and to demonstrate the subsequent benefits correlated with connecting substantial amount of DG, new commercial arrangements are required to be created. Moreover, [16] suggested three possible approaches: to recover the cost of applying active management directly via the price control mechanism; to establish an incentive scheme to encourage the uptake of DG integration; and to establish a market mechanism, outside of the regulatory framework.

### 2.2.2 Regulatory challenges

The traditional typical design of distribution networks and operation of passive networks restricted the implementation of large scale of DG due to the lack of welldefined policies and certain regulatory frameworks. [16], [21] recommended that to promote the increased DG implementation, it is necessary to develop and issue appropriate polices that support the DG integration into the distribution networks.

### 2.2.3 Technical challenges

The implications of increased DG penetration into the distribution network depend on various parameters [21]:

1. The voltage level of the distributed network where the DG will be connected.
2. Category of the distribution network.
3. The load demand
4. The level of DG penetration

Accordingly, integration of DGs has significant effect on voltage profile, network losses and fault level [22]-[25]. For existing distribution networks, in which used to be radial and power flows from higher voltage level to lower voltage level. The resistance to reactance ratio ( $\mathrm{R} / \mathrm{X}$ ) is more than one for distribution network and less than one for transmission network. This is due to higher resistance that in turn, causes the voltage drop to increase in the distribution feeder. Moreover, due to higher values of $\mathrm{R} / \mathrm{X}$, the impact of the real power provided by DGs has more impact on voltage profile than the impact of reactive power [26].

The main function for most DGs is to only generate power, and do not contribute to the ancillary services that provide control to the power system and ensure stable operation. Despite that the DG implementation is increasing rapidly, there are technical barriers preventing the large scale of DG penetration into the existing distribution systems [27]. Protection is considered as one of the major issues when DG is connected to existing networks. Interface factors arise from the connection of DG to the utility distribution system. Consequently, high-level penetration of DG systems requires cautious technical consideration in particular the interface of DG influence to ensure and maintain compatibility with the existing grid [28] in [29].

### 2.3 Technical impacts of distributed generation on the distribution systems

### 2.3.1 Network voltage regulation

Consumer loads (such as electronic equipment; lighting; heating elements; and motors) and industrial applications are designed to provide their services from a nominally fixed voltage supply. Consequently, utilities are obliged by law to provide electricity at the consumer side at a voltage that does not deviate from the nominal voltage with a maximum of $\pm 10 \%$. The voltage at all nodes from the upstream at the generation, to the transmission, down to the distribution should be maintained to their nominal value. In other words, the voltage profile should be maintained constant from the generator terminals down to the consumer terminals [30]. Hence,
this requirement often tends to determine the distribution network design and capital cost [31].

The precise voltage levels used differ from country to country; however, the principle of operation remains unchanged [31]. Table 2.1 shows classification of voltage levels used.

TABLE 2.1: VOLTAGE LEVELS CLASSIFICATION IN DISTRIBUTION NETWORKS [31]

| Voltage Level | Voltage Range | Typical UK Voltages |
| :---: | :---: | :---: |
| Low Voltage (LV) | $\mathrm{LV}<1 \mathrm{kV}$ | $230(1$ phase)/400 (3 phase) V |
| Medium Voltage (MV) | $1 \mathrm{kV}<\mathrm{MV}<50 \mathrm{kV}$ | $33 \mathrm{kV}, 11 \mathrm{kV}$ |
| High Voltage (HV) | $50 \mathrm{kV}<\mathrm{HV}<150 \mathrm{kV}$ | 132 kV |

The current flow through the impedance of transmission lines, transformers, and cables makes the fact of voltage drop unavoidable. Compensation techniques are used to maintain a nearly flat voltage profile. A high voltage can be decreased or a low voltage can be increased at a node by the aid of connecting shunt inductor or shunt capacitor at this node respectively. Also, with the aid of connecting a load tap changing transformer at substation can regulate the system voltage [30].

The connection of distributed generation to a distribution network may introduce a significant impact on the voltage profile and power flow. These impacts may be positive or negative depending on the distribution system characteristics, and the DG location, and size [32], [33].

The voltage control is considered as a significant challenge that may inhibit the penetration of any further amount of DG capacity into the distribution networks. This is due to the fact of the change in the flow of power [16], [21]. Therefore, regulating the voltage through the distribution network requires more advanced strategy [21], [34]-[37].

Moreover, in [26], [38], [39], the voltage control aspect has been considered as a principal determining factor for implementing large scale of DG into distributed networks of various voltage levels (low and medium voltages). A number of studies have been performed to mathematically model the effect of high penetration level of DG on the voltage profile of distribution networks [34], [40], [41].

### 2.3.2 Power quality

In order to define the term power quality of electric power systems, it is crucial to introduce first the definition of the term reliability. Reliability refers to the ability of the electric system to deliver electric power to the consumer load without any interruption. Hence, the term power quality refers to the ability to deliver pure Sinusoidal waveform without variations in the nominal voltage or current characteristics [29]. There are two significant aspects of power quality that are usually discussed and considered in research [16], [21]: (1) transient voltage variations and (2) harmonic distortion of the network voltage. Transient voltage variations include voltage flicker, steps, and sags (dips).

### 2.3.3 Voltage flicker

The degree of flicker caused by a given generator is highly dependent on the network parameters, in particular the fault level and $\mathrm{R} / \mathrm{X}$ ratio at the point of common coupling. Consequently, the impact of generator embedding on the network differs from one point to another [30].

### 2.3.4 Voltage steps and sags

Voltage steps occur as result of sudden change in the voltage at the PCC due to an associated abrupt change in active or reactive power flow. This may occur due to switching of a generator either on or off [30].

Voltage sags are also known as voltage dips. It is commonly defined as any low voltage event that temporally occurs between $10 \%$ and $90 \%$ of the nominal RMS voltage lasting between 0.5 and 60 cycles. Whereas, momentary voltage interruption is considered at less than $10 \%$ of the nominal RMS voltage lasting between 0.5 cycles and 3 s . In medium voltage distribution networks, the voltage sags are generated by the occurrence of power system faults, which affect consumers differently according to their location in the electrical network [29]. Moreover, voltage sags may occur due to starting currents (also known as inrush currents) that typically occurs during the starting of induction generators. A soft -starter is equipped to the wind turbine circuits with large induction generators, to limit these inrush currents [30]. The voltage sags and steps may contribute to flicker if they became repetitive or cyclic [30].

The DG connection to the distribution system may have a significant contribution on the power quality. This contribution may be positive or negative. It depends on the distribution system and the connected DG unit characteristics. The positive impacts include improved reliability, voltage regulation, and reduction of transmission and distribution losses. Though, for inverter-based DG units, this may not occur, hence, DG can increase the current and the voltage distortions in the system [42].

Also, a significant standalone DG (such as wind turbine) may cause power quality issues in a weak distribution network particularly during starting and stopping [16], [21]. In [43], demonstrated that DG integration affects power quality, among which the most significant related events are voltage dips induced by failure defects. DG integration can enhance the power quality received by other distribution network users depending on particular circumstance [16], [21], [44], [45].

The power loss through the feeder could be reduced as a consequence of connecting the DG closer to the loads especially at a large scale. This will lead to less amount of power to be drawn from the distribution substitution, which in turn will reduce the amount of current flow throughout the path from the distribution substation to the loads [44] in [21].

Power quality is considered to be an increasingly significant issue and generation is generally subject to the same regulations as loads. Based on this, it has been recommended that this would work effectively in practice and that the careful design would be capable of achieving the required standards [16].

In [46], [47], performed comprehensive reviews on the power quality problems, reactive power management and voltage management where several control devices and methods have been discussed and comparisons of their performances have been presented.

### 2.3.5 Stability

The most common definition used in the literature has been first proposed by Kundur et al. (2004) as the ability of the system to withstand any physical disturbance and regain a condition of operating equilibrium equivalent to the initial operating condition, where most system variables are bounded to ensure that the entire system remains intact [48].

The power system stability has been recognised as significant issue in order to maintain a secure system operation since 1920's. Hence, a major consequence that may result from power system instability is major blackouts. Mainly, power system stability is a single problem. However, there are a number of forms of instabilities that a power system may undergo that cannot be effectively addressed discretely. The classification of power system stability into appropriate categories facilitates the analysis of power system stability which requires to determine the key factors that contribute to instability and to develop methods to improve system stability. The power system stability categorization is based on the physical nature of the resulting mode of instability, the size of disturbances, the devices, processes, and the time span that must be an essential requirement for stability assessment [48].

### 2.1.5.1 Power system stability is classified into three main categories:

1) Rotor angle stability: is the ability of synchronous machines connected to the system to remain in synchronism after the exposure to any disturbance [48].
2) Frequency stability: is the power system capability of maintaining a steady frequency after a severe system disruption leading to considerable imbalance between generation and load [48].
3) Voltage stability: is the ability of a power system to maintain constant voltages at all buses after occurrence of any disturbance initiated from a specified operation condition [48].

Traditionally, power system stability was not considered as a significant issue during the design of distribution networks. This was due to the fundamental topology that the network was passive and consequently remains stable under most circumstances provided the transmission network is itself stable [16], [21].

Also, Ref. [16] discussed that currently system stability is almost not considered when assessing distributed generation systems. Hence, this will change as the level of penetration of DG increases and their contribution to network security becomes critical. Ref. [3] highlighted the issues that need to be considered, which include transient (first swing stability), long term dynamic stability, and voltage collapse.

The stability of distribution networks should be substantially addressed as the penetration of DGs is increasing [21].

In [49]-[54], the change of flow of power from being uni-directional to being bidirectional due to DG integration into the distributed networks is affecting the network performance and stability in a number of ways.

A number of studies have been made to examine the stability issues, operations and control technologies of the distributed systems when large-scale DGs are integrated [46], [47], [55]-[57]. Ref. [55] and [56] have discussed various control strategies and stability issues focused on micro grids.

### 2.3.6 Protection

IEEE standards stated that the integration of distributed resources (DR) into the system may alter the system operating parameters and affect fault current levels. As a consequence, the existing protection scheme and its coordination settings may not operate as initially designed and should be evaluated under these modified parameters.

The connection of high DG capacity on a feeder also has an impact on fault location practices. DG that has a significant contribution to short-circuit currents may cause an unexpected operation of fault indicators that are used to locate fault position [3] .

There are several different significant aspects of protection need to be addressed when considering the installation of DG to distribution networks [16]:

1) Protection of the $D G$ from internal faults;
2) Protection of the faulted distribution network from fault currents generated by the DG;
3) Anti-islanding or loss-of-mains protection (islanding is expected to occur more with increase DG implantations);
4) Impact of DG on existing distribution system protection schemes

Protection systems developed for radial distribution systems are affected by the penetration of DG. This is due to the changes in the traditional distribution power system short circuit power, fault current level and the characteristics of the fault current, such as amplitude, direction, and distribution, as result of interconnecting DG [58].

Existing distribution networks were originally designed and built considering unidirectional power flow without anticipating the era of DG interconnection. Hence, in case of fault occurrence, the protection relays will not be able to coordinate among themselves accurately in a radial distribution network when a large amount of DGs are connected and Bi-directional power flow occurs [59], [60].

Based on the same radial topology, in [58] discussed the impact of DG integration on the distribution system operation and fault response, which in turn could be altered. As a consequence, the original time overcurrent protection coordination may not comply with the new situation. Though, an improved protection arrangement has been presented.

In [54], stated that the integration of a DG to a feeder influences the feeder protection scheme in three different aspects: the islanding phenomenon, the effect on over current relay performance and the reclosure to fuse coordination [32], [51]-[53].

Ref. [61] theoretical studies on the impact of DG on the current seen by protective devices demonstrated that the presence of DG may invalidate the overcurrent protection schemes.

Ref. [62] identified several conflicts between DG and distribution network protection operation, and examined some practical cases with reference to Italian networks.

### 2.3.7 Increase in network fault

Different types of DGs may produce various fault characteristics. An example of this is such as: if power electronic converters are used as the interface for DGs, due to the fast switching and control nature of power electronic converters, the short circuit currents and transients from the converter system may be distinctly restrained [58]. Moreover, several types of larger DG use directly connected rotating machines which in turn contribute to the network fault levels. Induction and synchronous generators will increase the fault level of the distribution system; however, their behaviour under sustained fault conditions is different [31].

Implications of increased fault current level caused by power system faults in the distribution system may generate voltage sags affecting consumers according to their location in the network, especially in medium voltage distribution networks [29].

The effect of increasing the network fault level by adding generation often leads to improved power quality. However, a single large DG, e.g. a wind turbine, on a weak network may lead to power quality problems particularly during starting and stopping [16].

### 2.4 Simulation in literature review

Ref. [63] presented the major issues that affect the distributed networks operation and control as a consequence of connecting huge amounts of DG. These are stability issues; change of short circuit level and voltage profiles; harmonics; malfunction of protection schemes; load losses variations; and power quality. Also, a load flow study has been performed to investigate the impact of a 3 MW wind turbine on the power system losses. The study was carried out using Neplan software for the IEEE 14-bus distribution test system. For this case study, they concluded that the connection of the DG has reduced the power losses.

In ref. [64] investigated the possibility of improving the distributed system voltage profile and reducing system losses through wind power penetration. Simulation was carried out on a 22 kV distribution network connected to a wind plant consisting of four synchronous Vestas V80-1800 kW type generators, using EGC VLIVY 4.2 and DAISY PAS off - Line V 3.5 programmes.

Ref. [65] investigated the effect of 30 MW DG consisting of wind (DFIG and DDWGs), PV, and energy storage on the dynamic operation of distribution systems during transient conditions on the IEEE sixteen bus distribution test system using PSSE and PSAT. Ref. [8] investigated the behaviour of the fault ride-through of distribution networks including DG.

Ref. [8] investigated the impact of CHP plants on voltage control, grid protection and fault level on an existing compact 8 -feeders Dutch distribution network. Voltage control issues and blinding of protection are may rarely happen on small distribution systems. However, ref. [8] strongly recommended that false tripping and fault level have to be precisely considered.

Authors in [33] investigated the impact of DG (synchronous generators) on voltage profile and short circuit analysis on different types of distribution systems (radial, loop and network at 33 kV and 34.5 kV respectively) using DigSILENT, while
varying the DG location and penetration level. Short circuit analysis was simulated according to VDE standards. Three types of faults were simulated for the radial system: 3 phase fault, phase-phase fault, and phase-ground fault. While for the other two distribution systems, only the 3-phase fault type was simulated.

In ref. [66] determined the maximum allowable DG (synchronous generators) capacity that could be connected to an existing MV Italian radial distribution network, while maintaining the DN parameters. Ref. [66] focused on studying the impact of DG penetration on the voltage profiles and line currents as a function of power factor, and short circuit currents. The short circuit analysis carried out in the study considered the 3-phase fault type only.

Ref. [20] investigated the impact of three different DG resources on a real existing medium voltage distribution network in Greece. The paper examined the impact of the DG penetration on the currents, losses, voltage profile, and the short circuit level of the network under study, using NEPLAN software package. The allocation and size of the PV units, the wind energy plant, and the hydroelectric plant were predetermined. The total installed capacity for each DG equal to 2.7 MW , 4MW, and 0.24 MW respectively. However, it was mentioned and noticed that the DG units were connected at remote sites from the MV busbars of the main substation. This mixed DG penetration had negative significant impact on the voltage profile of the network. Despite the possibility of improving the DG units power factor which work with an inductive power factor to keep the voltage within the acceptable limits, this did not solve the problem. It just slightly improved the voltage profile. At the same time, the short circuit level at the MV busbars of the infeeding substation, where it has the highest value did not exceed the design network value. The paper concluded that the irrational allocation of the DG units into the network not only leads to network sterilization as previously discussed, but also leads to the violation of technical constraints. It recommended that in order to avoid any future network operational failure; precise examination using the appropriate tools should be carried out, before any DG penetration into the network.

Ref. [67] analysed the impact of different types of distributed generators on protection coordination, fault current level and voltage profile in a 22 kV test radial distribution networks using MATLAB.

Also, in [68] studied the behaviour of around 10.5 MVA total combined heat and power (CHP) generators connected to real distribution network during faults and its impact on short circuit level using DigSILENT, comparing between short circuit calculations IEC 60909 and IEC 909 standards.

In [69] studied the influence of DG on distribution systems so as to determine the maximum distributed generation penetration that can be accommodated without affecting the system performance. This study investigated the effect of synchronous generators on the IEEE 13-bus test distribution system in terms of fault current, voltage total harmonic distortion (THDV), voltage sag, and voltage swell, using alternative transients program (ATP)-electromagnetic transients program (EMTP) software as a simulation tool. Short circuit calculations addressed the occurrence of single line to ground fault only in respect of same DG location with four cases representing different range of penetration level which are $0 \%, 10 \%, 20 \%, 30 \%$ respectively. The selection of DG was based on the recommendation of previous study performed to determine the reliable DG location on the IEEE 13-bus test distribution system [69].

In [70], the authors addressed some of the overvoltage issues and of the overcurrent protection problems that occur in case of connecting DG to existing networks. The IEEE 34 Node Radial test system was the system under study using Siemens PSS/ADEPT 5.3.2 software for load flow study and fault analysis. The DG unit used was synchronous generator; with penetration level of each DG was $20 \%$ of the original feeder load. The criteria of various DG locations attempted to be on how far or near from the substation, near the voltage regulators, and on laterals and main feeder. The fault analysis examined the maximum and minimum fault currents through each of the protective devices included in the system under study. Three phase fault and single line to ground fault through a fault resistance of $20 \Omega$ were performed for the three phase feeders and branches of the system to calculate the maximum fault current and the minimum fault current respectively. Though, for the single-phase branches, single line to ground faults were only applied, with no fault impedance has been used for calculation the maximum fault current, and $20 \Omega$ resistance was used for the minimum fault.

In [9], [67], [71] argued that the DG interconnections with the grid or network substantially contribute to the short circuit level of the DN, in which it is a significant factor that determines the maximum permissible penetration level. Accordingly, their studies investigated the contribution of DG interconnections on the short circuit level. Despite their agreement on the main concept and importance of idea, Authors in ref. [9] were selective on their choice for the DG types and focused on the directly coupled generators, as their contribution is much more crucial.

Ref. [71] examined the impact of type and interconnection of various DG units including diesel generator; 2 micro-turbines; PV; fuel cell; 2 wind farms; and fuel cell and battery on the fault current level. This study focused on the different interconnection methods of the different DG types used to the grid, and compared their contribution on the short circuit level, using MATLAB/Simulink. The simulation tested the three-phase fault at different locations of the network.

Ref. [9] simulations were carried out on a 10 kV cable distribution network consisting of several feeders in the Netherlands, using DigSilent Power Factory software, testing the occurrence of three phase fault. DFIG, AG, and CHPs (SG) are the DG connected to the network. Also, they compared between the results obtained from IEC standard calculations and the simulation results.

DG and grid contributions were evaluated in [72] under the cases of single line to ground faults and symmetrical three phase faults. The PSCAD software was used for the simulation of transient contributions of various DG units (PV, PSMG, DFIG, SG) respectively, with a range from 1 MVA - 3MVA each, in a tested medium voltage distribution network.

Ref. [73] examined the effect of DG in the fault location on a 25 MV distribution system using MATLAB/Simulink, investigating the different parameters impact such as magnitude of DG, fault impedance, and relative position of the fault location and the DG. The fault type tested in this study was the single line to ground.

In [74], this paper investigated the effect of a 3 MVA synchronous generator on short circuit level of a real 11 kV distribution network supplying industrial loads in Karachi, Pakistan. The network has been modelled on PSS SINCAL. The network
consists of 27 buses excluding the substation bus bar; seven $11 / 0.4 \mathrm{kV}$ transformers with total capacity of 4.75 MVA ; and five connected industrial loads. The short circuit levels were obtained for the all system buses in two different scenarios, with and without DG connection respectively. The penetration level of the selected DG unit represents around $50 \%$ of the total connected load, located at one location only throughout the study. The type and location of short circuit have not been mentioned in the article, although the authors have highlighted that 3-ph faults and single line to ground faults are the most severe faults that may occur.

### 2.4.1.1 Impact of PV on distributed networks

In [75] investigated the influence of high penetration residential PVs on protection and operation issues of a 22 kV residential distribution feeder in a suburb of Raleigh, NC. Hence, detailed system parameters were not provided in this paper. The paper described the system under study as a three phase circuit with unbalanced load where the PVs were connected on a phase basis. The simulation studies carried out using PSCAD to measure the fault current contribution on the operating time of the protective devices when PVs are connected to the system. This is through testing the fault current at the protective devices at different faults including three phase faults and single phase fault, through varying fault resistance; at different fault locations respectively. The selection criteria for fault location was based on the nearest and the farthest points in the protective device primary zone of protection. Also, the PV power output has been varied (assumed power output percentage is equal to percentage of the total system load).

For the same distribution system studied in [75], authors in [76] proposed an algorithm capable to provide an estimate of fault current profile on a distribution feeder with high PV penetration level during the first few seconds of the fault occurrence, to enhance the conventional fault analysis methods in order to facilitate the design and coordination of protection schemes. The study validated the proposed method by performing a fault current simulation study using PSCAD, to obtain detailed time-domain results, so as to be compared with the proposed algorithm results. The simulation calculated the fault current level through the feeder circuit breakers at the occurrence of three phase fault and single line to ground fault while varying the fault resistance, at four different nodes. The maximum difference

## Chapter Two: Literature Review

between the proposed algorithm and simulation results for the magnitude currents was found to be 6.16\%.

Ref. [77] studied the impact of photovoltaics on power flow, voltage, short circuit and relay protection respectively on 10 kV distribution network. PV located at two different locations, where three-phase short circuit current is tested on one of these locations. Simulation tool used was not provided in this paper.

### 2.5 Optimal allocation issues

Ref. [78] mentioned that the DG allocation issue has been only applied on very small scale of distribution systems with limited numbers of buses, despite the fact that distribution systems are usually of huge in terms of rating, and number of buses and branches. Also, the focus is to determine the optimal DG units location and size more than to find the optimal type of DG units. Authors in [78] recommended that more studies need to be performed to find which type of DG unit is the most suitable and adoptable for each bus of the distribution system.

### 2.6 Gap in research

There are several issues have not been covered in the existing literature until this research has been conducted, that is considered in this thesis. Also, there are conflicts in previous research in which this thesis will highlight and attempt to investigate these conflicts to have a reliable outcome. These issues and conflictions are presented in the following sections.

### 2.6.1 PV discussion

In some of the literature, the study of PV contribution on short circuit level of distributed networks is neglected and not substantially recognised. This is due to its limited impact on the short circuit level [9], [79]. The reasons considered for why PV has no significant contribution on short circuit level of distribution networks are:

1- The short circuit current of PV array is low and determined by the thermal limit of the semiconductors (typically 10-20\% of the rated nominal current) [9], [80], [81].

2- Inverters are usually supplemented with under-voltages relays [81].

3- PV current controlled inverters are over-current limited in the case of disturbances coming from the grid. [79], [81].

The PV may supply fault current to the fault under short circuit condition in the feeder. This injected fault current depends on the inverter design, that does not exceed the rated current as mentioned above, and, in which this fault current is still protected against through over current relays and/or fuses coordinated with the protection devices of the distribution feeders [72], [76]. Also, with expected high penetration levels of PV to meet increase of demand, and unpredicted disturbances that may occur such as faults occurring with high resistances out of the PV inverter over-current control and protective devices coordination scheme, or line overloading; some PV systems may be unable to distinguish this fault and injects more fault current to system. Consequently, thus this could cause a delay in the fault detection by the system protective devices and loses system relays coordination and protection reliability [79], [81]-[83]. Therefore, to maintain a resilient, secure and reliable system, the contribution of PV on short circuit current of distribution network shall not be ignored and disregarded. Though, it shall be crucial to investigate the effect of PV short circuit current on the system fault detection.

In ref. [81], stated that from a technical perspective, grid interfacing issues are important to consider for large scale of PV integration. In which, PV contribution to short circuit capacity is considered one the vital issues that needs to be addressed.

Ref [75] argued that despite the facts that PV have limited impact on the distribution system voltage profile and protection, so that high level of penetration could be adopted, it still crucial to investigate and study these parameters. Also, recommended that revisions should be made to existing protection and voltage control schemes.

In [20], the study demonstrated that in real networks operation, the connection of the PV units in combination with other DG resources still contributed to the failure of the network reliability. This ensures that the study of the impact of PV on the power systems studies is essential and should not be neglected.

However, this limitation could be advantage. PV may help in some critical or weak networks to have double role, first acts as current limiting source and second is generation source.

### 2.6.2 Type of fault studied

It is noticed that the three-phase fault type is the most common type of fault examined in the literature, followed by the single line to ground fault type. Few authors mentioned the reasons why they examined the occurrence of these types of faults in particular.

Reasons available in the literature for three-phase fault type:
1- It is the most common [72]
2- Have the highest impact on power system stability; where the most severe switching action with regard to the transient stability [84]
3- Major stress occurs during three-phase faults [9]
4- It is considered the most dangerous type of fault; as all three phases are short circuited and causes maximum damage to the system equipment [74]

5- causes the maximum fault current when the network neutral is earthed directly or through an earth fault current limiting impedance [85]

Reasons available in the literature for single-line to ground fault type:
1- Most likely to happen [72]
2- Causes the most common PQ problems (voltage sag and swell) [69]
This still ensures the importance of examining the three-phase fault and single line to ground fault types. Hence, the research did not provide enough attention to the lineline fault and line-line to ground fault types. Although, the former fault types still constitute to severe unbalanced operating conditions [84].

Hence, the IEEE [3] recommended that the DG needs to be demonstrated in a fault study computer program along with the existing distribution circuit models and different fault simulations performed in order to determine the fault current levels for accurate protection coordination and relay settings. A Short-circuit analysis employs a fault study program and studies the impact of three-phase, line-to-ground, line-toline, and line-to-line-to-ground faults on electrical distribution systems. The shortcircuit study typically calculates the total short-circuit currents as well as the contributions of individual motors, generators, and area EPS ties in the system.

IEEE stated that for DG impact studies, it is crucial that the DG short-circuit contribution to be represented appropriately. Accordingly, this ensures the importance to examine the four different types of fault that may occur in an electrical distribution system.

### 2.6.3 Percentage of distributed generation penetration level

Several studies discussed the significance of examining the impact of increased penetration of DG on distribution systems, and presented the technical challenges that need to be addressed. Though, few studies considered the study of the impact of DG at various penetration levels with $50 \%$ of total connected load, the maximum. In this thesis, the DG penetration level considered reached up to $85 \%$ of the generation capacity.

### 2.7 Summary

This chapter presented a review on the impact of DG on distributed networks. A number of generic statements from the relevant available literature have been included describing the modern phase of electrical power systems in particular the distributed networks. It can be concluded that the distribution networks main characteristics have been changed from being passive to being active due to the introduction of distributed generation. Certainly, this has driven various challenges to arise, that need to be addressed to be able to meet the increased DG implementation, such as commercial, regulatory and technical challenges. A brief review has been provided on the various technical impacts of DG on the distributed networks, showing the linkages to related issues such as power quality and increased network fault level. Also, this chapter presented the simulation studies performed in the existing literature examining the contribution of DG on power systems parameters in particular short circuit level of distributed networks.

Although, several studies attempted to discuss this topic, however many aspects related to this area is still open for further research. These can be summarized as follows:

1. Examining more types of fault including the all three types of unsymmetrical faults;
2. Increasing the DG penetration level to identify their maximum impact;
3. Including various DG types together with various locations;
4. Investigating the impact of DG on short circuit level on large systems with an appropriate number of buses;
5. Using different power system analysis simulation tool
6. Calculating short circuit level by various methods such as IEC and ANSI

## Chapter Three

## 3 Technology Overview

### 3.1 Introduction

In this chapter, there are two main sections presenting basic descriptions and characteristics for this study main subjects. First section, an overview of the electrical power systems focusing on the distributed systems will be presented. A detailed explanation of the distributed generation definition, importance, and main characteristics will be provided. Second section, an overview of short circuit aspect is presented.

### 3.2 Electrical power system arrangement

An electrical power system could be described in the simplest terms as an assembly of electric equipment installed to supply electric energy to consumers. The power system is divided into three main pillars: generation, transmission, and distribution. The distribution system is where the voltage is stepped down to medium voltage (MV) level at 132 kV and below [86], [87].

### 3.2.1 Distribution systems

A typical distribution network consists of a step-down transformer at a supply point feeding a various number of circuits that may have different lengths that can vary from a few hundred meters to a number of kilometres. Throughout these circuits, a series of step down transformers are equipped, from which the final consumer is supplied [86], [87].

### 3.2.1.1 Distribution system configurations

Distribution systems have several types different in configurations, designs and lengths. However, most of these types share common characteristics. In which the main feeder known as the mains or mainline is the back-bone of the circuit, where it is a three-phase circuit out of the substation. One or more circuits branch from the mains, known as taps; lateral taps; branches; or branch lines to which distribution transformers are connected. Along with, laterals are usually connected to the main
through a fuse. These laterals may be single-phase, two-phase, or three-phase depending on the nature of the load [89].

Distribution systems are classified into the following configurations in Figure 3.1 in which one or a combination of the following standard systems is applied.


Figure 3.1 Distribution System Configuration
A. Radial system is considered to be the simplest, where the load is supplied through one radial feeder. However, in case of a fault occurs along the mains, or at the laterals on which the fuse fail to clear the line, the entire feeder will be deenergised. Therefore, all consumers (load) connected to this feeder will suffer from supply interruption until the fault is cleared or the feeder is tied to an adjacent emergency feeder, if there is enough capacity to accommodate this extra load. This type is not reliable for sensitive loads such as hospital and military establishments, where are not capable of tolerating supply interruption [87], [90].
B. Loop system- this system employs two main feeders to supply the load. Hence, if a feeder fails to operate, the entire load of this feeder may supply from the second feeder, in which sufficient spare capacity is considered in the design and available. This system is more advanced than radial systems in regards to the supply interruption duration. This type of system may be operated with the loop as normally open or with the loop normally closed [90].

- Open - loop system where the load is supplied through one of two available feeders [87], that is, one side of the loop is connected to the supply through a disconnecting device that is intentionally left open, hence the second available feeder is also connected to the supply through a normally closed disconnecting device. Both feeders are tied together at their other ends through a switch or disconnecting device [90]. This system still is not reliable enough to provide continuous supply without interruption, since a fault could occur causing the disconnecting switches at both ends to open, leaving the entire feeder de-energized.
- Closed - loop system where the load is supplied through the two sides of the loop simultaneously [87], in which the arrangement of this configuration is typically identical to the open loop system, hence, the two disconnecting devices at both ends connected to the source are normally closed. This type requires a higher degree of accuracy in the protective devices selectivity and relay settings, which may be non-economical/not guaranteed to achieve.
C. Network system, refers to supplying the load by more than one radial feeder [87]. It is created by connecting together the mains in the radial systems to form a grid or mesh. The grid is connected to several power transformers supplied in turn from the sub-transmission and transmission lines at higher voltages [90].

In this thesis, network and radial systems are the systems of interest to investigate and study. This is due to the fact that in practical, these are the most common especially the distribution networks.

### 3.2.2 Integration of renewable energy generators into power systems

The conventional arrangement of power systems has always been set in a hierarchy assembly. From large centralised generation sourced from fossil fuels or nuclear power source, connected to extra high voltage transmission system down through the HV and LV systems to be distributed to consumers. Lately, renewable energy sources are taking over fossil fuels and nuclear power sources. Generators powered from renewable energy sources excluding large scale hydro and large off shore and onshore wind farms are typically much smaller than generators powered through fossil fuels and nuclear power. These small generators are not possible to be connected to the transmission system due to the cost of high voltage transformers and switchgear. Also, the geographical location of the generator is restricted by the
geographical location of the resources, which may not be always near the transmission system. Moreover, integration refers to the physical connection of the generator to the network while maintaining secure and safe operation of the system. Along with The generator control is essential, so that the energy resource is optimally exploited. Therefore, small generators are ideally to be connected to the distributed networks. Such generation is known as distributed generation [30].
3.2.2.1 Interface of distributed generation with the distributed network

The point at which the distributed generation unit is connected to the distribution network is known as the point of common coupling. Every DG unit has its own type of interface with the network, which enables to accommodate the generated power according to the grid requirements. The interface technologies are broadly divided into direct machine coupling and power electronics coupling [94].
A. Direct machine coupling with the distributed network

The direct machine coupling with the grid entails a DG source that harvests mechanical power such as wind power. The selection of the type of the machine depends on the nature of the mechanical power generated/provided. For a constant mechanical power, resulting in constant rotating shaft speed, the synchronous machine is the appropriate type, whereas for variable mechanical power, the induction machine is more suitable. Though, permanent magnet synchronous machines are used for slow rotational speed turbines [94].
B. Power electronics coupling with the distributed network

The power electronics interface conditions the power supplied by the DG unit to meet the grid requirements and improves the performance of the DG source. Power electronics converters such as DC/AC converters convert direct current (DC) power to alternating current (AC) power in order to be compatible with the grid AC power. DC/AC converters interface are applied with the PV systems. Furthermore, power electronics interface could still be used with the direct coupling machines such as DFIG wind turbines to adjust and control of active and reactive power, which is known as partial power electronics coupling to the grid [94]. Table 3.1 presents the type of interface for different DG sources.

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TABLE 3.1:TYPE OF INTERFACE FOR DIFFERENT DISTRIBUTED GENERATION SOURCES

| Energy source type | Type of interface |  |
| :---: | :---: | :---: |
| 年 | Direct Machine coupling - Type of |  |
| generator |  |  |
| (wind) |  |  |\(\left.\quad \begin{array}{c}Power <br>

Electronics\end{array}\right]\) AC/AC

### 3.2.2.2 Impact of type of interface on the distribution system

The interface type of the DG with the grid identifies its impact on the distribution system operation. Basically, there are various interfacing impacts on the distribution system such as [94]:

1. Determines the quality of the power generated by the DG source.
2. Identifies the DG efficiency
3. Controls the cost of DG installation

### 3.3 Overview of DG technologies

Some of the DG technologies and their main characteristic are as follows

### 3.3.1 Diesel generators

Diesel generators are considered the most established DG technology. It is very suitable for stand-alone applications. Their major advantage is that they can be
started and shut down almost spontaneously making them a viable choice for back up applications [4].

### 3.3.2 Hydropower

Hydropower converts the flow of water and the change in water level into electrical energy. The hydroelectric power stations are usually located on or near a water source (such as rivers) [95]. Power is generated through the flow of water in a controlled manner tuning turbines that drives electrical generators. Hydropower stations are classified into large scale hydro and small scale hydro depending on generation capacity. Large scale hydro could be addressed as centralised power generation as it is usually located at remote areas and requires strong transmission systems, though small scale hydro could be classified as distributed generation [30]. Small hydropower plants require low construction period, employ well-developed technology with an overall efficiency of over $80 \%$, low operation and maintenance costs due to automatic operating systems [94].

### 3.3.3 Fuel cells

A fuel cell converts chemical energy into electrical energy. A fuel cell consists of two electrodes (an anode and a cathode) and an electrolyte, retained in a matrix. Fuel cells utilize a variety of fuels such as natural gas, propane, landfill gas, diesel, naptha, methanol and hydrogen. Fuel cells are environmentally friendly and are $20 \%$ more efficient than other forms of energy conversion [86]. A single fuel cell generates output voltage less than 1 v . Therefore, in order to generate higher voltages; fuel cells are assembled above each other and are connected in series forming a fuel cell system [96]. There are four types of fuel cells with different electrolytes and operating temperatures as follows [96]:

1. Proton exchange membrane fuel cell (PEMFC) operating at $80^{\circ} \mathrm{C}$
2. Phosphoric acid fuel cell (PAFC) operating at $200^{\circ} \mathrm{C}$
3. Molten carbonate fuel cell (MCFC) operating at $650^{\circ} \mathrm{C}$
4. Solid oxide fuel cell (SOFC) operating at $1,000^{\circ} \mathrm{C}$

### 3.3.4 Solar energy

Solar energy is predicted to provide one-third of the world energy demand after 2060. Solar energy is divided into solar thermal and solar electricity. Solar thermal
uses the sun as direct source of heat energy to supply hot water for domestic use and swimming pools. Solar electricity uses photovoltaic for supplying electricity [97].

### 3.3.5 Photovoltaic power generation system

The photovoltaic cell is the main building block of the PV power system, as it is a semiconductor device that transforms solar light into electrical energy. This phenomenon is called 'Photovoltaic Effect'. Typically, it is few inches in size and produces about 1 Watt of power. In order to generate high power, PV cells are grouped in series and parallel circuits to form a PV module. Hence, numbers of PV modules are electrically connected in a series-parallel configuration to generate the required current and voltage. The PV array output power is affected by the operating conditions and the site conditions such as geometric location, irradiance level, and ambient temperature [97]-[99].

Photovoltaic system is classified into stand-alone photovoltaic system and gridconnected photovoltaic system. Their implementation depends upon the load function and operation conditions. Grid-connected photovoltaic system operates in parallel with and interconnected with the utility grid. A fundamental PV power generation system is shown in Figure 3.2.


Figure 3.2 Block diagram of a fundamental photovoltaic power generation system [97]
The stand-alone PV system is capable to be designed and sized to provide electricity independently from the utility grid to a wide range of applications varying from wrist watches to spacecraft. Also, electric vehicles, street lights, and remote buildings are highly emerging applications for the use of stand-alone PV system [97], [99].

### 3.3.6 Wind energy

Wind Turbine Generators

The rapid pace of technology development for wind turbine generators (WTGs) is a robust area of research. WTGs developed from small machines with output power ratings of few kilowatts to numerous megawatts; and from machine with very limited speed control and basic capabilities to a sophisticated machine with variable speed control and advanced capabilities using latest power electronics technologies [100]. Modern wind turbines are classified according to the type of generator equipped and configuration. These generators are categorised according to speed control characteristics (either fixed or variable) and use of power electronics. These are: Type 1; Type 2; Type 3; Type 4; and Type 5.

### 3.3.6.1 Characteristics of different types of wind turbine generators

Type 1: Fixed Speed Conventional Induction Generator

This is a squirrel-cage induction generator (SCIG) and is connected to the grid via step-up transformer equipped with soft starter and switched capacitor banks [100], [101]. The maximum output power is generated at a fixed wind speed. The major disadvantage of the SCIG is that it requires a reactive power for its excitation field and huge starting current. Therefore discrete capacitor banks and a soft starter are equipped within the turbine to overcome these implications [100]. Any fluctuations in the wind speed are converted into fluctuations in the mechanical torque and then converted into fluctuations in the electrical power. In weak networks, these fluctuations result in voltage variations at the point of coupling. Consequently, the wind turbine consumes variable amount of reactive power from the grid causing line losses and voltage imbalance. It is more suitable to be connected to a stiff grid [101].

Type 2: Limited Variable Speed Wound Rotor Induction Generator with Variable Rotor Resistance

The WTG configuration is similar to that of Type I, where the induction generator is connected the grid through as step up transformer; capacitor bank; and start softer with regards to the machine stator circuit; with a variable resistor connected to the rotor circuit. The variable resistor is capable of controlling the rotor currents more

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rapidly so as to keep constant power even during gusting conditions, and enhancing the machine's dynamic response in case of grid disturbances [100], [101].

Type 3: Variable Speed Doubly-Fed Induction Generator with Partial-Scale Frequency Converter

This type of generator is also known as doubly fed asynchronous generators. The DFIG is a wound rotor induction generator. This machine has a unique characteristic in which both the stator circuit and the rotor circuit are connected to the grid (Figure 3.3), providing more operational and controllable features and more efficiency than other types of wind turbines. The stator circuit is connected directly to the grid through a step-up transformer, whereas the rotor circuit is connected to the grid through power electronics circuit via slip rings by a current regulated, voltage-source converter, and step up transformer. This power electronics circuit controls the rotor current magnitude and phase. It allows more variable operation speed range, both above and below synchronous speed $\pm 50 \%$. The converters offer a wide range of output control that is only $30 \%$ of the rating of the machine. Active power is delivered to the grid through the stator circuit via the grid-connected invertor when the generator is running more than the synchronous speed. However, when the generator runs below the synchronous speed, active power flows form the grid, through both converters, and from rotor to stator. This in turn, offers the benefit of more speed range. Also, this adds to its flexible operation feature of active and reactive power control, while being able to run asynchronously [100], [102], [103], [2].


Figure 3.3 Schematic diagram of Type 3 WTG [100]
Type 4: Variable Speed with Full- Scale Frequency Converter

This type provides full variable speed wind turbine, in which is independent from the type of generator equipped. This type could accommodate different types of generators such as wound rotor synchronous machines; as permanent magnet synchronous machines, or as squirrel cage induction machines. The generator is connected to the grid via a full scale frequency converter. The full scale frequency converter enables control of the active and reactive power delivered by the generator to the grid and allows the generator to operate over a wide range of speeds. This type also offers flexible mechanical operation without affecting the electrical operation or efficiency, where the turbine could rotate at its optimal aerodynamic speed that in in return generates fluctuating AC power. Also, the gearbox may be excluded in some wind turbines configurations [100], [101], [104].

## Type 5: Variable Speed Synchronous Generator

Type 5 turbines consist of a variable-speed drive connected to a speed/torque converter coupled with a synchronous generator of which is directly connected to the grid via a synchronizing circuit breaker. The speed/torque converter converts the variable speed of the rotor shaft into a constant output shaft speed. The synchronous generator operates at a fixed speed, equivalent to the grid frequency. This system configuration provides a synchronized and a generator protection system; along with the speed and torque control of speed/torque converter and the automatic voltage regulator (AVR), thus enhances the synchronous generator to be designed to the desired speed and voltage [100].

It can be concluded that Type 1 and Type 2 have no voltage control; reactive power compensators; and provide fixed and limited variable speed respectively. Types 1 and 2 are considered as "old fashioned" technologies. These types are unable to contribute in voltage control and therefore considered as not compliant with the grid codes. Consequently, their use in the industry has decreased and their study in research has been out of interest [104]. Though, Types 3, 4, and 5 offer wide range of variable speed; active and reactive power control; and voltage control. This is due to the presence of advanced power electronics in their configuration. Type 3 has taken over in research and industry due to the advantage of the DFIG that it offers which is the independent control of real and active power, while being able to run asynchronously [100], [101]. Also, Type 4 especially the permanent magnet
synchronous generator technology started to gain focus on its research and production by large companies such as GE Energy and Vestas Wind Systems [101].

Despite the knowledge of the operating principles of these machines is known, the impact of these machines on the grid at the instance of grid disturbances such as short circuit is still uncertain, and requires more examination. This will facilitate the power system planning and protection design of introducing wind farms comprising these machines, into existing or during implementation of new grids [105] . Power system planning and protection highly depend on the type of wind turbine generator being connected. There various factors that may affect the fault current contribution of wind turbine generators such as: magnetic saturation; deep bar effects; and stator winding connection being wye or delta. Moreover, each of the wind turbine configurations behaves differently during faults. Furthermore, within these different types of wind turbines, manufacturers deploy variation in control, which in turn has an influence on the fault current contribution [106]. The presence of power electronics converters in Type 3 and 4 generators makes the short circuit behaviour more complicated than the Thevenin equivalent representation of synchronous generators [102].

### 3.4 Short circuit and short circuit currents

Short circuit is a significant parameter in the electrical power systems planning, design and operation. It is also known as faults. Short circuit is a failure in the network which interferes with the normal flow of current. The most common reasons for faults occurrence in power systems are lightning strikes; overhead lines breaking; damage of cables as a result of earth construction works; and internal faults ( such as ageing of insulation materials). This ensures that short-circuits cannot be avoided despite cautious planning and design, appropriate regular maintenance and thorough/disciplined operation of the system. Faults often result in the conductors being effectively shorted together or shorted to ground. This leads to the flow of very large current which is called short circuit current, which may cause severe damage to the installed electrical equipment [30], [107].

Effect of short circuit current occurrence on the power system may be [108]:

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1) The system components carrying the short circuit current will be subjected to high thermal and mechanical stresses that may not be capable to withstand these abnormal stresses and will be damaged.
2) At fault location, arcing and burning may happen destroying the adjacent components, and may cause an arc-flash burn hazard to personnel working on the equipment.
3) Short-circuit current may flow from the various rotating machines in the electrical power system to the fault location.
4) voltage drop is in proportion to the magnitude of the short-circuit currents flowing through the system elements, in particular at the fault location where the maximum voltage drop happens, however, all other sections of the power system may be subject to a voltage drop to some extent.

Therefore, short circuit currents have a significant impact on the design and operation of equipment of power system.

The short-circuit current is the maximum value of short circuit current that may occur in the system at given location with no fault impacts such as fault arc impedances (that reduce the fault current). The size and capacity of the power sources (such as generators) supplying the system have a direct impact on the shortcircuit current. Generally, the greater the capacity of the power sources supplying the system, the larger the short-circuit current [108]. The main factors that identify the magnitude and duration of the short-circuit currents are:

1) The type of fault
2) contribution of fault current sources available
3) The impedances between the sources and the fault location.

### 3.4.1 Types of fault

The types of fault that may occur in a power system are classified into symmetrical and unsymmetrical faults, also described as balanced and unbalanced faults. Symmetrical faults are faults involving the three-phases. Though, the unsymmetrical faults are faults involving some unbalance as: Line to ground faults, Line-to-Line to ground faults, and Line-to-Line faults.

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Figure 3.8 Schematic diagrams for type of faults

### 3.4.1.1 Short circuit level (fault level)

In addition to fault current $\mathrm{I}_{\mathrm{f}}$ (in kA ), fault MVA is frequently used as a rating and is often referred as the fault level. The fault level is expressed as follows [86]:

$$
\begin{equation*}
\text { MVA fault level }=\sqrt{3} V_{L} I_{f} \tag{3.1}
\end{equation*}
$$

where, the $\mathrm{V}_{L}$ is the nominal line voltage of the faulted section in kV .

### 3.4.1.2 Basics of short circuit current calculations

The calculation of the precise magnitude of a short-circuit current at a given time after the occurrence of a fault is considerably complex computation. Simplified methods have been developed that provide conservative calculated short circuit currents that could be compared with the tested short circuit current ratings of protective devices [108].

In this section, a simplified short circuit calculation is presented to provide a basic understanding to further advanced procedures. In order to calculate the short circuit current magnitude at any point of time, an R-L circuit with an ideal sinusoidal voltage source and a switch as shown in Figure 3.9 is considered. The fault is initiated by closure of the switch.

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Figure 3.9 R-L circuit model for short circuit current calculation
Assumptions considered are:

1) All machines internal voltages are constant
2) Machines reactances and resistances are constant
3) Saturation effects are ignored
4) Load currents (pre-fault currents) are neglected

The rms value for short circuit current (I) is calculated by this formula [108]:

$$
\begin{equation*}
I=\frac{E}{Z} \tag{3.2}
\end{equation*}
$$

where
E rms voltage
Z Is the Thevenin equivalent system impedance from the fault point back to and including the source or sources of short-circuit currents for the distribution system

Though in practice, the short circuit currents magnitudes vary with time. There are two main factors necessary to consider during the calculations of short circuit currents that varies with time [109]:

1) The presence of the DC component
2) The behaviour of rotating machines under short circuit conditions

The rotating machines including synchronous and induction motors, generators, and utility ties are the primary sources of short-circuit currents. All these rotating machines have machine currents that decay considerably with time due to reduction of flux in the machine during a short circuit. During the occurrence of a fault, synchronous and induction motors will perform as generators and will supply current to the fault depending on the amount of stored electrical energy [108].

Consequently, fault levels will vary considerably during a fault, taking into account the rapid drop of the current due to the armature reaction of the synchronous machines and the fact that fault clearance is not instantaneous [109]. The characteristics, locations, and sizes of the fault current sources connected to the distribution system when a fault occurs have an extensive impact on the initial magnitude and the wave shape of the fault current [108]. Therefore, short circuit currents have to be calculated prudently in order to obtain the accurate value for the relevant applications [109].

The calculation of the short circuit current as a function of time involves expansion of Equation (3.2) through the solution of the following differential equation for current i [108]:

$$
\begin{equation*}
\mathrm{Ri}+\mathrm{L} \frac{\mathrm{di}}{\mathrm{dt}}=\sqrt{2} \mathrm{E} \sin (\omega \mathrm{t}+\varphi) \tag{3.3}
\end{equation*}
$$

where

E is the rms magnitude of the sinusoidal voltage source
i Is the instantaneous current in the circuit at any time after the switch is closed

R Is the circuit resistance in ohms
L Is the circuit inductance in Henries
t Is time in seconds
$\varphi \quad$ Is the angle of the applied voltage in radians when the fault occurs
$\omega \quad$ Is the $2 \pi \mathrm{f}$ where f is the system frequency in hertz ( Hz )

The solution to Equation 2.3 is where the instantaneous current solution is derived:

$$
\begin{align*}
& i=-\frac{\sqrt{2} E}{Z} \sin (\alpha-\varphi) e^{-\frac{\omega t R}{X}}+\frac{\sqrt{2} E}{Z} \sin (\omega t+\alpha-\varphi)  \tag{3.4}\\
& i=-i_{d c} \sin (\alpha-\varphi) e^{-\frac{\omega t R}{X}}+\sqrt{2} I_{a c, r m s} \sin (\omega t+\alpha-\varphi) \tag{3.5}
\end{align*}
$$

where

$$
\begin{gather*}
\varphi=\tan ^{-1}\left(\frac{\omega L}{R}\right)=\tan ^{-1}\left(\frac{X}{R}\right)  \tag{3.6}\\
X=\omega L  \tag{3.7}\\
Z=\sqrt{R^{2}+X^{2}} \tag{3.8}
\end{gather*}
$$

In Equation 3.4, there are two distinct components of short circuit currents drawn: a) decaying dc component at exponential rate, b) ac component or steady state component.

The presence of the dc component depends on the time on the voltage sinusoidal waveform at which the fault occurs. The dc component adds a further increase on the fault current magnitude during the first few cycles. The dc component disappears eventually with time, in which it decays to zero in one to 30 cycles. The rate of decay depends on the $\mathrm{X} / \mathrm{R}$ ratio, the higher the $\mathrm{X} / \mathrm{R}$ ratio, the slower is the decay [108]. Remarkably, the magnitude and duration of the fault current depends on the $\mathrm{X} / \mathrm{R}$ ratio of the circuit impedance and the phase angle $\alpha$ of the voltage at instance of fault. Also, the difference between the initial fault magnitude and the final steady state fault current magnitude depends on these same parameters [108].

### 3.4.1.3 Short circuit currents calculations

The calculation of currents that flow when different types of fault occur is a fundamental task carried out at the design of power systems networks [86]. The magnitudes of the fault currents provide the power system engineer the protection current settings to be used and the circuit breakers ratings [86]. Basically, for simple systems up to 6-8 buses, calculations could be performed manually, however, for complex networks with several numbers of buses and significant amount of components, it is more reliable and viable that fault currents are obtained using computer programs [110]. Moreover, these digital calculations provide the advantage of advanced manipulations through considering different study cases scenarios such as applying faults at various points in the network under study. Along with, the capability of modelling the machines in terms of their varying mechanical and electrical parameters in order to study their behaviour during short circuit conditions offers an extraordinary potential [110].

### 3.4.1.4 Aim and objectives of short circuit studies

1) To determine maximum and minimum three-phase short circuit currents [86]
2) To determine the unsymmetrical fault current (single -line to ground; line-line to ground; line to line faults) [86]
3) To design the fault protection scheme, in order to select the circuit breakers, other switching or protecting devices, and switchgear components ratings and locations. As it should withstand the fault current for short periods and disconnect the faulted system quickly [111]
4) To determine the voltages and the transient performance of the networks under various fault conditions. This is because faults cause drop in voltage, unbalance and loss of stability [111]
5) To select system layout and design [111]

Calculation techniques
The calculation of short circuit currents which are expected to flow in the system under study requires identifying an equivalent circuit for each system element in order to adequately represent its performance under short circuit conditions. The short circuit currents calculations enquire the solving of complex differential equations; hence the use of simplifying techniques is a necessity to ease the calculations, while at the same time obtain accurate results [108]. These techniques are well established, authorized, and recognised to be providing acceptable results for short circuit currents using system parameters and conditions. The most common standards referred to in short circuit analysis are ANSI/IEEE and IEC. These standards are presented in details in chapter 4.

### 3.5 Summary

In this chapter, an overview of distribution systems has been presented. The penetration of DG into distributed systems has several benefits and implications. Short circuit may influence the protection scheme coordination and reliability due to the reversible flow of power as a result DG integration. Though, short circuit is a fundamental feature that has various causes to occur and different types. It is necessary to obtain accurate short circuit currents during the short circuit studies to ensure reliable and valid selection of protective devices ratings and coordination. Therefore, short circuit analysis is essential for identifying the protective devices

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ratings and relays settings and coordination to maintain secure fault protection system.

## Chapter Four

## 4 Short Circuit Calculations

### 4.1 Introduction

There are several authorised standards available to calculate the short circuit currents. These standards include IEC, ANSI, VDE, etc. In this thesis, IEC and ANSI are the standards selected to be used in the investigation. In this chapter, the conceptual techniques and detailed modelling of IEC and ANSI standards for short circuit calculations will be presented. This chapter consists of three main sections: first, short circuit calculation according to IEC standards will be presented; followed by the short circuit calculation according to ANSI standards in second section; and last, the differences in the calculation procedures between the two standards will be tabulated in the third section of this chapter.

### 4.2 Short circuit calculations according to IEC standards

The International Electrotechnical Commission (IEC) is a worldwide organization for standardization comprising all national electrotechnical committees (IEC National Committees). The first edition issued for short circuit calculation was the IEC 909 Standard in 1988. This was a derivative work taken from the German Verband Deutscher Electrotechniker (VDE) Standard. In 2001, a renewed version IEC 60909 has been published and has been acknowledged as the accepted European standard for calculation of symmetrical and unsymmetrical faults [68]. IEC 60909-0 2016 is the most recent edition issued in 2016. This version cancels and replaces the 2001 edition. The major technical changes included with respect to the previous edition are: a) contribution of wind power station units to the short-circuit current; b) contribution of power station units with full size converters to the short-circuit current [112]. This standard applies to all voltages up to 550 kV three-phase systems operating at nominal frequency ( 50 or 60 Hz ).

### 4.2.1 General characteristic: Definitions and assumptions

There are basic definitions and assumptions considered by the standard shall be demonstrated before discussing the short circuit current calculations.

### 4.2.1.1 IEC short circuit currents classification

The IEC standard considers four types of duties for the short circuit currents:

Initial symmetrical short circuit current $\left(\mathrm{I}_{\mathrm{k}}^{\prime \prime}\right)$ : rms value of the AC symmetrical component of a prospective short-circuit current applicable at the instant of short circuit if the impedance remains at zero-time value

Peak short circuit current ( $\mathrm{i}_{\mathrm{P}}$ ): maximum possible instantaneous value of the prospective short circuit current

Symmetrical short circuit breaking current ( $\mathrm{I}_{\mathrm{b}}$ ): rms value of an integral cycle of the symmetrical AC component of the prospective short circuit current at the instant of contact separation of the first pole to open of a switching device

Steady-state short-circuit current $\left(\mathrm{I}_{\mathrm{k}}\right)$ : rms value of the short-circuit current which remains after the decay of the transient phenomena

There are two different types of impedances considered in the standard: the shortcircuit impedances at the short-circuit location F , and the short-circuit impedances of individual electrical equipment.

Basically, the IEC distinguishes between single-fed short circuit, multiple single-fed short circuits and multiple-fed short circuits. Also, this classification is known as non-meshed and meshed networks respectively. The calculation of peak short-circuit current ( $i_{P}$ ) depends on the type of network especially in meshed networks, where specific methods shall be applied with adequate accuracy.

Also, IEC distinguishes between two fundamental faults which are 'Far-fromgenerator' and 'Near-to generator'. In the former, the magnitude of the symmetrical AC component of the prospective short-circuit current remains essentially constant (i.e. have no AC component decay) as shown in Figure 4.1, whereas in the latter, the magnitude of the symmetrical AC component of the prospective short-circuit current decreases with time (i.e. have AC component decay) as shown in Figure 4.2.


Figure 4.1 - Schematic diagram of short circuit current of a far-from-generator short circuit with constant AC component [112]


Figure 4.2- Schematic diagram of short circuit current of a near-to-generator short circuit with decaying AC component [112]

### 4.2.1.2 Equivalent voltage source

The IEC defines an equivalent voltage source as an ideal source applied at the short circuit location for calculating the short circuit current. This equivalent voltage source is the only active voltage of the system, where all other active voltages in the system are short-circuited. All network feeders, synchronous and asynchronous machines are replaced by their internal impedances. Moreover, IEC states that the

## Chapter Four: Short Circuit Calculations

operational data and the load of consumers, tap-changer position of transformers, and excitation of generators are not essential; hence, additional calculations about all the different possible load flows at the moment of short-circuit are superfluous [112]. This equivalent voltage source is derived as follows:

$$
\begin{equation*}
\text { Equivalent voltage source }=\frac{c \cdot U_{n}}{\sqrt{3}} \tag{4.1}
\end{equation*}
$$

where the c is the voltage factor (depends on system nominal voltage) in table 4.1; $U_{n}$ is the system nominal voltage.

The voltage factor c considers the differences between the voltage at the short-circuit location and the internal voltage of system feeders, motors and generators due to voltage variations; transformer taps changing; loads and capacitances ignorance during calculations; and subtranasient behaviour of generators and motors. The assumption for considering a voltage factor will result in reliable short-circuit currents, that are higher than in the real power system, though, this will avoid an uneconomic high safety margin [107]. Table 4.1 introduces the voltage factor c values to be considered.

TABLE 4.1: VOLTAGE FACTOR C [112]

| Nominal System <br> Voltage <br> $\boldsymbol{U}_{\boldsymbol{n}}$ | Maximum short circuit <br> currents $\boldsymbol{c}_{\boldsymbol{m a x}}$ | Minimum short circuit <br> currents $\boldsymbol{c}_{\boldsymbol{m i n}}$ |
| :---: | :---: | :---: |
| Low voltage <br> 100 V to 1000 V <br> voltage tolerance of <br> $\pm 6 \%$ | 1.05 |  |
| voltage tolerance of <br> $\pm 10 \%$ | 1.10 | 0.95 |
| High voltage <br> $>1 \mathrm{kV}$ to 230 kV <br> $>230 \mathrm{kV}$ | 1.10 | 0.9 |

Remark: $\mathrm{c}_{\text {max }}$ Un should not exceed the highest voltage Um for equipment of power systems as per IEC 60909-0 2016 standard

### 4.2.1.3 Maximum and minimum short circuit currents

The IEC standard distinguishes between maximum short-circuit currents and minimum short-circuit currents, in which the former is responsible for the rating of equipment regarding mechanical and thermal stresses, whereas the latter has to be calculated for the selection of the system protection such as selection of fuses [112]. Table 4.2 provides an overview of the IEC standard classification for the short circuit currents and types of failures that have to be considered.

TABLE 4.2: IEC STANDARD CLASSIFICATION FOR THE SHORT CIRCUIT CURRENTS AND TYPES OF FAILURE [112]

| Short circuit currents | Equipment | Relevant Currents |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | K 3 | K 2 |
|  |  |  |  |  |
| Dynamic | Components of installations | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{i}_{\mathrm{p}}$ | - |
| Switching on | Switching devices | $\mathrm{i}_{\mathrm{p}}$ | - | $\mathrm{i}_{\mathrm{p}}$ |
| Switching off | Switching devices | $\mathrm{I}_{\mathrm{b}}$ | - | $\mathrm{I}_{\mathrm{b}}$ |
| Thermal | Components of installations, lines | $\mathrm{I}_{\mathrm{th}}$ | - | $\mathrm{I}_{\mathrm{th}}$ |
| Minimum currents | Protection | - | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}, \mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}, \mathrm{I}_{\mathrm{k}}$ |
| Tripping of relays |  |  |  |  |

$\mathrm{I}_{\mathrm{th}}$-Thermal equivalent short-circuit current; k 1 - Line-to-earth short circuit, line-to-neutral short circuit; k2- Line-to-line short
circuit; k3-Three-phase short circuit

### 4.2.1.4 Calculation assumptions

The IEC standard takes the following assumptions for the calculation of maximum and minimum short-circuit currents [112]:
a) For the duration of the short circuit, there is no change neither in the type of short circuit nor the network involved, where a three-phase short-circuit remains three-phase and a line-to-earth short circuit remains line-to-earth during the time of short circuit.
b) The impedance of the transformers is referred to the tap-changer in main position.
c) Arc resistances are neglected.
d) Shunt admittances of non-rotating loads shall be neglected in the positive-, the negative- and the zero-sequence system.
e) Line capacitances shall be neglected in the positive- and negative-sequence system. Line capacitances in the zero-sequence system shall be taken into account in low-impedance earthed networks.
f) Magnetising admittances of transformers shall be neglected in the positiveand negative sequence system.

### 4.2.1.5 Calculation conditions

The IEC states that the following conditions shall be applied when calculating maximum and minimum short circuit currents [112].

Conditions for maximum short circuit currents calculations
a) Voltage factor $\mathrm{C}_{\text {max }}$ shall be applied in the absence of a national standard.
b) Select the system configuration and the maximum contribution from power station units and network feeders which lead to the maximum value of shortcircuit current at the short circuit location
c) Impedance correction factors shall be introduced in the positive-, the negative- and the zero-sequence system with exception of the impedances between neutral point and earth.
d) When equivalent impedances $\mathrm{Z}_{\mathrm{Q}}$ are used to represent external networks, the minimum equivalent short-circuit impedance shall be used which corresponds to the maximum short-circuit current contribution from the network feeders.
e) Motors shall be included
f) Resistance $R_{L}$ of lines (overhead lines and cables) shall be introduced at a temperature of $20^{\circ} \mathrm{C}$.

Conditions for minimum short-circuit currents calculations
a) Voltage factor $\mathrm{C}_{\text {min }}$ shall be applied.
b) Choose the system configuration and the minimum contribution from power station units and network feeders which lead to a minimum value of shortcircuit current at the short circuit location.
c) The impedance correction factors are equal to 1 .
d) Contributions of wind power stations units shall be neglected.
e) Contributions of photovoltaic power station units shall be neglected.
f) Contributions of motors shall be neglected.
g) Resistances $\mathrm{R}_{\mathrm{L}}$ of lines (overhead lines and cables, line conductors, and neutral conductors) shall be introduced at a higher temperature.

### 4.2.2 Calculation of initial short circuit current

### 4.2.2.1 Three-phase short circuit current ( $\mathbf{I}_{\mathbf{k}}^{\prime \prime}$ )

$$
\begin{equation*}
I_{k}^{\prime \prime}=\frac{c U_{n}}{\sqrt{3} Z_{k}}=\frac{c U_{n}}{\sqrt{3} \sqrt{R_{k}^{2}+X_{k}^{2}}} \tag{4.2}
\end{equation*}
$$

where $\mathrm{Z}_{\mathrm{k}}$ is the short-circuit impedance
The short-circuit impedance can be obtained by the network reduction or from the diagonal element of the nodal impedance matrix of the positive sequence system for the point where the short circuit.

### 4.2.2.2 Line-to-line short circuit ( $\mathbf{I}_{\mathbf{k} 2}$ )

$$
\begin{equation*}
I_{k 2}^{\prime \prime}=\frac{\sqrt{3}}{\left|\underline{Z}_{(1)}+\underline{Z}_{(2)}\right|} \frac{c U_{n}}{\sqrt{3}} \tag{4.3}
\end{equation*}
$$

If $\underline{Z}_{(2)}=\underline{Z}_{(1)}$, then the formula becomes

$$
\begin{equation*}
I_{k 2}^{\prime \prime}=\frac{\sqrt{3}}{2} I_{k}^{\prime \prime} \tag{4.4}
\end{equation*}
$$

4.2.2.3 Line-to-line short circuit with earth connection

Initial symmetrical line two (L2) short circuit current with earth connection

$$
\begin{align*}
& \mathrm{I}_{\mathrm{k} 2 \mathrm{EL} 2}^{\prime \prime}=\left|\frac{\sqrt{3}\left(\underline{\mathrm{Z}}_{0}-\mathrm{a} \underline{Z}_{(2)}\right)}{\underline{\mathrm{Z}}_{(1)} \underline{\mathrm{Z}}_{(2)}+\underline{\mathrm{Z}}_{(1)} \underline{Z}_{(0)}+\underline{\mathrm{Z}}_{(2)} \underline{Z}_{(0)}}\right| \frac{\mathrm{c} \mathrm{U}_{\mathrm{n}}}{\sqrt{3}}  \tag{4.5}\\
& \mathrm{I}_{\mathrm{k} 2 \mathrm{EL} 3}^{\prime \prime}=\left|\frac{\sqrt{3}\left(\underline{\mathrm{Z}}_{0}-\mathrm{a}^{2} \underline{\mathrm{Z}}_{(2)}\right)}{\underline{\mathrm{Z}}_{(1)} \underline{\mathrm{Z}}_{(2)}+\underline{\mathrm{Z}}_{(1)} \underline{\mathrm{Z}}_{(0)}+\underline{\mathrm{Z}}_{(2)} \underline{\mathrm{Z}}_{(0)}}\right| \frac{\mathrm{c} \mathrm{U}_{\mathrm{n}}}{\sqrt{3}}  \tag{4.6}\\
& I_{k E 2 E}^{\prime \prime}=\left|\frac{3 \underline{Z}_{(2)}}{\underline{Z}_{(1)} \underline{Z}_{(2)}+\underline{\mathrm{Z}}_{(1)} \underline{\mathrm{Z}}_{(0)}+\underline{\mathrm{Z}}_{(2)} \underline{\mathrm{Z}}_{(0)}}\right| \frac{\mathrm{c} \mathrm{U}_{\mathrm{n}}}{\sqrt{3}} \tag{4.7}
\end{align*}
$$

4.2.2.4 Line-to-earth short circuit $\left(\mathbf{I}_{\mathbf{k} \mathbf{1}}^{\prime \prime}\right)$

$$
\begin{equation*}
\mathrm{I}_{\mathrm{k} 1}^{\prime \prime}=\frac{3}{\left|\underline{\mathrm{Z}}_{(1)}+\underline{\mathrm{Z}}_{(2)}+\underline{\mathrm{Z}}_{(0)}\right|} \frac{\mathrm{c} \mathrm{U}_{\mathrm{n}}}{\sqrt{3}} \tag{4.8}
\end{equation*}
$$

4.2.2.5 Contribution of power stations with full size converter

If power stations with full size converter are to be considered then the maximum initial short circuit currents are to be calculated. The IEC adds the sum of the contributions of the wind power station units to the initial short circuit current, to the maximum initial symmetrical short-circuit current calculated without the contribution of the source currents of the power stations with full size converter.

Maximum initial Three-phase short circuit current ( $\mathbf{I}_{\mathbf{k m a x}}^{\prime \prime}$ )

$$
\begin{equation*}
I_{\mathrm{kmax}}^{\prime \prime}=\frac{1}{Z_{\mathrm{k}}} \frac{c_{\max } U_{\mathrm{n}}}{\sqrt{3}}+\frac{1}{Z_{\mathrm{k}}} \sum_{j=1}^{n} Z_{i j} \cdot I_{\mathrm{skPF} j}=I_{\mathrm{kmaxPFO}}^{\prime \prime}+I_{\mathrm{kPF}}^{\prime \prime} \tag{4.9}
\end{equation*}
$$

where
$\mathrm{I}_{\mathrm{skPFj}} \quad$ is the rms value of the maximum source current (positive-sequence system) in case of three-phase short-circuit at the high-voltage side of the unit transformer, given by the manufacturer;
$\mathrm{Z}_{\mathrm{ii}}, \mathrm{Z}_{\mathrm{ij}} \quad$ are the absolute values of the elements of the nodal impedance matrix of the positive-sequence system, where $i$ is the short-circuit node and j are the nodes where power station units with full size converters are connected;
$\mathrm{I}_{\mathrm{kmaxPFO}}^{\prime \prime} \quad$ is the maximum initial symmetrical short-circuit current without the influence of power station units with full size converter;
$\mathrm{I}_{\mathrm{kPF}}^{\mathrm{\prime}} \quad$ is the sum of the contributions of power station units with full size converter to the initial short-circuit current.

Maximum initial Line-to-line short circuit ( $\mathbf{I}_{\mathbf{k} \mathbf{~} \mathbf{m a x}}$ )

$$
\begin{align*}
& \mathrm{I}_{\mathrm{k} 2 \max }^{\prime \prime}=\frac{\sqrt{3}}{\left|\underline{\mathrm{Z}}_{(1) \mathrm{ii}}+\underline{\mathrm{Z}}_{(2) \mathrm{ii}}\right|} \frac{\mathrm{c}_{\max } U_{\mathrm{n}}}{\sqrt{3}} \\
+ & \frac{\sqrt{3}}{\left|\underline{\mathrm{Z}}_{(1) \mathrm{ii}}+\underline{\mathrm{Z}}_{(2) \mathrm{ii}}\right|} \sum_{\mathrm{j}=1}^{\mathrm{n}} \mathrm{Z}_{(1) \mathrm{ij}} . \mathrm{I}_{(1) \mathrm{sk} 2 \mathrm{PFj}}  \tag{4.10}\\
= & \mathrm{I}_{\mathrm{k} 2 \operatorname{maxPFO}}^{\prime \prime}+\mathrm{I}_{\mathrm{k} 2 \mathrm{PF}}^{\prime \prime}
\end{align*}
$$

where

| $\mathrm{I}_{(1) \mathrm{sk2PFj}}$ | is the rms value of the maximum source current (positivesequence system) in case of a line-to-line short circuit at the high-voltage side of the unit transformer, given by the manufacturer; |
| :---: | :---: |
| $\underline{\mathrm{Z}}_{(1) \mathrm{ii}}=\underline{\mathrm{Z}}_{\mathrm{ii}}$ | is the $i^{\text {th }}$ diagonal element of the nodal impedance matrix of the positive sequence system, where $i$ is the short-circuit node; |
| $\underline{Z}_{(2) \mathrm{ii}}$ | is the $i^{\text {th }}$ diagonal element of the nodal impedance matrix of the negative sequence system including the impedances of the power station units with full size converter, where $i$ is the short-circuit node; |
| $\underline{Z}_{(1) \mathrm{ij}}=\underline{Z}_{\mathrm{ij}}$ | are the elements of the nodal impedance matrix of the positivesequence system, where $i$ is the short-circuit node and $j$ are the nodes where power station units with full size converters are connected; |
| $\mathrm{I}_{\mathrm{k} 2 \text { maxPFO }}$ | is the maximum initial symmetrical short-circuit current calculated by the equivalent voltage source at the short-circuit location without influence of the source currents of the power station units with full size converter; |
| $\mathrm{I}_{\mathrm{k} 2 \mathrm{PF}}$ | is the sum of the contributions of power station units with full size converter to the initial short-circuit current. |

Maximum initial Line-to-line short circuit with earth connection

$$
\begin{align*}
\mathrm{I}_{\mathrm{k} 2 \mathrm{EL} 2 \max }^{\prime \prime}= & \left|\frac{\sqrt{3}\left(\underline{\mathrm{Z}}_{(0) \mathrm{ii}}-\mathrm{a} \underline{\mathrm{Z}}_{(2) \mathrm{ii}}\right)}{\underline{\mathrm{Z}}_{(1) \mathrm{ii}} \underline{Z}_{(2) \mathrm{ii}}+\underline{\mathrm{Z}}_{(1) \mathrm{ii}} \underline{\mathrm{Z}}_{(0) \mathrm{ii}}+\underline{\mathrm{Z}}_{(2) \mathrm{ii}} \underline{Z}_{(0) \mathrm{ii}}}\right| \cdot\left(\frac{\mathrm{c}_{\max } U_{\mathrm{n}}}{\sqrt{3}}\right. \\
& \left.+\sum_{\mathrm{j}=1}^{\mathrm{n}} \mathrm{Z}_{(1) \mathrm{ij}} \cdot \mathrm{I}_{(1) \text { sk2PFj }}\right)  \tag{4.11}\\
& =\mathrm{I}_{\mathrm{k} 2 \mathrm{EL} 2 \operatorname{maxPFO}}^{\prime \prime}+\mathrm{I}_{\mathrm{k} 2 \mathrm{EL} 2 \mathrm{PF}}^{\prime \prime}
\end{align*}
$$

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$$
\begin{align*}
& \mathrm{I}_{\mathrm{k} 2 \mathrm{EL} 3 \mathrm{max}}^{\prime \prime}=\left|\frac{\sqrt{3}\left(\underline{\mathrm{Z}}_{(0)} \mathrm{ii}-\mathrm{a}^{2} \underline{Z}_{(2) \mathrm{ii}}\right)}{\underline{\mathrm{Z}}_{(1) \mathrm{ii}} \underline{Z}_{(2) \mathrm{ii}}+\underline{\mathrm{Z}}_{(1) \mathrm{ii}} \underline{\mathrm{Z}}_{(0) \mathrm{ii}}+\underline{\mathrm{Z}}_{(2) \mathrm{ii}} \underline{\mathrm{Z}}_{(0) \mathrm{ii}}}\right| \cdot\left(\frac{\mathrm{c}_{\text {max }} \mathrm{U}_{\mathrm{n}}}{\sqrt{3}}\right. \\
& \left.+\sum_{\mathrm{j}=1}^{\mathrm{n}} \mathrm{Z}_{(1) \mathrm{ij}} \cdot \mathrm{I}_{(1) \mathrm{sk} 2 \mathrm{PFj}}\right)  \tag{4.12}\\
& =I_{\text {k2EL3maxPFO }}^{\prime \prime}+I_{\text {k2EL3PF }}^{\prime \prime} \\
& \mathrm{I}_{\text {kE2Emax }}^{\prime \prime}=\left|\frac{3 \underline{Z}_{(2) \mathrm{ii}}}{\underline{\mathrm{Z}}_{(1) \mathrm{ii}} \underline{\mathrm{Z}}_{(2) \mathrm{ii}}+\underline{\mathrm{Z}}_{(1) \mathrm{ii}} \underline{\mathrm{Z}}_{(0) \mathrm{ii}}+\underline{\mathrm{Z}}_{(2) \mathrm{ii}} \underline{\mathrm{Z}}_{(0) \mathrm{ii}}}\right| \cdot\left(\frac{\mathrm{c}_{\text {max }} U_{\mathrm{n}}}{\sqrt{3}}\right. \\
& \left.+\sum_{\mathrm{j}=1}^{\mathrm{n}} \mathrm{Z}_{(1) \mathrm{ij}} \cdot \mathrm{I}_{(1) \mathrm{sk} 2 \mathrm{PFj}}\right)=\mathrm{I}_{\mathrm{k} 2 \mathrm{E} 2 \operatorname{maxPFO}}+\mathrm{I}_{\mathrm{kE} 2 \mathrm{EPF}}^{\prime \prime} \tag{4.13}
\end{align*}
$$

where

| $\mathrm{I}_{(1) \mathrm{sk2PFj}}$ | is the rms value of the maximum source current (positivesequence system) in case of a line-to-line short circuit at the high-voltage side of the unit transformer, given by the manufacturer; |
| :---: | :---: |
| $\underline{Z}_{(1) \mathrm{ii}}=\underline{Z}_{\text {ii }}$ | is the $\mathrm{i}^{\text {th }}$ diagonal element of the nodal impedance matrix of the positive sequence system, where $i$ is the short-circuit node; |
| $\underline{Z}_{(2) \mathrm{ii}}$ | is the $\mathrm{i}^{\text {th }}$ diagonal element of the nodal impedance matrix of the negative sequence system including the impedances of the power station units with full size converter, where $i$ is the shortcircuit node; |
| $\underline{Z}_{(0) \mathrm{ii}}$ | is the $\mathrm{i}^{\text {th }}$ diagonal element of the nodal impedance matrix of the zero-sequence system, where $i$ is the short-circuit node; |
| $\underline{Z}_{(1) \mathrm{ij}}=\underline{Z}_{\mathrm{ij}}$ | are the elements of the nodal impedance matrix of the positivesequence system, where $i$ is the short-circuit node and $j$ are the nodes where power station units with full size converters are connected. |

Maximum initial Line-to-earth short circuit

$$
\begin{align*}
& I_{\mathrm{k} 1 \max }^{\prime \prime}=\frac{3}{\left|\underline{Z}_{(1) i i}+\underline{Z}_{(2) i i}+\underline{Z}_{(0) i i}\right|} \frac{c_{\max } U_{\mathrm{n}}}{\sqrt{3}} \\
& \quad+\frac{3}{\left|\underline{Z}_{(1) i i}+\underline{Z}_{(2) i i}+\underline{Z}_{(0) i i}\right|} \sum_{j=1}^{n} Z_{(1) i j} \cdot I_{(1) \mathrm{sk} 1 \mathrm{PF} j}  \tag{4.14}\\
& \quad=I_{\mathrm{k} 1 \text { maxPFO }}^{\prime \prime}+I_{\mathrm{k} 1 \mathrm{PF}}^{\prime \prime}
\end{align*}
$$

where
$\mathrm{I}_{(1) \text { sk1PFj }} \quad$ is the rms value of the maximum source current (positivesequence system) in case of a line-to-earth short circuit at the high-voltage side of the unit transformer, given by the manufacturer;
$\underline{Z}_{(1) \mathrm{ii}}=\underline{\mathrm{Z}}_{\mathrm{ii}} \quad$ is the $\mathrm{i}^{\text {th }}$ diagonal element of the nodal impedance matrix of the positive sequence system, where $i$ is the short-circuit node;
is the $\mathrm{i}^{\text {th }}$ diagonal element of the nodal impedance matrix of the negative sequence system including the impedances of the power station units with full size converter, where $i$ is the shortcircuit node;
$\underline{Z}_{(0) \text { ii }}$
$\underline{Z}_{(1) \mathrm{ij}}=\underline{Z}_{\mathrm{ij}}$
$\mathrm{I}_{\mathrm{k} 1 \text { maxPFO }}$
$I_{\text {" } 1 \text { PF }}$
is the $\mathrm{i}^{\text {th }}$ diagonal element of the nodal impedance matrix of the zero-sequence system, where $i$ is the short-circuit node; are the elements of the nodal impedance matrix of the positivesequence system, where $i$ is the short-circuit node and $j$ are the nodes where power station units with full size converters are connected.
is the maximum initial symmetrical short-circuit current calculated by the equivalent voltage source at the short-circuit location without influence of the source currents of the power station units with full size converter;
is the sum of the contributions of wind power station units with full size converter to the initial short-circuit current.

### 4.2.3 Calculation of peak short-circuit current

IEC 60909-0 2016 recommends that for identifying the peak short-circuit current, the initial symmetrical short-circuit current shall first be calculated considering that there are no fuses or current-limiting circuit-breakers to protect the substations, despite the fact that these protection equipment are existing. Afterwards, from the calculated initial symmetrical short-circuit current and characteristic curves of the fuses or current-limiting circuit-breakers, the peak short-circuit current (cut-off current) is determined [112].

### 4.2.3.1 Three-phase short circuit

For single-fed and multiple single-fed short circuits

$$
\begin{equation*}
\mathrm{i}_{\mathrm{p}}=\kappa \sqrt{2} \mathrm{I}_{\mathrm{k}}^{\prime \prime} \tag{4.15}
\end{equation*}
$$

where the factor $\kappa$ can be obtained from the curves or calculated from the following expression

$$
\begin{equation*}
\kappa=1.02+0.98 \mathrm{e}^{-3 \mathrm{R} / \mathrm{X}} \tag{4.16}
\end{equation*}
$$

For contribution of one power station unit with full size, the peak-short circuit current is calculated as follows:

$$
\begin{equation*}
i_{p}=\sqrt{2} I_{k P F}^{\prime \prime}=\sqrt{2} I_{\text {skPF }} \tag{4.17}
\end{equation*}
$$

The peak short circuit current $i_{p}$ at the short-circuit location $F$ that is considered fed from multiple single source, is the sum of the partial short-circuit currents.

$$
\begin{equation*}
\mathrm{i}_{\mathrm{p}}=\sum \mathrm{i}_{\mathrm{pi}} \tag{4.18}
\end{equation*}
$$

For multiple-fed short circuit

$$
\begin{equation*}
\mathrm{i}_{\mathrm{p}}=\kappa \sqrt{2} \mathrm{I}_{\mathrm{kmaxPFO}}^{\prime \prime}+\sqrt{2} \mathrm{I}_{\mathrm{kPF}}^{\prime \prime} \tag{4.19}
\end{equation*}
$$

where
$I_{\text {kmaxPFO }}^{\prime \prime} \quad$ is the maximum initial three-phase short-circuit current without
influence of power station units with full size converter calculated by Formula (4.2);
$\mathrm{I}_{\mathrm{kPF}}^{\prime \prime} \quad$ is the contribution of the power station units with full size converter calculated by Formula (4.9).

The $\kappa$ factor is computed by the same formula (4.16), adopting one of the three following methods (A, B, and C) for identifying the R/X ratio. However, the IEC highly recommends method C.

## Method A: Uniform R/X or X/R

The smallest ratio of $R / X$ or the largest ratio of $X / R$ of all branches of the network is considered. It is essential to select only the branches which carry partial short-circuit currents at the nominal voltage corresponding to the short-circuit location and branches with transformers feeding the voltage level of the short-circuit location. Any branch may be a series combination of several impedances [112].

Method B: Ratio $\mathrm{R} / \mathrm{X}$ or $\mathrm{X} / \mathrm{R}$ at the short-circuit location
For this method, the ratio $1.15 R_{k} / X_{k}$ is used, where the $R_{k} / X_{k}$ ratio is derived from the short-circuit impedance $\underline{Z}_{k}=R_{k}+j X_{k}$ as computed for the initial shortcircuit calculation; and the 1.15 factor is a safety factor to cover an inaccuracies caused from the meshed network complex impedances reduction. In low voltage networks the value of $1.15 \mathrm{R}_{\mathrm{k}} / \mathrm{X}_{\mathrm{k}}$ is limited to 1.8 and in high voltage networks to 2.0. It is not essential to use to 1.15 safety factor if the $\mathrm{R} / \mathrm{X}$ ratio remains smaller than 0.3 in all branches which carry a short-circuit current [112].

Method C: Equivalent Frequency $f_{c}$
This method adopts the equivalent frequency approach. Equivalent impedance $Z_{c}=R_{c}+j X_{c}$ is calculated assuming a source of 20 Hz for 50 Hz systems and 24 Hz systems to excite the network at the fault location. Then, the $\mathrm{R} / \mathrm{X}$ ratio at the fault is determined as follow [112]:

$$
\begin{equation*}
\frac{R}{X}=\frac{R_{c}}{X_{c}} * \frac{f_{c}}{f} \tag{4.20}
\end{equation*}
$$

where

| $Z_{c}=R_{c}+j X_{c}$ | is the equivalent impedance of the system as seen from the <br> short-circuit location for the assumed frequency $f_{c} ;$ |
| :--- | :--- |
| $R_{c}$ | is the real part of $Z_{c}\left(R_{c}\right.$ is generally not equal to the $R$ at <br> nominal frequency $) ;$ |
| $X_{c}$ | is the imaginary part of $Z_{c}\left(X_{c}\right.$ is generally not equal to the <br> $X$ at nominal frequency $).$ |

For a network with power station units with full size converter, the peak short-circuit current can be expressed as follows:
4.2.3.2 Line-to-line short circuit

$$
\begin{equation*}
i_{\mathrm{p} 2}=\kappa \sqrt{2} I_{\mathrm{k} 2 \operatorname{maxPFO}}^{\prime \prime}+\sqrt{2} I_{\mathrm{k} 2 \mathrm{PF}}^{\prime \prime} \tag{4.21}
\end{equation*}
$$

where
$\mathrm{I}_{\mathrm{k} 2 \text { maxPFO }}^{\prime \prime} \quad$ is the maximum initial line-to-line short-circuit current without influence of the source currents of power station units with full size converter calculated according to Formula (4.10);
$\mathrm{I}_{\mathrm{k} 2 \mathrm{PF}}^{\prime \prime} \quad$ is the contribution of the power station units with full size converter calculated according to Formula (4.10).
4.2.3.3 Line-to-line short circuit with earth connection

$$
\begin{equation*}
\mathrm{i}_{\mathrm{p} 2 \mathrm{EL} 2}=\kappa \sqrt{2} \mathrm{I}_{\mathrm{k} 2 \mathrm{EL} 2 \operatorname{maxPFO}}^{\prime \prime}+\sqrt{2} \mathrm{I}_{\mathrm{k} 2 \mathrm{EL} 2 \mathrm{PF}}^{\prime \prime} \tag{4.22}
\end{equation*}
$$

where
$\mathrm{I}_{\mathrm{k} 2 \mathrm{EL} 2 \text { maxPFO }}^{\prime \prime} \quad$ is the maximum initial line-to-line short-circuit current without influence of the source currents of power station units with full size converter calculated according to Formula (4.11);
$I_{\text {k2EL2PF }}^{\prime \prime} \quad$ is the contribution of the power station units with full size converter calculated according to Formula (4.11).
4.2.3.4 Line-to-earth short circuit

$$
\begin{equation*}
\mathrm{i}_{\mathrm{p} 1}=\kappa \sqrt{2} \mathrm{I}_{\mathrm{k} 1 \text { maxPFO }}^{\prime \prime}+\sqrt{2} \mathrm{I}_{\mathrm{k} 1 \mathrm{PF}}^{\prime \prime} \tag{4.23}
\end{equation*}
$$

where

$$
\begin{array}{ll}
\mathrm{I}_{\mathrm{k} 1 \text { maxPFO }}^{\prime} & \text { is the maximum initial line-to-earth short-circuit current without } \\
\text { influence of the source currents of power station units with full } \\
\text { size converter calculated according to Formula (4.14); } \\
\text { is the contribution of the power station units with full size } \\
I_{\mathrm{k} 1 \text { PF }}^{\prime \prime} & \text { converter calculated according to Formula (4.14). }
\end{array}
$$

4.2.4 Calculation of symmetrical breaking current ( $\boldsymbol{I}_{\mathbf{b}}$ )

### 4.2.4.1 Three-phase symmetrical breaking current

In case of multiple fed sources, far from generator faults, the symmetrical breaking current $I_{b}$ is assumed to be equal the maximum initial symmetrical current $I_{k m a x}^{\prime \prime}$

$$
\begin{equation*}
\mathrm{I}_{\mathrm{b}}=\mathrm{I}_{\mathrm{kmax}}^{\prime \prime} \tag{4.24}
\end{equation*}
$$

Similarly, the symmetrical breaking current of power station units with full size converter can be assumed to be equal the steady state short-circuit current ( $\mathrm{I}_{\mathrm{kPFmax}}$ ), in which the $\mathrm{I}_{\mathrm{kPFmax}}$ is provided by the manufacturer.

$$
\begin{equation*}
\mathrm{I}_{\mathrm{b}}=\mathrm{I}_{\mathrm{kPFmax}} \tag{4.25}
\end{equation*}
$$

For multiple single fed short circuits, the $\mathrm{I}_{\mathrm{b}}$ is computed by the summation of individual breaking currents contributions:

$$
\begin{equation*}
\mathrm{I}_{\mathrm{b}}=\sum_{\mathrm{i}} \mathrm{I}_{\mathrm{bi}} \tag{4.26}
\end{equation*}
$$

Symmetrical breaking currents of synchronous and asynchronous machines

## Chapter Four: Short Circuit Calculations

In case of near-to generator, multiple fed short circuits, the symmetrical breaking currents of synchronous and asynchronous machines are respectively given by

$$
\begin{gather*}
\mathrm{I}_{\mathrm{b}}=\mu \mathrm{I}_{\mathrm{kmax}}^{\prime \prime}  \tag{4.27}\\
\mathrm{I}_{\mathrm{b}}=\mu \mathrm{q} \mathrm{I}_{\mathrm{kmax}}^{\prime \prime} \tag{4.28}
\end{gather*}
$$

The factor $\mu$ depends on the minimum time delay $t_{\text {min }}$ and is a function of the ratio $\mathrm{I}_{\mathrm{kG}}^{\prime \prime} / \mathrm{I}_{\mathrm{rG}}$ for the synchronous machines, and $\mathrm{I}_{\mathrm{kM}}^{\prime \prime} / \mathrm{I}_{\mathrm{rM}}$ for the asynchronous machines; where $\mathrm{I}_{\mathrm{rG}}$ and $\mathrm{I}_{\mathrm{rM}}$ are the rated currents of the synchronous and asynchronous machines respectively. Similarly, the factor q depends on the minimum time delay $t_{\text {min }}$, hence, is a function of the ratio $\mathrm{P}_{\mathrm{rM}} / \mathrm{p}$, where the $\mathrm{P}_{\mathrm{rM}}$ is the rated active power in MW and p is the number of pairs of poles of the asynchronous machine. Both factors have specific formulas and diagrams in the IEC standard.

### 4.2.4.2 For unbalanced short-circuits

The short-circuit breaking current is assumed to be equal to the maximum initial short-circuit currents:

$$
\begin{equation*}
\mathrm{I}_{\mathrm{b} 2}=\mathrm{I}_{\mathrm{k} 2 \max }^{\prime \prime} \tag{4.29}
\end{equation*}
$$

4.2.4.3 Line-to-line short circuit with earth connection

$$
\begin{equation*}
\mathrm{I}_{\mathrm{b} 2 \mathrm{E}}=\mathrm{I}_{\mathrm{k} 2 \mathrm{Emax}}^{\prime \prime} \tag{4.30}
\end{equation*}
$$

4.2.4.4 Line-to-earth short circuit

$$
\begin{equation*}
\mathrm{I}_{\mathrm{b} 1}=\mathrm{I}_{\mathrm{k} 1 \max } \tag{4.31}
\end{equation*}
$$

### 4.2.5 Calculation of steady state short-circuit current $\left(\mathbf{I}_{\mathbf{k}}\right)$

### 4.2.5.1 Near-to-generator three-phase short circuits

Contribution of synchronous machines on $\mathrm{I}_{\mathrm{k}}$ depends on the excitation system, the voltage regulator action, and saturation influences, along with the presence of an impedance between the terminals of the machine and the short-circuit location.

Maximum steady-state short circuit current of synchronous machines is calculated as follows:

$$
\begin{equation*}
\mathrm{I}_{\mathrm{kmax}}=\lambda_{\max } \mathrm{I}_{\mathrm{rG}} \tag{4.32}
\end{equation*}
$$

where $\lambda_{\text {max }}$ is a factor that is determined graphically from graphs provided in the IEC standard.
4.2.5.2 Far from generator short circuit,

$$
\begin{equation*}
\mathrm{I}_{\mathrm{k}}=\mathrm{I}_{\mathrm{k}}^{\prime \prime} \tag{4.33}
\end{equation*}
$$

### 4.2.5.3 For unbalanced short-circuits

The steady-state short circuit current is assumed to be equal to the initial short-circuit currents:

$$
\begin{equation*}
\mathrm{I}_{\mathrm{k} 2}=\mathrm{I}_{\mathrm{k} 2}^{\prime \prime} \tag{4.34}
\end{equation*}
$$

4.2.5.4 Line-to-line short circuit with earth connection

$$
\begin{equation*}
\mathrm{I}_{\mathrm{k} 2 \mathrm{E}}=\mathrm{I}_{\mathrm{k} 2 \mathrm{E}}^{\prime \prime} \tag{4.35}
\end{equation*}
$$

4.2.5.5 Line-to-earth short circuit

$$
\begin{equation*}
\mathrm{I}_{\mathrm{k} 1}=\mathrm{I}_{\mathrm{k} 1}^{\prime \prime} \tag{4.36}
\end{equation*}
$$

### 4.3 Short circuit calculations according to ANSI/IEEE standards

The American National Standard Institute (ANSI) standard is a guideline for short circuit calculations for selection of equipment rating (circuit breakers) for electrical networks. This includes C37.010 for systems of nominal voltage above 1 kV , and C37.13 for systems below 1 kV [113], [114]. ANSI methods of short circuit calculations are commonly used all over North America and are widely accepted in many other countries worldwide. All equipment manufactured in the United States or exported to be used in the United States has been meeting or designed according to the ANSI standards requirements.

### 4.3.1 Basic assumptions considered are:

An equivalent voltage source at the fault location, which equals the prefault voltage at the location, replaces all external voltage sources and machine internal voltage sources [115].

All machines are represented by their internal impedances. Line capacitances and static loads are neglected. Transformer taps can be set at either the nominal position or at the tapped position [115]. For 3-phase fault, the fault is bolted, which in turn, arc resistances are not considered [115].

There are three different impedance networks created to calculate momentary, interrupting, and steady-state short circuit currents. These networks are: $1 / 2$ cycle network (subtransient network), 1.5-4 cycle network (transient network), and 30 cycle network (steady-state network) respectively. The $1 / 2$ cycle network is referred to as subtransient network due to the representation of all rotating machines are represented by their subtransient reactance. Similarly, this primarily reason applies for 1.5-4 cycle network and 30 cycle network respectively [115]. Table 4.3 represents the rotating machines reactances considered by the ANSI/IEEE standards for the three different cycle networks.

TABLE 4.3: CLASSIFICATION OF ROTATING MACHINES REACTANCES [115]

| Source type | $1 / 2$ cycle <br> network | $1.5-4$ cycle <br> network | 30 cycle <br> network |
| :--- | :---: | :---: | :---: |
| Utility | $\mathrm{X}^{\prime \prime}$ | $\mathrm{X}^{\prime \prime}$ | $\mathrm{X}^{\prime \prime}$ |
| Turbo generator | $\mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | $\mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | $\mathrm{X}_{\mathrm{d}}^{\prime}$ |
| Hydro-generators |  |  |  |
| With damper | $\mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | $\mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | $\mathrm{X}_{\mathrm{d}}^{\prime}$ |
| Without damper | $0.75 \mathrm{X}_{\mathrm{d}}^{\prime}$ | $0.75 \mathrm{X}_{\mathrm{d}}^{\prime}$ | $\mathrm{X}_{\mathrm{d}}^{\prime}$ |
| Condenser | $\mathrm{X}_{\mathrm{d}}^{\prime}$ | $\mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | - |
| Synchronous motor | $\mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | $1.5 \mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | - |
| Induction Machines |  |  |  |
| Above 1000HP, $1800 \mathrm{r} / \mathrm{min}$ or less | $\mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | $1.5 \mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | - |
| Above 250HP, 3600 r/min | $\mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | $1.5 \mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | - |
| All other above 50 HP | $1.2 \mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | $3.0 \mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | - |
| Below 50 HP | $1.67 \mathrm{X}_{\mathrm{d}}^{\prime \prime}$ | - | - |

$\mathrm{X}_{\mathrm{d}}$ is the positive sequence subtransient reactance of a synchronous machine or locked-rotor reactance of an induction machine ; $\mathrm{X}_{\mathrm{d}}^{\prime}$ is the positive sequence transient reactance of a synchronous machine

ANSI/IEEE Standards recommend the use of separate R and X networks to calculate $R / X$ values. An $R / X$ ratio is obtained for each individual faulted bus and short circuit current. This $\mathrm{R} / \mathrm{X}$ ratio is then used to determine the multiplying factor to account for the system DC offset [115].

In the cases of calculating the asymmetrical value of momentary and interrupting short circuit currents, through using the $1 / 2$ cycle and $1.5-4$ cycle networks respectively, the symmetrical rms value of the momentary and interrupting short circuit currents are initially determined, and then these values are multiplied by the relevant multiplying factors [115].

### 4.3.2 Types of calculations

ANSI standard classifies three basic types of short circuit currents, in which these are associated with three different time periods.

### 4.3.2.1 Calculation of the "first cycle" current

This represent the maximum value of the short circuit current up to and including one cycle immediately after the occurrence of fault, before its AC and DC components decay towards the steady-state value [108], [115]. This type of short circuit current is relevant to and referred to as "momentary" or "closing and latching" duties. Moreover, ETAP has a different identification to this type of current which is referred to as " $1 / 2$ cycle". The ETAP performs 3-phase, line-to-ground, line-to-line, and line-to-line-to-ground fault studies to calculate the short circuit currents in their rms values at $1 / 2$ cycle at the faulted buses. The values of short circuit currents computed by this method are applicable for several purposes such as sizing of fuses and low-voltage circuit breakers, and adjusting relay instantaneous settings.

The following procedure to calculate the momentary short circuit current [115]:
Calculates the symmetrical rms value of momentary short circuit current as provided

$$
\begin{equation*}
\mathrm{I}_{\mathrm{mom}, \mathrm{rms}, \mathrm{symm}}=\frac{\mathrm{V}_{\text {pre-fault }}}{\sqrt{3} \mathrm{Z}_{\mathrm{eq}}} \tag{4.37}
\end{equation*}
$$

where the $\mathrm{Z}_{\mathrm{eq}}$ is the equivalent impedance at the faulted bus from the $1 / 2$ cycle network

Calculates the asymmetrical rms value of momentary short-circuit current as follows

$$
\begin{equation*}
\mathrm{I}_{\mathrm{mom}, \mathrm{rms}, \mathrm{asymm}}=\mathrm{MF}_{\mathrm{m}} \mathrm{I}_{\mathrm{mom}, \mathrm{rms}, \mathrm{symm}} \tag{4.38}
\end{equation*}
$$

where $\mathrm{MF}_{\mathrm{m}}$ is the momentary multiplying factor, given as

$$
\begin{equation*}
M F_{m}=\sqrt{1+2 e^{-\frac{2 \pi}{X / R}}} \tag{4.39}
\end{equation*}
$$

Calculates the peak value of momentary short-circuit current as follows:

$$
\begin{equation*}
\mathrm{I}_{\text {mom,peak }}=\mathrm{MF}_{\mathrm{p}} \mathrm{I}_{\mathrm{mom}, \mathrm{rms}, \mathrm{symm}} \tag{4.40}
\end{equation*}
$$

where the $\mathrm{MF}_{\mathrm{p}}$ is the peak multiplying factor, given as

$$
\begin{equation*}
M F_{p}=\sqrt{2}\left(1+e^{-\frac{2 \pi}{X / R}}\right) \tag{4.41}
\end{equation*}
$$

It is to be noted that the generators and motors are represented by their positive, negative, and zero sequence subtransient reactance.

### 4.3.2.2 Calculation of the interrupting current

This represents the breaking current for medium and high-voltage circuit breaker parting times, relevant for the time period ranging from 1.5 to 4 cycles. ETAP perform 3-phase, line-to-ground, line-to-line, and line-to-line-to-ground fault studies to calculate short circuit currents in their rms values between 1.5 to 4 cycles at faulted buses. Generators are modelled by their positive, negative, and zero sequence subtransient reactance, and motors are modelled by their positive, negative, and zero sequence transient reactance.

The following procedure to calculate the interrupting short circuit current:

Calculates the symmetrical rms value of the interrupting short circuit current as provided:

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$$
\begin{equation*}
\mathrm{I}_{\mathrm{int}, \mathrm{rms}, \mathrm{symm}}=\frac{\mathrm{V}_{\mathrm{pre}-\mathrm{fault}}}{\sqrt{3} \mathrm{Z}_{\mathrm{eq}}} \tag{4.42}
\end{equation*}
$$

where the $\mathrm{Z}_{\text {eq }}$ is the equivalent impedance at the faulted bus from the $1.5-4$ cycle network

Calculate the short circuit current contributions to the fault location from the surrounding buses.

The ANSI/IEEE standard distinguishes between generating sources contribution to short circuit currents depending on location, denoted as either remote or local sources.

Fault fed from remote sources
It is considered a remote source contribution to a short circuit current when the short circuit current is fed from generator through two or more transformations, or with a per unit reactance external to the generator that is equal to or exceed 1.5 times the generator per unit subtransient reactance on a common MVA base. Hence, the effect of ac decay is not considered [110].

The symmetrical value is corrected by the multiplying factor of $M F_{r}$, where the factor $M F_{r}$ can be manipulated from standard figures available in ANSI/IEEE C37.010 for several typical contact parting times, though these figures only for half cycle tripping decay(low contact parting time). For higher contact parting time, the remote contributions multiplying factor is calculated as follows:

$$
\begin{equation*}
\mathrm{MF}_{\mathrm{r}}=\sqrt{1+2 \mathrm{e}^{-\frac{4 \pi}{\mathrm{X} / \mathrm{R}} \mathrm{t}}} \tag{4.43}
\end{equation*}
$$

where $t$ is the circuit breaker contact parting time in cycles

## Fault fed from local sources

It is considered local source contribution, when the short circuit current is fed from generators through no more than one transformation, or with a per unit external
reactance in series to the generator, which is less than 1.5 times the generator subtransient reactance. Thus, the effect of ac and dc decays is considered.

The symmetrical value is corrected by the factor of $\mathrm{MF}_{1}$. The determination of local contributions multiplying factor is similar to the $\mathrm{MF}_{\mathrm{r}}$ obtained from curves available in ref. [108].

For a system with several short circuit sources, determine the total remote contributions and total local contribution, through the NACD ratio

No AC Decay (NACD) ratio
The NACD ratio is defined as "the remote contributions to the total contributions for the short circuit current at a given location" [115]

It is calculated in ETAP as follows:

$$
\begin{equation*}
\mathrm{NACD}=\frac{\mathrm{I}_{\text {remote }}}{\mathrm{I}_{\text {total }}} \tag{4.44}
\end{equation*}
$$

where,

$$
\begin{equation*}
\mathrm{I}_{\text {total }}=\mathrm{I}_{\text {remote }}+\mathrm{I}_{\text {local }} \tag{4.45}
\end{equation*}
$$

Calculate the actual multiplying factor $\left(\mathrm{AMF}_{\mathrm{i}}\right)$

$$
\begin{equation*}
\mathrm{AMF}_{\mathrm{i}}=\mathrm{MF}_{\mathrm{l}}+\mathrm{NACD}\left(\mathrm{MF}_{\mathrm{r}}-\mathrm{MF}_{1}\right) \tag{4.46}
\end{equation*}
$$

Determine the adjusted rms interrupting short-circuit current using the following formula

$$
\begin{equation*}
\mathrm{I}_{\mathrm{int}, \mathrm{rms}, \mathrm{adj}}=A M F_{\mathrm{i}} \mathrm{I}_{\mathrm{int}, \mathrm{rms}, \mathrm{symm}} \tag{4.47}
\end{equation*}
$$

### 4.3.2.3 Calculation of the steady state short circuit currents

These represent the short circuit currents after 30 cycles and beyond from the moment of fault occurrence. These currents are also called time-delayed currents; this is relevant to the duration after the opening time of medium voltage circuitbreaker, despite the intentional time delay [108].

ETAP perform 3-phase, line-to-ground, line-to-line, and line-to-line-to-ground fault studies to calculate short circuit currents in their rms values at 30 cycles at faulted buses, which are considered the minimum short-circuit current values.

Generators are modelled by their positive, negative, and zero sequence reactance, and short circuit current contributions from induction machines, synchronous motors, and condensers are ignored [115].

### 4.4 ANSI/IEEE standard vs IEC standard

Basically, ANSI and IEC standards were developed to provide conservative results through detailed techniques for the short circuit current calculations for the determination of protection equipment ratings. Despite the same aims and objectives of the two standards, there are rarely common similarities between ANSI and IEC standards for the short circuit calculations. Both standards recognize the principal figure representing the short circuit current against the time, the rapid dc decay, and the ac component decay, though the AC and DC decays modellings are different. It is generally described that the IEC standard is a correction factors based calculation, whereas the ANSI standard is an impedance based calculation [113]. The IEC requires the calculation of the symmetrical initial current in order to calculate the other types of short circuit currents, and applies correction factors. However, ANSI is concerned with type of reactance considered for the calculation of each short circuit current. The main differences between the two counterparts methods are provided as follows in Table 4.4.

TABLE 4.4: COMPARISON BETWEEN IEC STANDARD AND ANSI STANDARD

| Characteristic | IEC | ANSI |
| :---: | :---: | :---: |
| System Frequency | 50 or 60 Hz | 60 Hz |
| Voltage Source | Equivalent voltage source, function of the system nominal voltage multiplied by c factor, depending on the system voltage level | Rated system voltage |
| Network Configuration | Classified into meshed and non-meshed networks, where certain multiplying factors and $\mathrm{X} / \mathrm{R}$ ratios are selected accordingly | Classified into three fault cycles networks to be selected depending on the purpose of the calculation: $1 / 2$ network; 1.5-4cycle network; 30 cycle network |
| Equipment Impedances | the network equipment impedances (generators, transformers, and power station units) are multiplied by correction factors | The machines impedances are categorized into transient and subtransient. |
| Location of rotating machines | Near and far sources Location of the rotating equipment from the fault point is significant for the breaking and steady state short circuit currents calculations | Remote and local sources Location of the generator is considered only if there are two transformers between the fault location and the generator or if the transfer (in between the fault location and the generator) reactance is 1.5 times greater than the generator reactance. Otherwise, it is considered local. |
| SC Current calculation methodology | The contribution of sc currents from each source is calculated ; and then the superposition is applied to calculate the total sc current | Applies Thevinin method where the network impedance is reduced and finally calculates the sc current |

### 4.5 Summary

In this chapter, the IEC and ANSI standards procedures for short circuit calculations have been presented. The main conceptual differences between IEC and ANSI have been described. Both procedures provide detailed modelling for the short circuit calculations, however, IEC requires more detailed power system data to be available

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than ANSI. The ANSI standard is concerned with the machines impedances, where multiplying factors are applied to ensure secure reliable results. The IEC standard is concerned with the initial short circuit current contribution of each source separately. Moreover, IEC distinguishes between the radial and loop network contribution, while ANSI does not consider this issue. IEC differentiates in the calculations between the sources location near or far from the short circuit point; however, ANSI only considers the generator to be remote or local depending on the transformation impedance value between the generator and the short circuit location.

## Chapter Five

## 5 IEEE 13 Bus Distribution Test System

### 5.1 Introduction

In this chapter, the main objective is to analyse the simulated results for the ANSI and IEC calculations. The analysis aim is to assess the impact of DG type, location and penetration level on the short circuit current of the distribution system under study. The short circuit currents magnitudes of the system under study with no DG connected are considered as reference inorder to be able to assess the impact of DG integration. Moreover, a comparison between the IEC simulated results and ANSI simulated results will be presented inorder to ensure valid and reliable results. Also, it is necessary to distinguish the competence between the two methods for short circuit calculations.

This chapter is divided into seven main sections. First, section 5.1 is an introduction and outline to the chapter. Section 5.2 will provide the main characteristics for the system under study. Section 5.3 will illustrate the case studies examined. Section 5.4 will present the ANSI simulated results and comprehensive analysis to the results. Similarly, section 5.5 will present and provide detailed analysis to the IEC simulated results. Section 5.6 will compare between the IEC and ANSI simulated results. Last, section 5.7 will provide a conclusion and recommendations.

### 5.2 System under study

The distribution test system used in this study is the IEEE 13-bus. The single line diagram is shown in Figure 5.1. The system elements full data are provided in Appendix A. This system is described as small test feeder operating at 4.16 kV ; however, it displays wide variety of components and characteristics that include:

1. Short and relatively highly loaded for a 4.16 kV feeder
2. One substation voltage regulator consisting of three single-phase units connected in wye
3. Overhead and underground lines with variety of phasing
4. Shunt capacitor banks
5. In-line transformer
6. Unbalanced spot and distributed loads [116]


Figure 5.1 IEEE 13 Bus Distribution Test System Single Line Diagram
This system has been selected for initial investigation to examine the performance of a small scale (in terms of voltage and MW rating) unbalanced distribution system during short circuit when different types of DG are connected at various penetration levels up to $85 \%$ of the system rated generation. This is to determine and identify the implications in small system and obtain basic understanding. The model is implemented and modified in ETAP 12 software, where the short circuit analysis is performed for different four cases presented in section 5.3. The short circuit analysis is run twice to include the two different simulations which are: ANSI and IEC
calculations methods. The IEEE 13-bus distribution test system original model is modified through connecting DG with various sizes and at different locations throughout the system under study. The DG units used are; Type 3 (DFIG) wind turbine generators (WTG), photovoltaics (PV), and diesel generators.

### 5.3 IEEE-13 bus distribution test system case studies

The study is divided into four main case studies to examine the impact of different DG types on different types of fault of distribution system under study. The four cases of different DG units connected to the system under study are:

Case 1: Wind
Case 2: PV

Case 3: Hybrid system (Wind and PV)
Case 4: Diesel Hybrid system (Diesel generator Wind, and PV)
For each case study, there are four different scenarios selected to study the impact of DG location on the short circuit level of the distribution system presented in Table 5.1.

TABLE 5.1: DIFFERENT SCENARIOS EXAMINED

| Scenario | Condition |
| :--- | :--- |
| Scenario 1 (S1) | No DG |
| Scenario 2 (S2) | 3 MW placed at Bus 632 |
| Scenario 3 (S3) | 3 MW at Bus 675 |
| Scenario 4 (S4) | 2x1.5 MW placed at buses 632 and 671 |

In cases 3 and 4 (where there are different types of DG units connected), the DG units ratings were equal. As in case 3, for S2 and S3, a 1.5 MW WTG and a 1.5 MW PV array were connected. The scenarios are varied to obtain valid and reliable results. The simulation involved examination of the occurrence of four types of fault which are 3-ph, LG, LL, and LLG at three different buses 632, 671, 675 respectively. The criterion for selection of buses where the fault may occur and DG location is based on the distance from the main utility grid and the concentration of loads. In which S2 represents the DG location near the utility grid. For the same DG capacity,

S3 represents the DG location at the furthest bus from the utility grid. Though, S4 represents the distribution of the DG capacity between two buses away from the utility grid and in the middle of the system. The evaluation of the simulation results is based on comparing the short circuit current magnitudes at each scenario with the SCC in case of no DG connected (S1) to the system under study.

### 5.4 Simulated results for ANSI calculations

The study selected for the short circuit calculation is $1.5-4$ cycles. This study performs 3-phase, line-to-ground, line-to-line, and line-to-line-to-ground fault studies per ANSI Standards. The study calculates short circuit currents in their rms values between 1.5 to 4 cycles at faulted buses. In this study, generators are represented by their positive, negative, and zero sequence subtransient reactance, and motors are modelled by their positive, negative, and zero sequence transient reactance [115]. The simulated results are presented in Tables $5.2-5.5$. The results are presented in this arrangement order to compare between the DG types, in regards their impact on the short circuit current, along with the influence of different DG location. Table 5.6 presents the impact of different penetration levels varied from $10 \%$ up to $85 \%$ for case 4 at S3.

### 5.4.1 Analysis of simulated results for ANSI calculations

Table 5.2 presents the simulated results for the short circuit current magnitudes of the system under study at no DG connected.

TABLE 5.2: ANSI SIMULATED RESULTS FOR SCENARIO 1 WITH NO DG INSTALLED (KA)

| Bus |  | No DG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | 3-Ph | LG | LL | LLG |
| 632 | 4.16 | 11.276 | 8.463 | 9.766 | 10.631 |
| 671 | 4.16 | 6.453 | 4.536 | 5.588 | 5.903 |
| 675 | 4.16 | 5.771 | 4.181 | 4.998 | 5.277 |

From Table 5.2, it is observed that the results for 3-ph fault case are the highest values in comparison to the other types of faults examined. Therefore, this could be considered as the most severe case in which could be selected to illustrate the short circuit current characteristics of the system with no DG connected. Hence, it is crucial to analyse the main short circuit contributors to this system, especially on the

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same buses where the DG is anticipated to be connected in further studies in this thesis.

TABLE 5.3: ANSI SIMULATED RESULTS FOR SCENARIO 2

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 632 | 4.16 | 13.318 | 9.337 | 11.967 | 12.844 | 11.494 | 8.534 | 9.954 | 10.685 | 12.392 | 8.948 | 10.950 | 11.760 | 12.793 | 10.673 | 11.249 | 12.267 |
| 671 | 4.16 | 6.922 | 4.717 | 6.083 | 6.398 | 6.510 | 4.554 | 5.638 | 5.921 | 6.720 | 4.640 | 5.868 | 6.170 | 6.809 | 4.889 | 5.934 | 6.254 |
| 675 | 4.16 | 6.143 | 4.333 | 5.389 | 5.657 | 5.807 | 4.193 | 5.029 | 5.298 | 5.979 | 4.267 | 5.216 | 5.479 | 6.054 | 4.476 | 5.271 | 5.564 |

TABLE 5.4: ANSI SIMULATED RESULTS FOR SCENARIO 3

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 632 | 4.16 | 12.577 | 9.010 | 11.103 | 11.936 | 11.435 | 8.514 | 9.903 | 10.670 | 12.028 | 8.787 | 10.545 | 11.360 | 12.283 | 9.491 | 10.730 | 11.713 |
| 671 | 4.16 | 8.423 | 5.203 | 7.681 | 7.954 | 6.644 | 4.599 | 5.754 | 6.089 | 7.516 | 4.922 | 6.712 | 6.956 | 7.923 | 6.657 | 7.017 | 7.652 |
| 675 | 4.16 | 7.813 | 4.910 | 7.190 | 7.482 | 6.014 | 4.268 | 5.209 | 5.571 | 6.886 | 4.606 | 6.178 | 6.409 | 7.286 | 6.405 | 6.478 | 7.034 |

TABLE 5.5: ANSI SIMULATED RESULTS FOR SCENARIO 4

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 632 | 4.16 | 13.030 | 9.217 | 11.639 | 12.502 | 11.464 | 8.524 | 9.928 | 10.675 | 12.361 | 8.939 | 10.923 | 11.748 | 12.342 | 10.121 | 10.893 | 11.812 |
| 671 | 4.16 | 7.731 | 5.001 | 6.962 | 7.268 | 6.579 | 4.576 | 5.697 | 5.991 | 6.783 | 4.659 | 5.923 | 6.178 | 7.220 | 5.855 | 6.403 | 6.823 |
| 675 | 4.16 | 6.768 | 4.569 | 6.062 | 6.303 | 5.847 | 4.208 | 5.063 | 5.370 | 6.079 | 4.300 | 5.303 | 5.578 | 6.365 | 5.283 | 5.626 | 6.012 |

TABLE 5.6: ANSI SIMULATED RESULTS FOR SCENARIO 3 AT DIFFERENT PENETRATION LEVELS AND DIESEL HYBRID MIX LOCATED AT BUS 675

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 632 | 4.16 | 12.283 | 9.491 | 10.730 | 11.713 | 11.714 | 9.034 | 10.225 | 11.132 | 11.589 | 8.886 | 10.095 | 10.989 | 11.400 | 8.650 | 9.891 | 10.771 |
| 671 | 4.16 | 7.923 | 6.657 | 7.017 | 7.652 | 7.049 | 5.616 | 6.221 | 6.645 | 6.872 | 5.309 | 6.034 | 6.419 | 6.615 | 4.867 | 5.753 | 6.098 |
| 675 | 4.16 | 7.286 | 6.405 | 6.478 | 7.034 | 6.384 | 5.286 | 5.650 | 6.083 | 6.201 | 4.966 | 5.456 | 5.838 | 5.936 | 4.512 | 5.166 | 5.479 |

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Table 5.7 presents the contribution of equipment installed in the system to 3 -ph short circuit currents when a fault occurs at 632,675 , and 671 respectively.

TABLE 5.7: THREE-PHASE SHORT CIRCUIT CURRENT MAGNITUDES (KA) AND PERCENTAGE OF THE TOTAL SHORT CIRCUIT CURRENT

| Faulted Bus | 632 |  | 675 |  | 671 |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 11.276 |  | 5.771 |  | 6.453 |  |
|  | SCC (kA) | $\%$ | SCC (kA) | $\%$ | SCC (kA) | $\%$ |
| Utility Grid U1 | 9.864 | 87.5 | 4.385 | 76.0 | 4.957 | 76.8 |
| Line 5 | 1.247 | 11.1 | 4.467 | 77.4 | 5.049 | 78.2 |
| Lump 1 | 1.047 | 9.3 | 0.466 | 8.1 | 0.526 | 8.2 |
| Lump 6 | 0.695 | 6.2 | 0.7 | 12.1 | 0.791 | 12.3 |
| Lump 3 | 0.497 | 4.4 | 0.572 | 9.9 | 0.565 | 8.8 |
| Cable 606_500 | 0.497 | 4.4 | 5.213 | 90.3 | 0.565 | 8.8 |
| switch | 0.497 | 4.4 | 5.213 | 90.3 | 0.565 | 8.8 |
| Line 2 | 0.121 | 1.1 | 0.054 | 0.9 | 0.061 | 1.0 |
| Transformer T1 | 0.121 | 1.1 | 0.054 | 0.9 | 0.061 | 1.0 |
| Lump 10 | 0.063 | 0.6 | 0.028 | 0.5 | 0.032 | 0.5 |
| Lump 11 | 0.056 | 0.5 | 0.056 | 1.0 | 0.063 | 1.0 |

The contribution of other loads in the system is not included in the results in Table 5.7. This is due to the ANSI standard assumption in which load currents could be neglected as they are much smaller than the fault currents. Therefore, it can be concluded that static loads have no significant contribution to the short circuit current.

From the short circuit analysis performed, it was concluded that the utility grid has significantly contributed to the short circuit current at the three different faulted buses 632,675, and 671 respectively for all type of faults examined. Whereas for 3ph fault at faulted bus 632, the total simulated symmetrical short circuit current is 11.276 kA , of which the utility grid (U1) contributed 9.864 kA . Thus, is approximately 87\% of the total 3-ph short circuit current at bus 632 .

The five motors ( Lump 1, Lump 3, Lump 6, Lump 10, and lump 11) connected to the system have contributed to total short circuit currents at the faulted buses 632,675 , and 671 respectively for all types of fault. The location of motors in regards to the fault location has varied the SCC results considerably. From table 5.25, it is observed for Lumps 3 and 6, which are connected directly to the buses 675 and 671
respectively, that their contributions to SCC to these buses when a fault occurs are higher than their contribution on SCC at faulted bus 632. This could be due to the series impedances considered of the line 5 and the cable 606_500 connected between bus 632 and lumps 3 and 6 . It should be not that the line and cable resistances are proportional of the conductor length (i.e. 2000 ft . for Line 5).

From Tables 5.3-5.5

The simulated results show that the maximum short circuit current magnitudes occurred in the following descending order at faulted buses 632, 671, and 675 respectively. It can be observed that the SCCs at faulted bus 632 is approximately double the SCCs at faulted buses 671 and 675. In addition, the short circuit current magnitudes for the four types of faults tested decremented order in which the 3-ph fault current values are the highest; LL-G; LL; and the lowest are the LG fault current magnitudes, respectively.

### 5.4.1.1 Impact of DG type on short circuit current

For the three scenarios examined S2, S3, and S4, it is noticed that the short circuit currents magnitudes were the highest in case of WTGs are connected to the distribution network. The WTG impact on short circuit current magnitudes is the highest for all types of fault studied and all faulted buses examined 632, 675, and 671 respectively. The diesel hybrid followed the WTGs in the significant impact on SCC, then the hybrid. Conversely, the impact of PV on short circuit current is observed to be the least, for all types of fault and faulted buses tested.

Further analysis in case 3 for 3 -ph fault simulation results has been performed to ensure reliable assessment. The contribution of each DG type separately on the fault current of the IEEE 13-bus distributed test system is considered. Simulated results from the short circuit study were taken and the percentage of DG contribution of total fault current at its allocated bus has been calculated, presented in Tables 5.8 and 5.9.

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TABLE 5.8: COMPARISON OF DG UNITS CONTRIBUTION ON THE SHORT CIRCUIT CURRENT LEVEL AT S2

| Faulted Bus | \%U1 | \%WTG | \%PV | \%Diesel Generator |
| :---: | :---: | :---: | :---: | :---: |
| 632 | 77.1 | 5.5 | 0.2 | 6.7 |
| 671 | 67.7 | 4.9 | 0.1 | 5.9 |
| 675 | 67.0 | 4.8 | 0.1 | 5.8 |

TABLE 5.9: COMPARISON BETWEEN DG UNITS CONTRIBUTION ON THE SHORT CIRCUIT CURRENT AT S3

| Faulted Bus | \%U1 | \%WTG | \%PV | \%Diesel Generator |
| :---: | :---: | :---: | :---: | :---: |
| 632 | 80.3 | 4.3 | 0.1 | 5.2 |
| 671 | 62.6 | 8.6 | 0.3 | 10.4 |
| 675 | 60.2 | 9.7 | 0.3 | 11.8 |

The utility grid contribution has the highest percentage of the total short circuit current, exceeding more than $50 \%$ in both scenarios S2 and S3 respectively, in comparison to the percentage contribution of the DG types connected. The highest percentage reached up to $80.3 \%$ in Scenario 3 at the occurrence of 3-ph fault at bus 632. Remarkably, it is almost double the percentage for the same conditions at scenario 2. The DFIG wind turbine contribution never exceeded the $10 \%$ in both scenarios. The PV contribution ranged from $0.1-0.3 \%$ in both scenarios 2 and 3. It is noticed that when the DG mix was located at the nearest bus to the grid (bus 632) the grid contribution was higher in Scenario 2 than scenario 3, for faults occurring at buses 671 , and 675 [2].

For S2 and S3, it could be observed that the diesel generators connected contributed more that the WTG and PV. The induction and synchronous machines connected on a system remain to supply current to the fault during short circuit due to the limited amount of stored flux in the machine. However, the current decays significantly with time due to the reduction in this stored energized field [108]. The diesel generator connected the system under study adopts the synchronous machine characteristics and behaviour during short circuit, in which it maintains the stored flux for more cycles resulting in higher symmetrical SCC more than the induction machines. Moreover, the WTG installed in the system under study is DFIG that is equipped with power electronics which controls SCC.

### 5.4.1.2 Impact of DG location on short circuit current

In this section, it is intended to compare between the short circuit current magnitudes in terms of the DG location impact. From Tables $5.3-5.5$, it is noticed that for the four types of fault examined, the results reflected the same performance for the different types of DG integrated in respect to same location. The maximum SCC usually occurred at scenario S2 (in which the DG is located at bus 362) and the faulted bus 632. The minimum SCC usually occurred at scenario 3 (in which the DG is located at bus 675). It is noticed that scenario S 4 is in the intermediate between S 2 and S3. Furthermore, the results demonstrated that in the case of PV is integrated to the distribution network, the SCC magnitudes could be considered approximately equal in the three scenarios examined.

### 5.4.1.3 Worst case scenarios for ANSI calculations

From Tables 5.2 - 5.5, the overall worst 10 cases occurred at the system under study have been selected for 3-ph and LL-G faults, and presented in Figures 5.2 and 5.3. The LL-G fault currents are the highest of the faulted line currents examined. Hence, the LL-G fault current has been presented to represent the worst case scenario of the faulted line currents. It is noticed that all of the worst case scenarios have occurred at bus 632 for the two types of fault respectively.


Figure 5.1. The worst cases during 3-ph fault for ANSI calculations

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Figure 5.2. The worst cases during LL-G fault for ANSI calculations
From Figures 5.2 and 5.3, it is observed that the worst case for both fault types is at the case of wind at scenario two (S2). The least DG impact is the PV at scenario two (S2). In comparing the scenarios that reflect the impact of DG location on the system short circuit level, it is noticed that scenario 2 represented the worst location a DG could be located for all types of DG used and DG mix applied in this study. Wind is the worst DG type regardless of the three scenarios S2, S3, and S4 that have been tested respectively. Similarly, the DG mixes are among the critical cases for the three scenarios.

### 5.4.1.4 Lowest case scenarios for ANSI calculations

From Tables $5.2-5.5$, the least short circuit currents occurred during the 3-ph and LL-G faults inorder to be able to identify the most appropriate DG type and their suitable locations for the 13 bus distribution system studied in this thesis. These types of faults are selected based on the previous analysis discussed earlier, where the highest values of short circuit currents occurred. The results for the lowest short circuit currents during the 3-ph and LL-G faults are represented in Figure 5.4and 5.5.

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Figure 5.3 The minimum short circuit currents during 3-ph fault for ANSI calculations


Figure 5.4 The minimum short circuit currents during LL-G fault for ANSI calculations
It is observed that the two figures are not identical in terms of the type of DG and scenarios sequence. The least SCC achieved when a fault occurred at buses 675 and 671 respectively. Both figures have the least SCC in case of no DG at scenario S1 when a fault occurred at bus 675. It is noticed that the PV for all scenarios studied during the fault occurrence at bus 675 is the most DG type sustained the system SCC to a minimum.

In Figures 5.4 and 5.5, it could be observed that the minimum short circuit currents were at the case where 3-ph and LL-G faults occurring at bus 675 with all types and

DG mix tested in scenario S2 (DG located at bus 632). In Figure 5.5, this figure shows that system SCC could be improved if the DG are located at certain locations.

### 5.4.1.5 Impact of DG penetration level

Figure 5.6 presents the impact of different penetration levels of diesel hybrid DG during the occurrence of 3-ph faults at buses 632,675, and 671 respectively.


Figure 5.5 Penetration level vs 3-ph short circuit currents for diesel hybrid mix located at bus 675 for ANSI calculations

It is noticed that the short circuit currents are directly proportional to the penetration level, as the penetration level increases the short circuit currents increases. The maximum increase calculated between the $85 \%$ penetration level and the no DG level is found to be $8.9 \%$ higher at faulted bus 632. The difference between SCC during a fault at bus 632 and fault at buses 675 and 671 is observed to be about the double. The short circuit currents are the highest at faulted bus 632, followed by 671, and least at faulted bus 675.

### 5.5 Analysis of simulated results for IEC calculations

The simulated results for IEC standard are different than the ANSI standard results in regards to the different types of prospective short circuit current that should be calculated. These are: initial symmetrical current ( $\left(\mathrm{I}_{\mathrm{k}}^{\prime \prime}\right)$; peak short circuit current $\left(\mathrm{i}_{\mathrm{p}}\right)$; symmetrical short-circuit breaking current ( $\mathrm{I}_{\mathrm{b}}$ ); and steady-state short circuit current ( $\mathrm{I}_{\mathrm{k}}$ ). The computation is set to calculate the maximum short circuit currents which determine the capacity or rating of electrical equipment (IEC). In this thesis, the main principal is to calculate the short circuit current to evaluate the system performance during short circuit with DG integration. The minimum short circuit currents are calculated for selection of fuses and for setting of protectives devices. Furthermore, The IEC condition for calculating the minimum short circuit currents is to neglect the contribution of wind power stations, PV units and motors, which is out of the scope of this study.

The LG, LL, LLG, \& 3-Phase Faults (IEC 60909) study is selected in ETAP 12 for the short circuit calculation. This study performs line-to-ground, line-to-line, line-to-line-to-ground, and three-phase fault studies per IEC 60909 Standard. The study calculates initial symmetrical rms, peak and symmetrical breaking rms, and steadystate rms short-circuit currents at faulted buses. However, the symmetrical breaking rms current for the 3-ph fault is not considered by ETAP in this study. ETAP 12 models the generators by their positive, negative, and zero sequence reactance, while motors are modelled by their locked-rotor impedance [115]. The IEC standard considers an equivalent voltage source at the faulted bus for the initial symmetrical current calculation. The voltage factor $c$ value varies depending on the system rated voltage. For the system under study ( 4.16 kV rated voltage), the $c$ factor is selected to be 1.10 according to IEC-909606. According to IEC classification to types of circuits during short circuit, the system under study in this chapter could be considered as multiple fed short-circuit.

The simulated results for the system at no DG connected are presented in Table 5.10. For the same system with different types of DG connected (Wind, PV, Hybrid, and diesel hybrid respectively) considering different scenarios, these simulated results are presented in Tables 5.11-5.22.

TABLE 5.10: IEC SIMULATED RESULTS FOR SCENARIO 1- NO DG

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 12.291 | 24.162 | 9.864 | 8.984 | 17.662 | 8.984 | 8.984 | 10.644 | 20.925 | 10.644 | 10.644 | 11.536 | 22.679 | 11.536 | 11.536 |
| 671 | 4.16 | 7.714 | 15.914 | 5.237 | 5.139 | 10.602 | 5.139 | 5.139 | 6.680 | 13.782 | 6.680 | 6.680 | 7.026 | 14.495 | 7.026 | 7.026 |
| 675 | 4.16 | 6.906 | 13.562 | 4.733 | 4.751 | 9.330 | 4.751 | 4.751 | 5.981 | 11.745 | 5.981 | 5.981 | 6.284 | 12.341 | 6.284 | 6.284 |

TABLE 5.11: IEC SIMULATED RESULTS FOR SCENARIO 2 - WIND

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 15.729 | 32.707 | 9.864 | 10.067 | 20.934 | 10.067 | 10.067 | 13.614 | 28.308 | 13.614 | 13.614 | 14.602 | 30.362 | 14.602 | 14.602 |
| 671 | 4.16 | 8.514 | 17.902 | 5.237 | 5.364 | 11.278 | 5.364 | 5.364 | 7.372 | 15.500 | 7.372 | 7.372 | 7.731 | 16.256 | 7.731 | 7.731 |
| 675 | 4.16 | 7.526 | 14.884 | 4.733 | 4.937 | 9.765 | 4.937 | 4.937 | 6.516 | 12.888 | 6.516 | 6.516 | 6.817 | 13.483 | 6.817 | 6.817 |

TABLE 5.12: IEC SIMULATED RESULTS FOR SCENARIO 3 - WIND

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}{ }^{\prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}{ }^{\prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}{ }^{\prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}{ }^{\text {a }}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 14.053 | 27.816 | 9.864 | 9.569 | 18.941 | 9.569 | 9.569 | 12.167 | 24.083 | 12.167 | 12.167 | 13.059 | 25.849 | 13.059 | 13.059 |
| 671 | 4.16 | 10.899 | 23.043 | 5.237 | 5.906 | 12.486 | 5.906 | 5.906 | 9.432 | 19.940 | 9.432 | 9.432 | 9.775 | 20.6667 | 9.775 | 9.775 |
| 675 | 4.16 | 10.347 | 22.123 | 4.733 | 5.610 | 11.995 | 5.610 | 5.610 | 8.952 | 19.141 | 8.952 | 8.952 | 9.324 | 19.936 | 9.324 | 9.324 |

TABLE 5.13: IEC SIMULATED RESULTS FOR SCENARIO 4 - WIND

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 15.068 | 30.666 | 9.864 | 9.876 | 20.099 | 9.876 | 9.876 | 13.040 | 26.538 | 13.040 | 13.040 | 13.987 | 28.465 | 13.987 | 13.987 |
| 671 | 4.16 | 9.881 | 21.140 | 5.237 | 5.695 | 12.183 | 5.695 | 5.695 | 8.550 | 18.291 | 8.550 | 8.550 | 8.918 | 19.079 | 8.918 | 8.918 |
| 675 | 4.16 | 8.542 | 16.902 | 4.733 | 5.207 | 10.303 | 5.207 | 5.207 | 7.392 | 14.626 | 7.392 | 7.392 | 7.676 | 15.188 | 7.676 | 7.676 |

TABLE 5.14: IEC SIMULATED RESULTS FOR SCENARIO 2 - PV

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 12.526 | 24.349 | 10.120 | 9.056 | 17.603 | 9.056 | 9.056 | 10.848 | 21.087 | 10.848 | 10.848 | 11.597 | 22.542 | 11.597 | 11.597 |
| 671 | 4.16 | 7.778 | 15.970 | 5.315 | 5.157 | 10.588 | 5.157 | 5.157 | 6.736 | 13.831 | 6.736 | 6.736 | 7.047 | 14.468 | 7.047 | 7.047 |
| 675 | 4.16 | 6.944 | 13.578 | 4.788 | 4.763 | 9.313 | 4.763 | 4.763 | 6.014 | 11.759 | 6.014 | 6.014 | 6.288 | 12.295 | 6.288 | 6.288 |

TABLE 5.15: IEC SIMULATED RESULTS FOR SCENARIO 3 - PV

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 12.429 | 24.246 | 10.151 | 9.025 | 17.606 | 9.025 | 9.025 | 10.764 | 20.998 | 10.764 | 10.764 | 11.563 | 22.556 | 11.563 | 11.563 |
| 671 | 4.16 | 7.906 | 16.025 | 5.500 | 5.194 | 10.529 | 5.194 | 5.194 | 6.846 | 13.878 | 6.846 | 6.846 | 7.165 | 14.523 | 7.165 | 7.165 |
| 675 | 4.16 | 7.162 | 13.784 | 5.031 | 4.832 | 9.300 | 4.832 | 4.832 | 6.202 | 11.937 | 6.202 | 6.202 | 6.560 | 12.624 | 6.560 | 6.560 |

TABLE 5.16: IEC SIMULATED RESULTS FOR SCENARIO 4 - PV

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 12.480 | 24.299 | 10.127 | 9.041 | 17.604 | 9.041 | 9.041 | 10.808 | 21.044 | 10.808 | 10.808 | 11.579 | 22.545 | 11.579 | 11.579 |
| 671 | 4.16 | 7.848 | 16.006 | 5.400 | 5.177 | 10.558 | 5.177 | 5.177 | 6.797 | 13.862 | 6.797 | 6.797 | 7.074 | 14.427 | 7.074 | 7.074 |
| 675 | 4.16 | 6.981 | 13.572 | 4.847 | 4.775 | 9.282 | 4.775 | 4.775 | 6.046 | 11.753 | 6.046 | 6.046 | 6.344 | 12.333 | 6.344 | 6.344 |

TABLE 5.17: IEC SIMULATED RESULTS FOR SCENARIO 2 - HYBRID

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}{ }^{\prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 14.118 | 28.395 | 9.987 | 9.586 | 19.280 | 9.586 | 9.586 | 12.221 | 24.578 | 12.221 | 12.221 | 13.091 | 26.329 | 13.091 | 13.091 |
| 671 | 4.16 | 8.167 | 16.987 | 5.274 | 5.268 | 10.958 | 5.268 | 5.268 | 7.071 | 14.708 | 7.071 | 7.071 | 7.410 | 15.412 | 7.410 | 7.410 |
| 675 | 4.16 | 7.253 | 14.273 | 4.759 | 4.857 | 9.558 | 4.857 | 4.857 | 6.280 | 12.358 | 6.280 | 6.280 | 6.570 | 12.929 | 6.570 | 6.570 |

TABLE 5.18: IEC SIMULATED RESULTS FOR SCENARIO 3 - HYBRID

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 13.322 | 26.248 | 9.995 | 9.333 | 18.388 | 9.333 | 9.333 | 11.535 | 22.725 | 11.535 | 11.535 | 12.395 | 24.420 | 12.395 | 12.395 |
| 671 | 4.16 | 9.413 | 19.583 | 5.358 | 5.585 | 11.618 | 5.585 | 5.585 | 8.147 | 16.948 | 8.147 | 8.147 | 8.438 | 17.555 | 8.438 | 8.438 |
| 675 | 4.16 | 8.733 | 17.801 | 4.872 | 5.254 | 10.709 | 5.254 | 5.254 | 7.557 | 15.403 | 7.557 | 7.557 | 7.833 | 15.966 | 7.833 | 7.833 |

TABLE 5.19: IEC SIMULATED RESULTS FOR SCENARIO 4 - HYBRID

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 14.078 | 28.357 | 9.995 | 9.576 | 19.288 | 9.576 | 9.576 | 12.185 | 24.545 | 12.185 | 12.185 | 13.077 | 26.341 | 13.077 | 13.077 |
| 671 | 4.16 | 8.240 | 17.026 | 5.358 | 5.287 | 10.925 | 5.287 | 5.287 | 7.135 | 14.742 | 7.135 | 7.135 | 7.423 | 15.338 | 7.423 | 7.423 |
| 675 | 4.16 | 7.291 | 14.264 | 4.816 | 4.868 | 9.525 | 4.868 | 4.868 | 6.313 | 12.351 | 6.313 | 6.313 | 6.582 | 12.878 | 6.582 | 6.582 |

TABLE 5.20: IEC SIMULATED RESULTS FOR SCENARIO 2 - DIESEL HYBRID

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}{ }^{\text {a }}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 14.424 | 29.365 | 10.237 | 11.578 | 23.569 | 11.578 | 11.578 | 12.512 | 25.472 | 12.512 | 12.512 | 13.553 | 27.591 | 13.553 | 13.553 |
| 671 | 4.16 | 8.236 | 17.207 | 5.501 | 5.584 | 11.667 | 5.584 | 5.584 | 7.137 | 14.911 | 7.137 | 7.137 | 7.484 | 15.636 | 7.484 | 7.484 |
| 675 | 4.16 | 7.309 | 14.425 | 4.948 | 5.121 | 10.105 | 5.121 | 5.121 | 6.333 | 12.498 | 6.333 | 6.333 | 6.648 | 13.12 | 6.648 | 6.648 |

TABLE 5.21: IEC SIMULATED RESULTS FOR SCENARIO 3 - DIESEL HYBRID

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 13.478 | 26.655 | 10.751 | 10.108 | 19.99 | 10.108 | 10.108 | 11.681 | 23.101 | 11.681 | 11.681 | 12.692 | 25.1 | 12.692 | 12.692 |
| 671 | 4.16 | 9.709 | 20.412 | 6.201 | 7.639 | 16.06 | 7.628 | 7.639 | 8.424 | 17.711 | 8.424 | 8.424 | 9.108 | 19.149 | 9.108 | 9.108 |
| 675 | 4.16 | 9.038 | 18.773 | 5.111 | 7.414 | 15.399 | 7.385 | 7.414 | 7.848 | 16.301 | 7.848 | 7.848 | 8.558 | 17.777 | 8.558 | 8.558 |

TABLE 5.22: IEC SIMULATED RESULTS FOR SCENARIO 4 - DIESEL HYBRID

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 14.039 | 28.225 | 10.825 | 10.947 | 22.009 | 10.947 | 10.947 | 12.107 | 24.34 | 12.107 | 12.107 | 13.137 | 26.41 | 13.137 | 13.137 |
| 671 | 4.16 | 9.06 | 19.136 | 5.863 | 6.766 | 14.289 | 6.766 | 6.766 | 7.806 | 16.487 | 7.806 | 7.806 | 8.294 | 17.517 | 8.294 | 8.294 |
| 675 | 4.16 | 7.926 | 15.656 | 5.239 | 6.052 | 11.953 | 6.052 | 6.052 | 6.834 | 13.498 | 6.834 | 6.834 | 7.297 | 14.413 | 7.297 | 7.297 |

TABLE 5.23: IEC SIMULATED RESULTS FOR SCENARIO 3 AT 10\% PENETRATION LEVEL - DIESEL HYBRID

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}{ }^{\prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 12.444 | 24.476 | 9.970 | 9.152 | 18.001 | 9.152 | 9.152 | 10.772 | 21.187 | 10.772 | 10.772 | 11.680 | 22.974 | 11.680 | 11.680 |
| 671 | 4.16 | 7.941 | 16.409 | 5.345 | 5.444 | 11.249 | 5.444 | 5.444 | 6.870 | 14.195 | 6.870 | 6.870 | 7.244 | 14.970 | 7.244 | 7.244 |
| 675 | 4.16 | 7.142 | 14.098 | 4.774 | 5.058 | 9.986 | 5.058 | 5.058 | 6.177 | 12.194 | 6.177 | 6.177 | 6.494 | 12.821 | 6.494 | 6.494 |

TABLE 5.24: IEC SIMULATED RESULTS FOR SCENARIO 3 AT 30\% PENETRATION LEVEL - DIESEL HYBRID

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 12.756 | 25.142 | 10.194 | 9.467 | 18.660 | 9.467 | 9.467 | 11.033 | 21.747 | 11.033 | 11.033 | 11.979 | 23.611 | 11.979 | 11.979 |
| 671 | 4.16 | 8.430 | 17.522 | 5.578 | 6.075 | 12.627 | 6.075 | 6.075 | 7.279 | 15.129 | 7.279 | 7.279 | 7.731 | 16.069 | 7.731 | 7.731 |
| 675 | 4.16 | 7.653 | 15.336 | 4.864 | 5.709 | 11.439 | 5.709 | 5.709 | 6.605 | 13.236 | 6.605 | 6.605 | 7.025 | 14.077 | 7.025 | 7.025 |

TABLE 5.25: IEC SIMULATED RESULTS FOR SCENARIO 3 AT 50\% PENETRATION LEVEL - DIESEL HYBRID

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 12.937 | 25.529 | 10.327 | 9.636 | 19.015 | 9.636 | 9.636 | 11.185 | 22.073 | 11.185 | 11.185 | 12.153 | 23.982 | 12.153 | 12.153 |
| 671 | 4.16 | 8.730 | 18.209 | 5.722 | 6.449 | 13.450 | 6.449 | 6.449 | 7.530 | 15.705 | 7.530 | 7.530 | 8.038 | 16.765 | 8.038 | 8.038 |
| 675 | 4.16 | 7.972 | 16.122 | 4.918 | 6.102 | 12.342 | 6.102 | 6.102 | 6.871 | 13.897 | 6.871 | 6.871 | 7.367 | 14.900 | 7.367 | 7.367 |

TABLE 5.26: IEC SIMULATED RESULTS FOR SCENARIO 3 AT 85\% PENETRATION LEVEL - DIESEL HYBRID

| Bus |  | 3-Ph |  |  | LG |  |  |  | LL |  |  |  | LLG |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{I}_{\mathrm{k}}$ | $\mathrm{i}_{\mathrm{p}}$ | $\mathrm{I}_{\mathrm{b}}$ | $\mathrm{I}_{\mathrm{k}}$ |
| 632 | 4.16 | 13.478 | 26.655 | 10.751 | 10.108 | 19.99 | 10.108 | 10.108 | 11.681 | 23.101 | 11.681 | 11.681 | 12.692 | 25.1 | 12.692 | 12.692 |
| 671 | 4.16 | 9.709 | 20.412 | 6.201 | 7.639 | 16.06 | 7.628 | 7.639 | 8.424 | 17.711 | 8.424 | 8.424 | 9.108 | 19.149 | 9.108 | 9.108 |
| 675 | 4.16 | 9.038 | 18.773 | 5.111 | 7.414 | 15.399 | 7.385 | 7.414 | 7.848 | 16.301 | 7.848 | 7.848 | 8.558 | 17.777 | 8.558 | 8.558 |

### 5.5.1 Analysis of simulated results for IEC calculations

Referring to Tables 5.10-5.22, it is possible to notice the following:

For unbalanced faults (LG, LL, and LL-G):

- The symmetrical short circuit breaking current ( $\mathrm{I}_{\mathrm{b}}$ ) is equal to the initial symmetrical current $\left(I_{k}^{\prime \prime}\right)$. This is according to the IEC assumption considered for the $I_{b}$ calculation. In which $I_{b}$ is assumed to be equal to $I_{k}^{\prime \prime}$ for the all types of unbalaced faults. However, this assumption should be only applied if the generator is far away from the fault
- The steady-state short circuit current ( $\mathrm{I}_{\mathrm{k}}$ ) is equal to the initial symmetrical current $\left(I_{k}^{\prime \prime}\right)$. This is according on the IEC rule for the clculation of $I_{k}$, which is based on the assumption that the flux decay in the generator is neglected.

For 3-ph, LL, and LL-G faults, the highest initial symmetrical current ( $\mathrm{I}_{\mathrm{k}}$ ) occurred in the case of wind at S 2 at faulted bus 632. As the peak short circuit current ( $\mathrm{i}_{\mathrm{p}}$ ) depends on the $I_{k}^{\prime \prime}$, the highest $i_{p}$ is for case of wind at S 2 at faulted bus 632 .

For LG fault, the case of diesel hybrid at S2 is found to be the highest values for $\mathrm{I}_{\mathrm{k}}$. Simultaneously, the maximum $i_{p}$ is found to be for the same case study.

Consequently, as the steady state short circuit currents are equal to the initial symmetrical currents $I_{k}^{\prime \prime}$ for unbalanced faults, therefore, the highest $I_{k}$ is found to be in case of wind at S 2 at faulted bus 632. Hence, for the 3-ph fault, the highest $\mathrm{I}_{\mathrm{k}}$ is observed to occur at case of diesel hybrid at S4 at faulted bus 632.

The main short circuit contributors to this system, especially on the same buses where the DG will be connected to in further studies in this thesis are presented in Table 5-27. This table 5-27 provides the 3-ph initial symmetrical short circuit currents when a fault occurs at 632,675 , and 671 respectively

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TABLE 5.27: THREE-PHASE INITIAL SYMMETRICAL SHORT CIRCUIT CURRENT MAGNITUDES (KA) AND PERCENTAGE OF THE TOTAL SHORT CIRCUIT CURRENT

| Faulted Bus | 632 |  | 675 |  | 671 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Total SCC (kA) | 12.291 |  | 6.906 |  | 7.714 |  |
|  | SCC (kA) | $\%$ | SCC (kA) | $\%$ | SCC (kA) | $\%$ |
| Utility Grid U1 | 9.864 | 80.3 | 4.505 | 65.2 | 5.116 | 66.3 |
| Line 5 | 1.954 | 15.9 | 4.732 | 68.5 | 5.374 | 69.7 |
| Lump 1 | 3.416 | 27.8 | 1.560 | 22.6 | 1.772 | 23.0 |
| Lump 6 | 1.091 | 8.9 | 1.162 | 16.8 | 1.320 | 17.1 |
| Lump 3 | 0.775 | 6.3 | 0.954 | 13.8 | 0.938 | 12.2 |
| Cable 606_500 | 0.775 | 6.3 | 5.971 | 86.5 | 0.938 | 12.2 |
| switch | 0.775 | 6.3 | 5.971 | 86.5 | 0.938 | 12.2 |
| Line 2 | 0.394 | 3.2 | 0.180 | 2.6 | 0.204 | 2.6 |
| Transformer |  |  |  |  |  |  |
| T1 | 0.394 | 3.2 | 0.180 | 2.6 | 0.204 | 2.6 |
| Lump 10 | 0.106 | 0.9 | 0.048 | 0.7 | 0.055 | 0.7 |
| Lump 11 | 0.088 | 0.7 | 0.093 | 1.3 | 0.106 | 1.4 |

According to the IEC standard, non-rotating loads are disregarded for the short circuit current calculations. Therefore, it could be observed that the contribution of other non-rotating loads in the system is not included in the results in Table 5.27.

From Table 5.27, during a 3 -ph fault at bus 632, the total initial symmetrical short circuit current ( $\mathbf{I}_{\mathbf{k}}^{\prime \prime}$ ) is found to be 12.291 kA , of which the utility grid (U1) contributed 9.864 kA . Thus, is approximately $80 \%$ of the total $3-\mathrm{ph}$ initial symmetrical current at bus 632 .

The five motors ( Lump 1, Lump 3, Lump 6, Lump 10, and lump 11) connected to the system have contributed to total short circuit currents at the faulted buses 632,675 , and 671 respectively. The location of motors in regards to the fault location has varied the SCC results relatively. From Table 5.27, it could be said that due to the series impedances of the transmission lines, cables, and transformers in between the fault and the motors, this could still have limited influence on the short circuit current.

### 5.5.1.1 Impact of DG type on short circuit current

Similarly to the ANSI analysis in 5.4.1, the contribution of each DG type distinctly is considered of the total SCC at each faulted bus for the IEC method. Simulated results from the short circuit study were taken and the percentage of each type of DG
used of the total SCC at its allocated bus has been calculated, and presented in Tables 5.28 and 5.29.

TABLE 5.28: COMPARISON OF DG UNITS CONTRIBUTION ON THE SHORT CIRCUIT CURRENT LEVEL AT S2

| Faulted Bus | \%U1 | \%WTG | \%PV | \%Diesel Generator |
| :---: | :---: | :---: | :---: | :---: |
| 632 | 68.4 | 8.1 | 1.6 | 6.5 |
| 671 | 56.5 | 6.7 | 1.3 | 5.4 |
| 675 | 55.6 | 6.6 | 1.3 | 5.3 |

TABLE 5.29: COMPARISON BETWEEN DG UNITS CONTRIBUTION ON THE SHORT CIRCUIT CURRENT AT S3

| Faulted Bus | \%U1 | \%WTG | \%PV | \%Diesel Generator |
| :---: | :---: | :---: | :---: | :---: |
| 632 | 73.2 | 5.9 | 1.2 | 4.8 |
| 671 | 52.7 | 11.4 | 2.2 | 9.2 |
| 675 | 49.8 | 12.9 | 2.5 | 10.4 |

From Tables 5.28 and 5.29, it is found that:

- U1 contributes approximately about $50 \%$ and more of the total SCC at faulted bus for S2 and S3
- WTG percentage of the total SCC at different faulted bus for S2 and S3 is more than the diesel generator and PV percentages.
- Comparing the DG contribution between S2 and S3

Fault at bus 632: contribution of DG on SCC is lower at S3 than S2

Fault at bus 671: contribution of DG on SCC is higher at S3 than S2
Fault at bus 675: contribution of DG on SCC is higher at S2 than S3

### 5.5.1.2 Impact of DG location on short circuit current

From Table 5.11 - 5.22 , it can be noticed that for the four types of fault examined, the highest SCCs usually occurred at scenario S2 (in which the DG is located at bus 362) and the faulted bus 632 for the four case studies examined. The minimum SCC usually occurred at scenario 3 (in which the DG is located at bus 675), while scenario S4 is in the intermediate between S2 and S3.

### 5.5.1.3 Worst case scenarios for IEC calculations

From Tables $5.10-5.22$, the overall worst 10 cases occurred at the system under study have been selected for 3-ph and LL-G faults, and presented in Figures 5.7 and 5.8 for the IEC simulated results. The LL-G fault currents are the highest of the faulted line currents examined. Hence, the LL-G fault current has been presented to represent the worst case scenario of the faulted line currents. It is noticed that all of the worst case scenarios have occurred at bus 632 for the two types of fault respectively.


Figure 5.6 The worst cases during 3-ph fault for IEC calculations


Figure 5.7 The worst cases during LL-G fault for IEC calculations

From figures 5.7 and 5.8, it is observed that the worst case for both fault types is at the case of wind at scenario two (S2). The least DG impact is the PV at scenario two (S2). In comparing the scenarios that reflect the impact of DG location on the system short circuit level, it is noticed that scenario 2 represented the worst location a DG could be located for all types of DG used and DG mix applied in this study. In case of wind only, it is found that this is the worst DG type regardless of the three scenarios S2, S3, S4 that have been tested respectively. Similarly, the DG mix is among the critical cases for the three scenarios.

### 5.5.1.4 Lowest case scenarios for IEC calculations

The results for the lowest short circuit currents during the 3-ph and LL-G faults are represented in Figures 5.9 and 5.10.


Figure 5.8 The minimum short circuit currents during 3-ph fault for IEC calculations

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Figure 5.9 The minimum short circuit currents during LL-G fault for IEC calculations
From Figures 5.9 and 5.10, it could be noticed that the least SCC achieved when a fault occurred at buses 675 and 671 respectively. Both figures have the least SCC in case of no DG at scenario S1 when a fault occurred at bus 675. The PV for scenarios S2, S3, and S4 at faulted bus 675 is the most DG type maintained lowest.

### 5.5.1.5 Impact of DG penetration level

Figure 5.11 presents the impact of different penetration levels of diesel hybrid DG during the occurrence of 3 -ph faults at buses 632, 675, and 671 respectively.


Figure 5.10 Penetration level vs 3-ph short circuit currents for diesel hybrid mix located at bus 675 for IEC calculation

From Figure 5.11, it could be noticed that as the penetration level increases the SCC increases. The maximum increase calculated between the $85 \%$ penetration level and the no DG level is found to be approximately 9.7 \% higher at faulted bus 632. The difference between SCC during a fault at bus 632 and faulted bus 675 is noticed to be around the double. The short circuit currents are the highest at faulted bus 632, followed by 671, and least at faulted bus 675 .

### 5.6 Comparison between ANSI and IEC simulated results

- It is noticed that the initial symmetrical IEC currents are found to be higher than the symmetrical ANSI currents. This behaviour can be attributed to the following factors considered by the IEC for the initial symmetrical currents calculation:
- Higher voltage factor $c$ adopted in the equivalent voltage source
- Subtransient impedances considered for all rotating loads in the system.
- Use of impedance correction factors
- Referring to Tables 5.8 and 5.28, the following comments are:
- Contribution of U1 of the total SCC at faulted buses 632,675, and 671 is higher in ANSI more than IEC
- Contribution of diesel generator of the total SCC at faulted buses 632,675, and 671 is higher in ANSI more than IEC
- Contribution of WTG of the total SCC at faulted buses 632,675, and 671 is higher in IEC more than ANSI
- Contribution of PV WTG of the total SCC at faulted buses 632,675, and 671 is higher in IEC more than ANSI
- From ANSI results, the diesel generator contribution is higher than the WTG. Though, in IEC it less than the WTG contribution
- In comparing between the IEC Figures 5.7-5.10 and ANSI Figures 5.2-5.5
- For 3-ph and LL-G short circuit currents 10 worst cases

In IEC, the order for the 10 worst cases is found not to be the same order as in ANSI

- For 3-ph and LL-G short circuit currents 10 least cases

In IEC, the order for the 10 minimum cases is found not to be the same sequence as in ANSI

- Comparing between Figure 5.6 and 5.11

The simulated results at faulted bus 671 are found to be higher in IEC more than in ANSI, which led to alter the impact of DG on faulted buses. The results at faulted bus 671 are higher than the results at faulted bus 675 for IEC

### 5.7 Summary

In this chapter the modified IEEE 13 bus test distribution system has been modelled in ETAP 12 to examine the impact of different types of DG (wind, PV, hybrid, and diesel hybrid) on the short circuit level. In addition to the impact of DG location and various penetration levels for diesel hybrid integration into the system studied. The short circuit analysis performed using the ANSI and IEC methods for the calculation of SCC at selected bus at occurrence of 3-ph, L-G, LL, LL-G faults.

The simulated results showed that the SCC for 3-ph fault is the highest in comparison to all types of fault tested for both calculation methods. This is due to the positive sequence impedances that are involved in the 3 -ph fault calculation are higher than the negative and zero sequences. For the unbalanced faults, LL-G is found to be the highest for IEC and ANSI standards.

The DFIG WTG is found to have a significant impact on the calculated short circuit currents when connected as the only DG source or when integrated with different types of DG. Conversely, it could be said that the PV have a limited impact on the short circuit currents neither connected as only source nor with other types of DG.

In the system under study, the relation between the DG location and SCC is relatively crucial, especially when the DG is connected near the utility grid, where the maximum values of SCCs were obtained. Scenario S4 confirmed this remark that is found, in which the SCCs are independent from the DG type or capacity once it is connected adjacent to the utility grid. Thus is a result of the high contribution of the utility grid on the SCC at the bus where it is connected. Furthermore, the SCCs for S3 where lower than S2 and S3 results, as the DG is connected to the furthest bus from the utility grid.

The examination of the different penetration level ( $10 \%, 30 \%, 42 \%$, and $85 \%$ ) of the utility rating showed that there is a direct relation between the penetration level of

DG and the SCCs. With the incremental increase of DG capacity connected to the system under study, there was an incremental increase in the SCCs. However, this increase could be considered as a limited, since the maximum difference between the SCC at no DG connected and with $85 \%$ penetration of DG is found to be about $9 \%$ depending on method of short circuit current calculation.

In the comparison between ANSI and IEC simulated results for the same system and scenarios applied, it was found that the IEC method yielded to higher values to the SCCs more than the ANSI method. Thus as a result to the impedance correction factors and voltage factor c taken into account by the IEC method. Therefore, the analysis outcome for the system was not similar for the two methods. IEC results led to different critique than that reached from ANSI results.

## Chapter Six

## 6 IEEE 30 Bus Distribution Test System

### 6.1 Introduction

In this chapter, the main objective is to analyse the simulated results for ANSI and IEC calculations for the IEEE 30 bus, in order to evaluate the impact of DG type, location and penetration level on the short circuit current. The short circuit currents magnitudes of the system under study with no DG connected are considered as reference in order to be able to assess the impact of DG integration. Moreover, a comparison between the IEC simulated results and ANSI simulated results will be presented in order to ensure valid and reliable results.

This chapter is divided into seven main sections. First, section 6.1 is an introduction and outline to the chapter. Section 6.2 will provide the main characteristics for the system under study. Section 6.3 will illustrate the case studies examined. Section 6.4 will present the ANSI simulated results and comprehensive analyses to the results. Similarly, section 6.5 will present and provide detailed analysis to the IEC simulated results. Section 6.6 will compare between IEC and ANSI simulated results. Last, section 6.7 will provide a conclusion and recommendations.

### 6.2 System under study

The distribution test system used in this study is the IEEE 30-bus, shown in Figure 6.1. The system elements full data are provided in Appendix B.


Figure 6.1 The IEEE30 bus system [12]

The model is implemented and modified in ETAP 14 software, where the short circuit analysis is performed for different six scenarios presented in section 6.3.

Initially, it was essential to ensure that the system is stable. Therefore, load flow analysis has been performed to obtain the magnitude and phase angle of voltage at each bus, and the real and reactive power flowing in each transmission line. Furthermore, in this system, the criteria to select the buses for DG installation is found to be different from the IEEE 13-bus distribution test system. For latter system, the distance from the main grid was considered as the reference on which the DG will be located. Whereas, the IEEE 30 bus system, there is no main grid to be
taken as a reference. Therefore, the buses where the DG will be connected were selected based on their voltage profile at the base case (no DG installed) based on the Newton-Raphson (NR) load flow analysis. Results for load flow analysis are presented in Appendix C. It was found that the buses with lower voltage profile were: 7, 26, 29, and 30. Similar results were found in [117] after performing Newton-Raphson load flow analysis on the same system under study using MATLAB 7.0. Detailed load flow analysis is out of the scope of this research, however, it was crucial to be performed and considered to be aware with the system performance for coherent evaluation and assessment.

### 6.3 IEEE-30 bus distribution test system case studies

There are four cases of different DG units connected to the system under study as follows:

Case 1: Wind

Case 2: PV
Case 3: Hybrid system (Wind and PV)
Case 4: Diesel Hybrid system (Diesel generator Wind, and PV)

For each case study, there are six different scenarios selected to study the impact of DG location and capacity on the short circuit level of the distribution system presented in Table 6.1. The six scenarios for each case were repeated at different penetration levels: $10 \% ; 30 \%, 42 \%$; and $85 \%$ respectively.

TABLE 6.1: DIFFERENT SCENARIOS EXAMINED

| Scenario |  |
| :---: | :--- |
| Scenario 1 (S1) | DG placed at Bus 7 |
| Scenario 2 (S2) | DG placed at Bus 26 |
| Scenario 3 (S3) | DG placed at Bus 29 |
| Scenario 4 (S4) | DG placed at Bus 30 |
| Scenario 5 (S5) | DG placed at Bus 7 and Bus 29 |
| Scenario 6 (S6) | DG placed at Bus 26 and Bus 30 |

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In cases 3 and 4 (where there are different types of DG units connected), the DG units ratings were equal. Similarly, DG capacities for S5 and S6 were divided equally.

### 6.3.1 Preliminary analysis for load flow studies

Load flow analysis has been performed after modifying the system model by including the DG at different scenarios with various penetration levels. Table 6.2 present a summary of load flow results obtained.

TABLE 6.2: SUMMARY OF LOAD FLOW ANALYSIS FOR MODIFIED IEEE 30 BUS TEST SYSTEM

| Case ID | Load Flow Analysis <br> (System Status) |
| :--- | :--- |
| No DG | Converged |
| 10\% Penetration Level |  |
| Case 1: Wind | Converged at all scenarios <br> Converged at all scenarios <br> Converged at all scenarios <br> Case 3: Wind and PV <br> Case 4: Wind, PV, and Diesel |
| 30\% Penetration Level |  |
| Case 1: Wind | Converged at all scenarios <br> Case 2: PV <br> Cane 3: Wind and PV <br> Case 4: Wind, PV, and Diesel |
| 42\% Penetration Level | Converged at all scenarios scenarios |
| Case 1: Wind | Diverged at S2, S3, and S4 <br> Case 2: PV |
| Case 3: Wind and PV | Diverged at S2, S3, and S4 |
| Caserged at S2, S3, and S4 |  |
| Converged at all scenarios |  |

In the $42 \%$ penetration level of wind, the load flow failed to converge for S2, S3, and S4 respectively. However, the load flow converged for S1, S5, and S6 respectively. In comparing between S1, S2, S3, and S4 parameters, it could be found that these scenarios could be considered identical in terms of DG capacity, though different in terms of DG location. For S5 and S6, these scenarios are different from S1, S2, S3, and S4 in terms of DG capacity. In investigating the reason for system divergence in given scenarios, it has been observed that the bus voltages at buses 26,29 , and 30 for

S2, S3, and S4 respectively are the same and equal to 33 kV . However, the bus voltage at bus 7 for S 1 is 132 kV . This raised the question, is there a direct relation between the bus voltage and the DG capacity. An initial justification has been considered that the bus with a lower voltage in the system under study is unable to accommodate DG with high penetration level of $42 \%$. Whereas, the distribution network still could withstand the same DG capacity if it is distributed between the buses with same voltage 33 kV as in the S 5 and S 6 , or if the DG located at a higher bus voltage 132 kV as in S1. Though, a further scenario has been created to verify this preliminary assumption. The same DG capacity has been relocated to bus 28 (the selection criteria based on the same zone of diverged buses, but with higher bus voltage 132 kV ). After performing load flow analysis, the system converged for the same DG capacity.

More load flow studies were simulated and yet failed to converge, despite the fact of taking into consideration different parameters such as: (Refer to EATP help load flow):

- Increasing number of iterations for Newton Raphson load flow analysis including 5, 50, and 99 iterations respectively. Though, five iterations are the maximum number of iterations recommended for NR by ETAP.
- Performing different load flow solution methods such as Adaptive NewtonRaphson, Fast-decoupled, and Accelerated Gauss-Seidel (GS).

The load flow solution methods are Newton-Raphson, Adaptive Newton-Raphson, Fast-decoupled, and Accelerated Gauss-Seidel. NR and GS are the most common used methods for load flow analysis. These methods tend to converge in the load flow studies for transmission systems more than distribution networks systems. This is due to the fact that distribution networks systems are considered to be "illconditioned power networks". The following characteristics of distribution networks made these methods not suitable to be applied [118], [119]:

- Radial structure or weakly-meshed topologies
- High resistance to reactance (R/X)

In distribution networks $\mathrm{R} / \mathrm{X}$ for transmission lines and cables are in range 0.5 to 7 , more than in transmission networks, usually less than 0.5

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- Type of Load

Load flow methods assume static load flow, where it is not the case for distribution networks; non-linear load models (such as rectifiers)

- Unbalanced distributed loads.
- Distributed generation

These characteristics, along with the large number of nodes and branches of distribution networks make the load flow solution methods inappropriate and not reliable for load flow studies of unbalanced distribution systems. Therefore unbalanced load flow studies and some distribution systems components shall be accurately modelled according to three phase basis. Moreover, there are a number of modified load flow solutions methods and algorithms especially designed for distribution networks presented in the literature [117].

### 6.3.2 Short circuit analysis

The short circuit analysis is run twice to include the two calculation methods: ANSI and IEC. The IEEE 30-bus system original model is modified through connecting DG with various capacities, penetration levels and at various locations. The DG units used are; Type 3 (DFIG) wind turbine generators (WTG), photovoltaics (PV), and diesel generators. The short circuit study included the four types of fault: 3-ph; LG; LL; and LLG at all the system buses respectively.

### 6.4 Simulated results for ANSI calculations

The study selected for the short circuit calculation is $1.5-4$ cycles. This study performs 3-phase, line-to-ground, line-to-line, and line-to-line-to-ground fault studies per ANSI Standards. The study calculates short circuit currents in their rms values between 1.5 to 4 cycles at faulted buses. In this study, generators are represented by their positive, negative, and zero sequence subtransient reactance, and motors are modelled by their positive, negative, and zero sequence transient reactance [115] .

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The simulated results are presented in Appendix D. The results are presented in this arrangement order to compare between the DG types, in regards their impact on the short circuit current, along with the influence of different DG location.

### 6.5 Analysis of simulated results for ANSI calculations

Table 6.3 presents the simulated results for the short circuit current magnitudes of the system under study at no DG connected.

TABLE 6.3: ANSI SIMULATED RESULTS AT NO DG INSTALLED (KA)

| Bus |  | Type of Faults |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | 3 -Ph | LG | LL | LLG |
| 1 | 132 | 9.698 | 11.89 | 8.551 | 11.241 |
| 2 | 132 | 8.526 | 9.442 | 7.46 | 9.129 |
| 3 | 132 | 5.254 | 5.285 | 4.569 | 5.323 |
| 4 | 132 | 6.698 | 6.585 | 5.83 | 6.75 |
| 5 | 132 | 5.666 | 5.56 | 4.934 | 5.671 |
| 6 | 132 | 7.537 | 7.353 | 6.565 | 7.573 |
| 7 | 132 | 4.947 | 4.752 | 4.296 | 4.912 |
| 8 | 132 | 5.686 | 5.745 | 4.953 | 5.766 |
| 9 | 33 | 12.945 | 13.195 | 11.252 | 13.257 |
| 10 | 33 | 14.592 | 14.122 | 12.668 | 14.608 |
| 11 | 11 | 19.151 | 22.956 | 16.689 | 21.863 |
| 12 | 33 | 12.56 | 12.087 | 10.91 | 12.527 |
| 13 | 11 | 21.077 | 25.741 | 18.329 | 24.903 |
| 14 | 33 | 6.796 | 6.497 | 5.89 | 6.693 |
| 15 | 33 | 10.355 | 9.767 | 8.98 | 10.16 |
| 16 | 33 | 8.416 | 8.154 | 7.297 | 8.372 |
| 17 | 33 | 10.627 | 10.206 | 9.217 | 10.535 |
| 18 | 33 | 7.085 | 6.702 | 6.139 | 6.928 |
| 19 | 33 | 7.377 | 6.92 | 6.393 | 7.174 |
| 20 | 33 | 7.711 | 7.311 | 6.683 | 7.553 |
| 21 | 33 | 11.907 | 11.292 | 10.327 | 11.712 |
| 22 | 33 | 11.665 | 11.119 | 10.117 | 11.514 |
| 23 | 33 | 7.012 | 6.715 | 6.076 | 6.901 |
| 24 | 33 | 8.754 | 8.331 | 7.586 | 8.577 |
| 25 | 33 | 5.669 | 5.573 | 4.912 | 5.653 |
| 26 | 33 | 2.551 | 2.446 | 2.209 | 2.526 |
| 27 | 33 | 6.217 | 6.217 | 5.388 | 6.309 |
| 28 | 132 | 4.446 | 4.314 | 3.863 | 4.428 |
| 29 | 33 | 3.289 | 3.137 | 2.849 | 3.232 |
| 30 | 33 | 3.315 | 3.035 | 2.871 | 3.241 |
|  |  |  |  |  |  |

From Table 6.3, it is observed that for all types of fault examined, the highest SCCs occurred at buses 10,11 , and 13 . These buses are the outcome of substations $132 / 33$ kV . The decrease in voltage caused the SCC to increase. Also, the substation impedance contributes to the $\mathrm{R} / \mathrm{X}$ ratio. There is no general pattern to types of fault as in the 13-bus distribution test system. Every bus has responded differently to the types of fault applied. This could be summarised as follows:

For buses 1, 2, 3, 11, and 13: the LG fault results were higher than LLG and 3-ph results. For buses 4, 5, 6, 10, and 12: the LLG fault results were higher than 3-ph and LG results. Whereas for Buses 8 and 9, the LLG fault results greater than LG and 3ph faults values. However, for the rest of the buses starting from bus 14 to bus 30, the SCCs for the 3-ph fault were the highest; more than LLG and LG. it could be summarised as follows:

At Buses 1, 2, 3, 11, and 13 LG > LLG > 3-ph
At Buses 4, 5, 6, 10, and 12 LLG > 3-ph> LG
At Buses 8 and 9
LLG > LG > 3-ph
At Buses 14-30 3-ph $>$ LLG $>$ LG
6.5.1 Impact of DG penetration level on short circuit current

For every scenario, comparison between the four penetration levels ( $10 \%, 30 \%$, $42 \%$, and $85 \%$ ) and the scenario of no DG is performed and presented in Figures 6.2-6.5. The comparison is performed on the buses that adopted the DG in each scenario, in order to examine the impact of DG penetration level on the short circuit current of the allocated buses.

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### 6.5.1.1 Scenario One

A 3 -ph fault at bus 7 is examined; the simulated results at bus 7 for different penetration levels and DG types are presented in Figure 6.2


Figure 6.2 Short Circuit current versus different DG penetration level for Three-phase fault at bus 7
From Figure 6.2, it could be noticed that there is an increase in the SCCs with the increase of penetration level. The case of diesel hybrid system is noticed to be the highest case for the $10 \%$ penetration, with an increase of 0.326 kA (around 6\%) from case of no DG. It could be observed that the case of wind is the highest type of DG in comparison to the other types and DG mix used for penetration levels $30 \%, 42 \%$, and $85 \%$ respectively.

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A LG fault at bus 7 is examined; the simulated results at bus 7 for different penetration levels and DG types are presented in Figure 6.3.


Figure 6.3 Short Circuit current versus different DG penetration level for LG fault at bus 7
From Figure 6.3, it could be observed that in case of wind for the $42 \%$ and $85 \%$ of penetration, the SCCs are higher in comparison to the other penetration levels and other DG types. The difference in case of no DG connected and $85 \%$ of wind is around $90 \%$ increase.

A LL fault at bus 7 is examined; the simulated results at bus 7 for different penetration levels and DG types are presented in Figure 6.4.


Figure 6.4 Short Circuit current versus different DG penetration level for LL fault at bus 7

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A LLG fault at bus 7 is examined; the simulated results at bus 7 for different penetration levels and DG types are presented in Figure 6.5.


Figure 6.5 Short Circuit current versus different DG penetration level for LLG fault at bus 7
It could be concluded that for scenario one (S1), in instance of faults occurring at bus 7, the short circuit currents for every type of fault showed different outcomes. The LG fault yielded to a significant increase in case of wind at $42 \%$ and $85 \%$ of penetration, in comparison to the other types of DG used and penetrations $10 \%$ and $30 \%$. For all types of fault, at $85 \%$ and $42 \%$ penetration, wind is the highest, followed by diesel hybrid, hybrid system, and PV is the lowest case. However, at $30 \%$ of DG penetration, hybrid system is higher than diesel hybrid system.

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### 6.5.1.2 Scenario Two

A 3-ph fault at bus 26 is examined; the simulated results at bus 26 for different penetration levels and DG types are presented in Figure 6.6


Figure 6.6 Short Circuit current versus different DG penetration level for Three-phase fault at bus 26 From Figure 6.6, it could be noticed that the increase in SCCs with the increase in penetration level started to double at $42 \%$ penetration level in particular in case of wind and diesel hybrid.

A LG fault at bus 26 is examined; the simulated results at bus 26 for different penetration levels and DG types are presented in Figure 6.7.


Figure 6.7 Short Circuit current versus different DG penetration level for LG fault at bus 26

From Figure 6.7, it could be observed that the SCCs incremented rapidly at $30 \%$ penetration level in case of wind where it exceeded the double in comparison to $10 \%$ penetration. Also, wind is much higher than other types of DG for $30 \%$, $42 \%$ and $85 \%$ of penetration.

A LL fault at bus 26 is examined; the simulated results at bus 26 for different penetration levels and DG types are presented in Figure 6.8.


Figure 6.8 Short Circuit current versus different DG penetration level for LL fault at bus 26

A LLG fault at bus 26 is examined; the simulated results at bus 26 for different penetration levels and DG types are presented in Figure 6.9.

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Figure 6.9 Short Circuit current versus different DG penetration level for LLG fault at bus 26
From Figures 6.6-6.9, for the four types of fault, it could be observed the following:

- $42 \%$ and $85 \%$ penetration levels: Wind impact on the SCCs is the highest, followed by diesel hybrid and hybrid, while the PV is the lowest impact.
- $30 \%$ penetration level: hybrid impact is higher than the diesel hybrid, though the wind and PV impacts are still similar to the $42 \%$ and $85 \%$ penetration levels.
- $10 \%$ penetration level: diesel hybrid influence on the SCCs is greater than wind, during the occurrence of 3 -ph and LL faults.

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### 6.5.1.3 Scenario Three

A 3-ph fault at bus 29 is examined; the simulated results at bus 29 for different penetration levels and DG types are presented in Figure 6.10


Figure 6.10 Short Circuit current versus different DG penetration level for Three-phase fault at bus 29 A LG fault at bus 29 is examined; the simulated results at bus 29 for different penetration levels and DG types are presented in Figure 6.11.


Figure 6.11 Short Circuit current versus different DG penetration level for LG fault at bus 29

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A LL fault at bus 29 is examined; the simulated results at bus 29 for different penetration levels and DG types are presented in Figure 6.12.


Figure 6.12 Short Circuit current versus different DG penetration level for LL fault at bus 29
A LLG fault at bus 29 is examined; the simulated results at bus 29 for different penetration levels and DG types are presented in Figure 6.13.


Figure 6.13 Short Circuit current versus different DG penetration level for LLG fault at bus 29 It is noticed that Scenario 3 is similar to scenario 2 in terms of consequence of different penetration levels and impact of DG types on the short circuit current.

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### 6.5.1.4 Scenario Four

A 3-ph fault at bus 30 is examined; the simulated results at bus 30 for different penetration levels and DG types are presented in Figure 6.14.


Figure 6.14 Short Circuit current versus different DG penetration level for Three-phase fault at bus 30
A LG fault at bus 30, the simulated results at bus 30 for different penetration levels and DG types are presented in Figure 6.15.


Figure 6.15 Short Circuit current versus different DG penetration level for LG fault at bus 30

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A LL fault at bus 30 is examined; the simulated results at bus 30 for different penetration levels and DG types are presented in Figure 6.16.


Figure 6.16 Short Circuit current versus different DG penetration level for LL fault at bus 30
A LLG fault at bus 30 is examined; the simulated results at bus 30 for different penetration levels and DG types are presented in Figure 6.17.


Figure 6.17 Short Circuit current versus different DG penetration level for LLG fault at bus 30
From Figures 6.14-6.17, it could be noticed that for $85 \%$ penetration level, the hybrid system exceeded the diesel hybrid values. This did not occur for other scenarios.

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### 6.5.1.5 Scenario Five

In this scenario, the DG capacity is divided over two buses. This is to examine the impact of DG capacity on the short circuit currents, and to identify the influence of dividing the capacity along the network. The results of the four types of fault simulated on bus 7 and 29 respectively are presented in Figures 6.18-6.21.


Figure 6.18 Short Circuit current versus different DG penetration level for Three-phase fault at buses 7 and 29


Figure 6.19 Short Circuit current versus different DG penetration level for LG fault at buses 7 and 29

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Figure 6.20 Short Circuit current versus different DG penetration level for LL fault at buses 7 and 29


Figure 6.21 Short Circuit current versus different DG penetration level for LLG fault at buses 7 and 29

When comparing Figures 6.18-6.21 with Scenario 1 and scenario 3, it is observed that for bus 7 and 29, there was no change in the DG type performance. The sequence of DG types at each penetration level for the four types of fault applied is similar. Whereas, the impact of DG on SCC at bus 7 is very near to the results in S1. This is due to the existence of bus 7 in the transmission side of the network. However, for bus 29 the results indicated that with reducing the DG capacity, the SCCs are reduced.

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### 6.5.1.6 Scenario Six

The aim of this scenario is similar to scenario 5 , where the main objective is to examine the impact of DG capacity on the short circuit currents, and to identify the influence of dividing the capacity along the network. In this scenario the examined buses are 26 and 30. S5 and S6 are similar in capacities and different in location. The various scenarios would provide varied and reliable results.

The results of the four types of fault simulated on bus 26 and 30 respectively are presented in Figures 6.22- 6.25.


Figure 6.22 Short Circuit current versus different DG penetration level for Three-phase fault at buses 26 and 30


Figure 6.23 Short Circuit current versus different DG penetration level for LG fault at buses 26 and 30

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Figure 6.24 Short Circuit current versus different DG penetration level for LL fault at buses 26 and 30


Figure 6.25 Short Circuit current versus different DG penetration level for LLG fault at buses 26 and 30

In comparing figures $6.22-6.25$ with S2 and S4 figures, it is found that for penetration levels $10 \%, 30 \%$, and $42 \%$; the profile of DG types on the buses 26 and 30 is similar when these buses are accommodating the same DG type at increased capacity. Whereas for bus 30 at $85 \%$ penetration level, the diesel hybrid system increased the SCCs to exceed the hybrid system impact on SCCs, while in S4, the hybrid system was the dominant. Though, the short circuit currents for these buses in reduced, as a result of reducing the DG capacity.

### 6.5.2 Worst case scenarios

The worst 10 case scenarios are extracted and presented in Figure 6.26. It is found that the most severe scenarios that led to higher short circuit currents happened at $85 \%$ penetration level of wind.


Figure 6.26 The worst cases for ANSI calculations
From Figure 6.26, it is noticed that S4 and S3 representing buses 30 and 29 respectively, are the most common buses affected when DG is installed during the occurrence of all types of fault. Furthermore, wind at bus 26 (S2) contributed effectively to the short circuit current on this bus for LG and LLG faults.

### 6.6 Analysis of simulated results for IEC calculations

As previously figured out in chapter five that the simulated results for IEC standard are different than the ANSI standard results due to the different types of prospective short circuit current determined (initial symmetrical current ( $\mathrm{I}_{\mathrm{k}}^{\prime \prime}$ ); peak short circuit current ( $\mathrm{i}_{\mathrm{p}}$ ); symmetrical short-circuit breaking current $\left(\mathrm{I}_{\mathrm{b}}\right)$; and steady-state short circuit current ( $\mathrm{I}_{\mathrm{k}}$ ).

Similarly to IEEE 13 bus distribution test system simulation, the computation is set to calculate the maximum short circuit currents which determine the capacity or rating of electrical equipment.

The LG, LL, LLG, and 3-Phase Faults (IEC 60909) study is selected in ETAP 14 for the short circuit calculation. This study performs line-to-ground, line-to-line, line-to-
line-to-ground, and three-phase fault studies per IEC 60909 Standard. The study calculates initial symmetrical rms, peak and symmetrical breaking rms, and steadystate rms short-circuit currents at faulted buses. Detailed analyses have been provided in chapter five that differentiated between the different types of IEC simulated short circuit currents. In this chapter, the analyses are focused on the initial symmetrical current as it is found that the initial symmetrical current $\left(I_{\mathrm{k}}\right.$ ) $)$ is the most SCC equivalent to ANSI symmetrical current, in order to be able to compare results. ETAP 14 models the generators by their positive, negative, and zero sequence reactance, while motors are modelled by their locked-rotor impedance [115]. The voltage factor $c$ value varies depending on the system rated voltage. For the system under study, the $c$ factor is selected to be 1.10 according to IEC-909606. The simulated results for the short circuit study are presented in Appendix D.

### 6.6.1 Worst case scenarios

From simulated results, it is found that the most severe scenarios that led to higher short circuit currents happened at $85 \%$ penetration level of wind. The worst 10 case scenarios are extracted and presented in Figure 6.27.


Figure 6.27 The worst cases for IEC calculations
From Figure 6.27, it is observed that scenario four (S4) in case of wind at bus 30 is the worst case scenario occurred in this study.

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### 6.7 Differences between ANSI and IEC results

In this section the differences between ANSI and IEC results are calculated and presented in percentage in Tables 6.4-6.9.

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TABLE 6.4: COMPARISON BETWEEN ANSI RESULTS AND IEC RESULTS FOR SCENARIO 1

| 3-ph Fault | Wind |  |  | Diesel Hybrid System |  |  | Hybrid System |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% |
| 0\% | 4.947 | 6.134 | 24.0 | 4.947 | 6.134 | 24.0 | 4.947 | 6.134 | 24.0 | 4.947 | 6.134 | 24.0 |
| 10\% | 5.101 | 6.325 | 24.0 | 5.273 | 6.546 | 24.1 | 5.156 | 6.427 | 24.7 | 5.022 | 6.215 | 23.8 |
| 30\% | 5.671 | 7.103 | 25.3 | 5.273 | 6.546 | 24.1 | 5.555 | 6.984 | 25.7 | 5.022 | 6.215 | 23.8 |
| 42\% | 6.809 | 9.041 | 32.8 | 6.417 | 7.999 | 24.7 | 5.85 | 7.416 | 26.8 | 5.277 | 6.487 | 22.9 |
| 85\% | 7.906 | 10.332 | 30.7 | 7.296 | 9.021 | 23.6 | 6.575 | 8.384 | 27.5 | 5.844 | 7.089 | 21.3 |


| LG Fault | Wind |  |  | Diesel Hybrid System |  |  |  | Hybrid System |  |  | PV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 4.752 | 5.667 | 19.3 | 4.752 | 5.667 | 19.3 | 4.752 | 5.667 | 19.3 | 4.752 | 5.667 |  |
| $10 \%$ | 5.267 | 6.331 | 20.2 | 4.959 | 5.897 | 18.9 | 4.892 | 5.83 | 19.2 | 4.798 | 5.712 |  |
| $30 \%$ | 5.684 | 6.827 | 20.1 | 4.959 | 5.897 | 18.9 | 5.144 | 6.123 | 19.0 | 4.798 | 5.712 |  |
| $42 \%$ | 8.113 | 10.093 | 24.4 | 5.612 | 6.625 | 18.1 | 5.327 | 6.338 | 19.0 | 4.956 | 5.869 |  |
| $85 \%$ | 9.067 | 11.123 | 22.7 | 6.025 | 7.069 | 17.3 | 5.718 | 6.783 | 18.6 | 5.296 | 6.205 |  |


| LL Fault | Wind |  |  | Diesel Hybrid System |  |  | Hybrid System |  |  | PV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 4.296 | 5.322 | 23.9 | 4.296 | 5.322 | 23.9 | 4.296 | 5.322 | 23.9 | 4.296 | 5.322 |
| $10 \%$ | 4.438 | 5.489 | 23.7 | 4.595 | 5.683 | 23.7 | 4.497 | 5.577 | 24.0 | 4.362 | 5.393 |
| $30 \%$ | 4.97 | 6.161 | 24.0 | 4.595 | 5.683 | 23.7 | 4.879 | 6.058 | 24.2 | 4.362 | 5.393 |
| $42 \%$ | 6.157 | 7.837 | 27.3 | 5.649 | 6.958 | 23.2 | 5.17 | 6.432 | 24.4 | 4.585 | 5.631 |
| $85 \%$ | 7.147 | 8.955 | 25.3 | 6.415 | 7.853 | 22.4 | 5.842 | 7.27 | 24.4 | 5.078 | 6.154 |
|  | 21.2 |  |  |  |  |  |  |  |  |  |  |


| LLG Fault | Wind |  |  | Diesel Hybrid System |  |  |  | Hybrid System |  |  | PV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 4.912 | 5.995 | 22.0 | 4.912 | 5.995 | 22.0 | 4.912 | 5.995 | 22.0 | 4.912 | 5.995 |  |
| $10 \%$ | 5.217 | 6.372 | 22.1 | 5.203 | 6.351 | 22.1 | 5.094 | 6.235 | 22.4 | 4.926 | 6.009 |  |
| $30 \%$ | 5.704 | 6.991 | 22.6 | 5.203 | 6.351 | 22.1 | 5.437 | 6.688 | 23.0 | 4.926 | 6.009 |  |
| $42 \%$ | 7.633 | 9.863 | 29.2 | 6.222 | 7.602 | 22.2 | 5.702 | 7.044 | 23.5 | 5.287 | 6.386 |  |
| $85 \%$ | 8.572 | 10.916 | 27.3 | 6.987 | 8.494 | 21.6 | 6.346 | 7.86 | 23.9 | 5.929 | 7.073 |  |

TAble 6.5: COMPARISON BETWEEN ANSI RESULTS AND IEC RESULTS FOR SCENARIO 2

| 3-ph Fault | Wind |  |  | Diesel Hybrid System |  |  |  | Hybrid System |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | ANSI | IEC | $\%$ | ANSI | IEC | $\%$ | ANSI | IEC | $\%$ | ANSI | IEC | \% |  |
| $0 \%$ | 2.551 | 3.06 | 20.0 | 2.551 | 3.06 | 20.0 | 2.551 | 3.06 | 20.0 | 2.551 | 3.06 | 20.0 |  |
| $10 \%$ | 3.174 | 3.841 | 21.0 | 3.803 | 4.632 | 21.8 | 3.391 | 4.232 | 24.8 | 3.052 | 3.596 | 17.8 |  |
| $30 \%$ | 4.542 | 10.488 | 130.9 | 3.803 | 4.632 | 21.8 | 5.008 | 6.464 | 29.1 | 3.052 | 3.596 | 17.8 |  |
| $42 \%$ | 9.952 | 14.193 | 42.6 | 8.267 | 10.257 | 24.1 | 6.196 | 8.192 | 32.2 | 5.099 | 5.8 | 13.7 |  |
| $85 \%$ | 17.355 | 25.137 | 44.8 | 13.979 | 17.425 | 24.7 | 9.843 | 13.304 | 35.2 | 8.264 | 9.253 | 12.0 |  |


| LG Fault | Wind |  |  | Diesel Hybrid System |  |  | Hybrid System |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 2.446 | 2.87 | 17.3 | 2.446 | 2.87 | 17.3 | 2.446 | 2.87 | 17.3 | 2.446 | 2.87 | 17.3 |
| $10 \%$ | 3.942 | 4.69 | 19.0 | 3.136 | 3.659 | 16.7 | 2.95 | 3.472 | 17.7 | 2.743 | 3.172 | 15.6 |
| $30 \%$ | 10.148 | 12.73 | 25.4 | 3.136 | 3.659 | 16.7 | 3.645 | 4.281 | 17.4 | 2.743 | 3.172 | 15.6 |
| $42 \%$ | 13.985 | 17.74 | 26.9 | 4.47 | 5.158 | 15.4 | 4.024 | 4.722 | 17.3 | 3.731 | 4.208 | 12.8 |
| $85 \%$ | 24.727 | 31.544 | 27.6 | 5.211 | 5.97 | 14.6 | 4.759 | 5.54 | 16.4 | 4.647 | 5.211 | 12.1 |


| LL Fault | Wind |  |  | Diesel Hybrid System |  |  | Hybrid System |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0\% | 2.209 | 2.65 | 20.0 | 2.209 | 2.65 | 20.0 | 2.209 | 2.65 | 20.0 | 2.209 | 2.65 | 20.0 |
| 10\% | 2.783 | 3.326 | 19.5 | 3.354 | 4.03 | 20.2 | 3.012 | 3.664 | 21.6 | 2.644 | 3.114 | 17.8 |
| 30\% | 7.136 | 9.077 | 27.2 | 3.354 | 4.03 | 20.2 | 4.544 | 5.596 | 23.2 | 2.644 | 3.114 | 17.8 |
| 42\% | 9.555 | 12.282 | 28.5 | 7.446 | 8.967 | 20.4 | 5.701 | 7.091 | 24.4 | 4.416 | 5.023 | 13.7 |
| 85\% | 16.187 | 21.751 | 34.4 | 12.66 | 15.253 | 20.5 | 9.178 | 11.515 | 25.5 | 7.158 | 8.014 | 12.0 |


| LLG Fault | Wind |  |  | Diesel Hybrid System |  |  |  | Hybrid System |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 2.526 | 3.017 | 19.4 | 2.526 | 3.017 | 19.4 | 2.526 | 3.017 | 19.4 | 2.526 | 3.017 | 19.4 |  |
| $10 \%$ | 3.959 | 4.753 | 20.1 | 3.705 | 4.449 | 20.1 | 3.311 | 4.035 | 21.9 | 3.062 | 3.56 | 16.3 |  |
| $30 \%$ | 9.221 | 12.429 | 34.8 | 3.705 | 4.449 | 20.1 | 4.811 | 5.955 | 23.8 | 3.062 | 3.56 | 16.3 |  |
| $42 \%$ | 12.572 | 17.374 | 38.2 | 7.835 | 9.452 | 20.6 | 5.956 | 7.451 | 25.1 | 5.19 | 5.863 | 13.0 |  |
| $85 \%$ | 21.976 | 30.793 | 40.1 | 13.071 | 15.769 | 20.6 | 9.412 | 11.867 | 26.1 | 8.153 | 9.111 | 11.8 |  |

Table 6.6: COMPARISON BETWEEN ANSI RESULTS AND IEC RESULTS FOR SCENARIO 3

| 3-ph Fault | Wind |  |  | Diesel Hybrid System |  |  | Hybrid System |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% |
| 0\% | 3.289 | 4.08 | 24.0 | 3.289 | 4.08 | 24.0 | 3.289 | 4.08 | 24.0 | 3.289 | 4.08 | 24.0 |
| 10\% | 3.912 | 4.857 | 24.2 | 4.564 | 5.678 | 24.4 | 4.131 | 5.258 | 27.3 | 3.705 | 4.524 | 22.1 |
| 30\% | 8.342 | 11.57 | 38.7 | 4.564 | 5.678 | 24.4 | 5.745 | 7.493 | 30.4 | 3.705 | 4.524 | 22.1 |
| 42\% | 10.757 | 15.278 | 42.0 | 9.048 | 11.324 | 25.2 | 6.934 | 9.224 | 33.0 | 5.523 | 6.457 | 16.9 |
| 85\% | 18.166 | 26.227 | 44.4 | 14.768 | 18.5 | 25.3 | 10.581 | 14.34 | 35.5 | 8.55 | 9.727 | 13.8 |


| LG Fault | Wind |  |  | Diesel Hybrid System |  |  |  | Hybrid System |  |  | PV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 3.137 | 3.799 | 21.1 | 3.137 | 3.799 | 21.1 | 3.137 | 3.799 | 21.1 | 3.137 | 3.799 |  |
| $10 \%$ | 4.729 | 5.762 | 21.8 | 3.848 | 4.614 | 19.9 | 3.649 | 4.412 | 20.9 | 3.39 | 4.056 |  |
| $30 \%$ | 11.025 | 13.881 | 25.9 | 3.848 | 4.614 | 19.9 | 4.396 | 5.295 | 20.5 | 3.39 | 4.056 |  |
| $42 \%$ | 14.903 | 18.937 | 27.1 | 5.349 | 6.329 | 18.3 | 4.828 | 5.808 | 20.3 | 4.39 | 5.092 |  |
| $85 \%$ | 25.661 | 32.757 | 27.7 | 6.283 | 7.391 | 17.6 | 5.717 | 6.832 | 19.5 | 5.531 | 6.341 |  |


| LL Fault | Wind |  |  | Diesel Hybrid System |  |  |  | Hybrid System |  |  | PV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 2.849 | 3.534 | 24.0 | 2.849 | 3.534 | 24.0 | 2.849 | 3.534 | 24.0 | 2.849 | 3.534 |  |
| $10 \%$ | 3.423 | 4.207 | 22.9 | 4.015 | 4.935 | 22.9 | 3.656 | 4.553 | 24.5 | 3.21 | 3.919 |  |
| $30 \%$ | 7.836 | 10.014 | 27.8 | 4.015 | 4.935 | 22.9 | 5.188 | 6.487 | 25.0 | 3.21 | 3.919 |  |
| $42 \%$ | 10.261 | 13.222 | 28.9 | 8.124 | 9.891 | 21.8 | 6.349 | 7.986 | 25.8 | 4.784 | 5.593 |  |
| $85 \%$ | 17.529 | 22.696 | 29.5 | 13.345 | 16.182 | 21.3 | 9.828 | 12.413 | 26.3 | 7.406 | 8.425 |  |


| LLG Fault | Wind |  |  |  | Diesel Hybrid System |  |  |  | Hybrid System |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 3.232 | 3.976 | 23.0 | 3.232 | 3.976 | 23.0 | 3.232 | 3.976 | 23.0 | 3.232 | 3.976 |
| $10 \%$ | 4.688 | 5.756 | 22.8 | 4.386 | 5.38 | 22.7 | 3.985 | 4.961 | 24.5 | 3.737 | 4.505 |
| $30 \%$ | 10.047 | 13.513 | 34.5 | 4.386 | 5.38 | 22.7 | 5.436 | 6.828 | 25.6 | 3.737 | 4.505 |
| $42 \%$ | 13.429 | 18.485 | 37.6 | 8.456 | 10.317 | 22.0 | 6.558 | 8.296 | 26.5 | 5.757 | 6.672 |
| $85 \%$ | 22.848 | 31.918 | 39.7 | 13.662 | 16.599 | 21.5 | 9.967 | 12.656 | 27.0 | 8.706 | 9.886 |

TABLE 6.7: COMPARISON BETWEEN ANSI RESULTS AND IEC RESULTS FOR SCENARIO 4

| 3-ph Fault | Wind |  |  | Diesel Hybrid System |  |  | Hybrid System |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | ANSI | IEC | $\%$ | ANSI | IEC | $\%$ | ANSI | IEC | \% | ANSI | IEC | \% |
| $0 \%$ | 3.315 | 4.282 | 29.2 | 3.315 | 4.282 | 29.2 | 3.315 | 4.282 | 29.2 | 3.315 | 4.282 | 29.2 |
| $10 \%$ | 3.937 | 5.056 | 28.4 | 4.593 | 5.885 | 28.1 | 4.155 | 5.459 | 31.4 | 3.716 | 4.697 | 26.4 |
| $30 \%$ | 8.381 | 11.793 | 40.7 | 4.593 | 5.885 | 28.1 | 5.768 | 7.692 | 33.4 | 3.716 | 4.697 | 26.4 |
| $42 \%$ | 10.797 | 15.504 | 43.6 | 9.081 | 11.539 | 27.1 | 6.957 | 9.424 | 35.5 | 5.503 | 6.55 | 19.0 |
| $85 \%$ | 18.209 | 26.456 | 45.3 | 10.603 | 18.718 | 76.5 | 14.802 | 14.54 | -1.8 | 8.514 | 9.765 | 14.7 |


| LG Fault | Wind |  |  | Diesel Hybrid System |  |  |  | Hybrid System |  |  | PV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 3.035 | 3.751 | 23.6 | 3.035 | 3.751 | 23.6 | 3.035 | 3.751 | 23.6 | 3.035 | 3.751 | 23.6 |
| $10 \%$ | 4.714 | 5.891 | 25.0 | 3.688 | 4.471 | 21.2 | 3.504 | 4.29 | 22.4 | 3.255 | 3.957 | 21.6 |
| $30 \%$ | 11.033 | 14.051 | 27.4 | 3.688 | 4.471 | 21.2 | 4.179 | 5.058 | 21.0 | 3.255 | 3.957 | 21.6 |
| $42 \%$ | 14.924 | 19.135 | 28.2 | 5.028 | 5.953 | 18.4 | 4.564 | 5.501 | 20.5 | 4.148 | 4.826 | 16.3 |
| $85 \%$ | 25.687 | 32.965 | 28.3 | 5.344 | 6.849 | 28.2 | 5.838 | 6.373 | 9.2 | 5.162 | 5.901 | 14.3 |


| LL Fault | Wind |  |  | Diesel Hybrid System |  |  |  | Hybrid System |  |  | PV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 2.871 | 3.708 | 29.2 | 2.871 | 3.708 | 29.2 | 2.871 | 3.708 | 29.2 | 2.871 | 3.708 | 29.2 |
| $10 \%$ | 3.444 | 4.378 | 27.1 | 4.04 | 5.115 | 26.6 | 3.678 | 4.727 | 28.5 | 3.219 | 4.068 | 26.4 |
| $30 \%$ | 7.87 | 10.208 | 29.7 | 4.04 | 5.115 | 26.6 | 5.209 | 6.66 | 27.9 | 3.219 | 4.068 | 26.4 |
| $42 \%$ | 10.296 | 13.417 | 30.3 | 8.152 | 10.076 | 23.6 | 6.37 | 8.159 | 28.1 | 4.767 | 5.674 | 19.0 |
| $85 \%$ | 17.567 | 22.894 | 30.3 | 9.849 | 16.37 | 66.2 | 13.375 | 12.586 | -5.9 | 7.375 | 8.458 | 14.7 |


| LLG Fault | Wind |  |  |  | Diesel Hybrid System |  |  |  | Hybrid System |  |  | PV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \%$ | 3.241 | 4.147 | 28.0 | 3.241 | 4.147 | 28.0 | 3.241 | 4.147 | 28.0 | 3.241 | 4.147 | 28.0 |  |
| $10 \%$ | 4.657 | 4.378 | -6.0 | 4.399 | 5.553 | 26.2 | 3.997 | 5.131 | 28.4 | 3.658 | 4.522 | 23.6 |  |
| $30 \%$ | 10.043 | 13.648 | 35.9 | 4.399 | 5.553 | 26.2 | 5.452 | 7.001 | 28.4 | 3.658 | 4.522 | 23.6 |  |
| $42 \%$ | 13.435 | 18.637 | 38.7 | 8.477 | 10.495 | 23.8 | 6.578 | 8.473 | 28.8 | 5.626 | 6.591 | 17.2 |  |
| $85 \%$ | 22.859 | 32.078 | 40.3 | 9.995 | 16.78 | 67.9 | 13.686 | 12.838 | -6.2 | 8.536 | 9.733 | 14.0 |  |

TABLE 6.8: COMPARISON BETWEEN ANSI RESULTS AND IEC RESULTS FOR SCENARIO 5

| 3-ph Fault | Bus | Wind |  |  | Diesel Hybrid |  |  | Hybrid |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | No | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% |
| $0 \%$ | 7 | 4.947 | 6.134 | 24.0 | 4.947 | 6.134 | 24.0 | 4.947 | 6.134 | 24.0 | 4.947 | 6.134 | 24.0 |
|  | 29 | 3.289 | 4.08 | 24.0 | 3.289 | 4.08 | 24.0 | 3.289 | 4.08 | 24.0 | 3.289 | 4.08 | 24.0 |
| $10 \%$ | 7 | 5.076 | 6.295 | 24.0 | 5.139 | 6.373 | 24.0 | 5.058 | 6.288 | 24.3 | 4.982 | 6.171 | 23.9 |
|  | 29 | 3.743 | 4.661 | 24.5 | 4.001 | 4.986 | 24.6 | 3.711 | 4.671 | 25.9 | 3.467 | 4.272 | 23.2 |
| $30 \%$ | 7 | 5.609 | 7.099 | 26.6 | 5.139 | 6.373 | 24.0 | 5.264 | 6.57 | 24.8 | 4.982 | 6.171 | 23.9 |
|  | 29 | 5.802 | 7.81 | 34.6 | 4.001 | 4.986 | 24.6 | 4.08 | 5.074 | 24.4 | 3.467 | 4.272 | 23.2 |
| $42 \%$ | 7 | 5.914 | 7.677 | 29.8 | 5.715 | 7.096 | 24.2 | 5.423 | 6.799 | 25.4 | 5.114 | 6.308 | 23.3 |
|  | 29 | 7.003 | 9.657 | 37.9 | 6.17 | 7.702 | 24.8 | 5.116 | 6.661 | 30.2 | 4.242 | 5.092 | 20.0 |
| $8 \%$ | 7 | 6.875 | 8.997 | 30.9 | 6.448 | 8.003 | 24.1 | 5.905 | 7.471 | 26.5 | 5.316 | 6.518 | 22.6 |
|  | 29 | 10.835 | 15.38 | 41.9 | 9.109 | 11.39 | 25.1 | 7.008 | 9.316 | 32.9 | 5.563 | 6.498 | 16.8 |


| LG Fault | Bus | Wind |  |  | Diesel Hybrid |  |  | Hybrid |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | No | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% |
| 0\% | 7 | 4.752 | 5.667 | 19.3 | 4.752 | 5.667 | 19.3 | 4.752 | 5.667 | 19.3 | 4.752 | 5.667 | 19.3 |
|  | 29 | 3.137 | 3.799 | 21.1 | 3.137 | 3.799 | 21.1 | 3.137 | 3.799 | 21.1 | 3.137 | 3.799 | 21.1 |
| 10\% | 7 | 5.249 | 6.311 | 20.2 | 4.876 | 5.802 | 19.0 | 4.828 | 5.753 | 19.2 | 4.773 | 5.687 | 19.1 |
|  | 29 | 4.246 | 5.172 | 21.8 | 3.563 | 4.288 | 20.3 | 3.406 | 4.122 | 21.0 | 3.245 | 3.91 | 20.5 |
| 30\% | 7 | 5.939 | 7.184 | 21.0 | 4.876 | 5.802 | 19.0 | 4.961 | 5.907 | 19.1 | 4.773 | 5.687 | 19.1 |
|  | 29 | 7.248 | 9.04 | 24.7 | 3.563 | 4.288 | 20.3 | 3.596 | 4.324 | 20.2 | 3.245 | 3.91 | 20.5 |
| 42\% | 7 | 6.564 | 8.075 | 23.0 | 5.224 | 6.187 | 18.4 | 5.065 | 6.028 | 19.0 | 4.854 | 5.765 | 18.8 |
|  | 29 | 9.257 | 11.65 | 25.8 | 4.522 | 5.385 | 19.1 | 4.141 | 5 | 20.7 | 3.713 | 4.385 | 18.1 |
| 85\% | 7 | 8.173 | 10.06 | 23.0 | 5.624 | 6.627 | 17.8 | 5.356 | 6.365 | 18.8 | 4.98 | 5.886 | 18.2 |
|  | 29 | 14.992 | 19.04 | 27.0 | 5.362 | 6.343 | 18.3 | 4.85 | 8.533 | 75.9 | 4.408 | 5.111 | 15.9 |

Chapter Six: IEEE 30 Bus Distribution Test System

| LL Fault | Bus | Wind |  |  | Diesel Hybrid |  |  | Hybrid |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | No | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% |
| 0\% | 7 | 4.296 | 5.322 | 23.9 | 4.296 | 5.322 | 23.9 | 4.296 | 5.322 | 23.9 | 4.296 | 5.322 | 23.9 |
|  | 29 | 2.849 | 3.534 | 24.0 | 2.849 | 3.534 | 24.0 | 2.849 | 3.534 | 24.0 | 2.849 | 3.534 | 24.0 |
| 10\% | 7 | 4.416 | 5.462 | 23.7 | 4.473 | 5.532 | 23.7 | 4.404 | 5.456 | 23.9 | 4.327 | 5.355 | 23.8 |
|  | 29 | 3.272 | 4.037 | 23.4 | 3.508 | 4.328 | 23.4 | 3.254 | 4.045 | 24.3 | 3.003 | 3.7 | 23.2 |
| 30\% | 7 | 4.952 | 6.157 | 24.3 | 4.473 | 5.532 | 23.7 | 4.599 | 5.7 | 23.9 | 4.327 | 5.355 | 23.8 |
|  | 29 | 5.337 | 6.761 | 26.7 | 3.508 | 4.328 | 23.4 | 3.565 | 4.395 | 23.3 | 3.003 | 3.7 | 23.2 |
| 42\% | 7 | 5.261 | 6.657 | 26.5 | 5.003 | 6.166 | 23.2 | 4.756 | 5.898 | 24.0 | 4.442 | 5.475 | 23.3 |
|  | 29 | 6.548 | 8.359 | 27.7 | 5.839 | 6.713 | 15.0 | 4.607 | 5.767 | 25.2 | 3.675 | 4.411 | 20.0 |
| 85\% | 7 | 6.216 | 7.798 | 25.5 | 5.67 | 6.962 | 22.8 | 5.219 | 6.48 | 24.2 | 4.619 | 5.658 | 22.5 |
|  | 29 | 10.333 | 13.31 | 28.8 | 8.177 | 9.95 | 21.7 | 6.416 | 8.065 | 25.7 | 4.819 | 5.629 | 16.8 |


| LLG Fault | Bus | Wind |  |  | Diesel Hybrid |  |  | Hybrid |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | No | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% |
| 0\% | 7 | 4.912 | 5.995 | 22.0 | 4.912 | 5.995 | 22.0 | 4.912 | 5.995 | 22.0 | 4.912 | 5.995 | 22.0 |
|  | 29 | 3.232 | 3.976 | 23.0 | 3.232 | 3.976 | 23.0 | 3.232 | 3.976 | 23.0 | 3.232 | 3.976 | 23.0 |
| 10\% | 7 | 5.194 | 6.345 | 22.2 | 5.082 | 6.199 | 22.0 | 5.007 | 6.119 | 22.2 | 4.914 | 5.997 | 22.0 |
|  | 29 | 4.197 | 5.163 | 23.0 | 3.879 | 4.769 | 22.9 | 3.602 | 4.463 | 23.9 | 3.451 | 4.199 | 21.7 |
| 30\% | 7 | 5.795 | 7.189 | 24.1 | 5.082 | 6.199 | 22.0 | 5.184 | 6.35 | 22.5 | 4.914 | 5.997 | 22.0 |
|  | 29 | 6.747 | 8.836 | 31.0 | 3.879 | 4.769 | 22.9 | 3.91 | 4.792 | 22.6 | 3.451 | 4.199 | 21.7 |
| 42\% | 7 | 6.312 | 8.001 | 26.8 | 5.593 | 6.821 | 22.0 | 5.325 | 6.537 | 22.8 | 5.054 | 6.131 | 21.3 |
|  | 29 | 8.492 | 11.37 | 33.9 | 5.839 | 7.146 | 22.4 | 4.879 | 6.13 | 25.6 | 4.382 | 5.193 | 18.5 |
| 85\% | 7 | 7.696 | 9.82 | 27.6 | 6.24 | 7.601 | 21.8 | 5.747 | 7.089 | 23.4 | 5.329 | 6.421 | 20.5 |
|  | 29 | 13.509 | 18.59 | 37.6 | 8.509 | 10.38 | 21.9 | 6.626 | 8.377 | 26.4 | 5.797 | 6.713 | 15.8 |

TABLE 6.9: COMPARISON BETWEEN ANSI RESULTS AND IEC RESULTS FOR SCENARIO 6

| 3-ph Fault | Bus | Wind |  |  |  | Diesel Hybrid |  |  | Hybrid |  |  | PV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | No | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% |
| $0 \%$ | 26 | 2.551 | 3.06 | 20.0 | 2.551 | 3.06 | 20.0 | 2.551 | 3.06 | 20.0 | 2.551 | 3.06 | 20.0 |
|  | 30 | 3.315 | 4.282 | 29.2 | 3.315 | 4.282 | 29.2 | 3.315 | 4.282 | 29.2 | 3.315 | 4.282 | 29.2 |
| $10 \%$ | 26 | 3.017 | 3.653 | 21.1 | 3.274 | 3.969 | 21.2 | 2.988 | 3.662 | 22.6 | 2.773 | 3.297 | 18.9 |
|  | 30 | 3.798 | 4.888 | 28.7 | 4.074 | 5.233 | 28.4 | 3.762 | 4.898 | 30.2 | 3.49 | 4.46 | 27.8 |
| $30 \%$ | 26 | 5.072 | 6.785 | 33.8 | 4.541 | 3.969 | -12.6 | 3.817 | 4.793 | 25.6 | 2.773 | 3.297 | 18.9 |
|  | 30 | 5.937 | 8.12 | 36.8 | 5.375 | 5.233 | -2.6 | 4.606 | 6.05 | 31.4 | 3.49 | 4.46 | 27.8 |
| $42 \%$ | 26 | 6.274 | 8.634 | 37.6 | 5.457 | 6.69 | 22.6 | 4.424 | 5.67 | 28.2 | 3.719 | 4.292 | 15.4 |
|  | 30 | 7.154 | 9.982 | 39.5 | 6.303 | 8.004 | 27.0 | 5.22 | 6.937 | 32.9 | 4.302 | 5.278 | 22.7 |
| $85 \%$ | 26 | 10.102 | 14.35 | 42.1 | 8.401 | 10.38 | 23.6 | 6.336 | 8.336 | 31.6 | 5.222 | 5.899 | 13.0 |
|  | 30 | 11.002 | 15.717 | 42.9 | 9.267 | 11.717 | 26.4 | 7.144 | 9.62 | 34.7 | 5.671 | 6.694 | 18.0 |


| LG Fault | Bus | Wind |  |  |  | Diesel Hybrid |  |  | Hybrid |  |  | PV |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | No | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% |
| $0 \%$ | 26 | 2.446 | 2.87 | 17.3 | 2.446 | 2.87 | 17.3 | 2.446 | 2.87 | 17.3 | 2.446 | 2.87 | 17.3 |
|  | 30 | 3.035 | 3.751 | 23.6 | 3.035 | 3.751 | 23.6 | 3.035 | 3.751 | 23.6 | 3.035 | 3.751 | 23.6 |
| $10 \%$ | 26 | 3.523 | 4.18 | 18.6 | 2.876 | 3.359 | 16.8 | 2.723 | 3.198 | 17.4 | 2.581 | 3.005 | 16.4 |
|  | 30 | 4.257 | 5.298 | 24.5 | 3.449 | 4.202 | 21.8 | 3.296 | 4.047 | 22.8 | 3.131 | 3.838 | 22.6 |
| $30 \%$ | 26 | 6.486 | 7.993 | 23.2 | 3.448 | 3.359 | -2.6 | 3.159 | 3.709 | 17.4 | 2.581 | 3.005 | 16.4 |
|  | 30 | 7.355 | 9.277 | 26.1 | 4.004 | 4.202 | 4.9 | 3.714 | 4.52 | 21.7 | 3.131 | 3.838 | 22.6 |
| $42 \%$ | 26 | 8.459 | 10.558 | 24.8 | 3.773 | 4.374 | 15.9 | 3.43 | 4.031 | 17.5 | 3.113 | 3.544 | 13.8 |
|  | 30 | 9.396 | 11.934 | 27.0 | 4.326 | 5.167 | 19.4 | 3.98 | 4.827 | 21.3 | 3.576 | 4.25 | 18.8 |
| $8 \%$ | 26 | 14.162 | 17.91 | 26.5 | 4.492 | 5.176 | 15.2 | 4.06 | 4.753 | 17.1 | 3.78 | 4.248 | 12.4 |
|  | 30 | 15.159 | 19.363 | 27.7 | 5.062 | 5.982 | 18.2 | 4.613 | 5.544 | 20.2 | 4.217 | 4.885 | 15.8 |

Chapter Six: IEEE 30 Bus Distribution Test System

| LL Fault | Bus | Wind |  |  |  | Diesel Hybrid |  |  | Hybrid |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | No | ANSI | IEC | $\%$ | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% |  |
| $0 \%$ | 26 | 2.209 | 2.65 | 20.0 | 2.209 | 2.65 | 20.0 | 2.209 | 2.65 | 20.0 | 2.209 | 2.65 | 20.0 |  |
|  | 30 | 2.871 | 3.708 | 29.2 | 2.871 | 3.708 | 29.2 | 2.871 | 3.708 | 29.2 | 2.871 | 3.708 | 29.2 |  |
| $10 \%$ | 26 | 2.645 | 3.164 | 19.6 | 2.878 | 3.448 | 19.8 | 2.627 | 3.171 | 20.7 | 2.402 | 2.855 | 18.9 |  |
|  | 30 | 3.321 | 4.233 | 27.5 | 3.573 | 4.542 | 27.1 | 3.301 | 4.242 | 28.5 | 3.023 | 3.863 | 27.8 |  |
| $30 \%$ | 26 | 4.702 | 5.873 | 24.9 | 4.028 | 3.448 | -14.4 | 3.412 | 4.15 | 21.6 | 2.402 | 2.855 | 18.9 |  |
|  | 30 | 5.458 | 7.03 | 28.8 | 4.752 | 4.542 | -4.4 | 4.102 | 5.239 | 27.7 | 3.023 | 3.863 | 27.8 |  |
| $42 \%$ | 26 | 5.912 | 7.472 | 26.4 | 4.872 | 5.838 | 19.8 | 4.003 | 4.909 | 22.6 | 3.221 | 3.717 | 15.4 |  |
|  | 30 | 6.682 | 8.64 | 29.3 | 5.607 | 6.974 | 24.4 | 4.702 | 6.006 | 27.7 | 3.727 | 4.571 | 22.6 |  |
| $85 \%$ | 26 | 9.692 | 12.418 | 28.1 | 7.564 | 9.075 | 20.0 | 5.828 | 7.216 | 23.8 | 4.523 | 5.109 | 13.0 |  |
|  | 30 | 10.48 | 13.601 | 29.8 | 8.316 | 10.231 | 23.0 | 6.539 | 8.328 | 27.4 | 4.912 | 5.798 | 18.0 |  |


| LLG Fault | Bus | Wind |  |  |  | Diesel Hybrid |  |  | Hybrid |  |  | PV |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Penetration Level | No | ANSI | IEC | $\%$ | ANSI | IEC | \% | ANSI | IEC | \% | ANSI | IEC | \% |  |
| $0 \%$ | 26 | 2.526 | 3.017 | 19.4 | 2.526 | 3.017 | 19.4 | 2.526 | 3.017 | 19.4 | 2.526 | 3.017 | 19.4 |  |
|  | 30 | 3.241 | 4.147 | 28.0 | 3.241 | 4.147 | 28.0 | 3.241 | 4.147 | 28.0 | 3.241 | 4.147 | 28.0 |  |
| $10 \%$ | 26 | 3.499 | 4.191 | 19.8 | 3.206 | 3.84 | 19.8 | 2.924 | 3.531 | 20.8 | 2.757 | 3.229 | 17.1 |  |
|  | 30 | 4.191 | 5.27 | 25.7 | 3.925 | 4.971 | 26.6 | 3.632 | 4.651 | 28.1 | 3.394 | 4.24 | 24.9 |  |
| $30 \%$ | 26 | 6.02 | 7.832 | 30.1 | 4.377 | 3.84 | -12.3 | 3.69 | 4.508 | 22.2 | 2.757 | 3.229 | 17.1 |  |
|  | 30 | 6.839 | 9.047 | 32.3 | 5.09 | 4.971 | -2.3 | 4.385 | 5.612 | 28.0 | 3.394 | 4.24 | 24.9 |  |
| $42 \%$ | 26 | 7.747 | 10.353 | 33.6 | 5.228 | 6.278 | 20.1 | 4.269 | 5.264 | 23.3 | 3.806 | 4.34 | 14.0 |  |
|  | 30 | 8.615 | 11.621 | 34.9 | 5.933 | 7.388 | 24.5 | 4.955 | 6.356 | 28.3 | 4.356 | 5.228 | 20.0 |  |
| $85 \%$ | 26 | 12.744 | 17.543 | 37.7 | 7.942 | 9.551 | 20.3 | 6.074 | 7.569 | 24.6 | 5.313 | 5.965 | 12.3 |  |
|  | 30 | 13.666 | 18.869 | 38.1 | 8.626 | 10.635 | 23.3 | 6.734 | 8.628 | 28.1 | 5.792 | 6.737 | 16.3 |  |

From Tables 6.4 - 6.9, it could be observed that the IEC simulated results are much higher than the ANSI simulated results in most of the examined scenarios, except in few instances. This occurred at $85 \%$ penetration level of hybrid in scenario S4 for 3ph, LL and LLG fault. Also, IEC results were lower than ANSI results in scenarios S5 and S6 more frequently than in S1-S4.

### 6.8 Summary

This chapter main objective was to investigate the impact of four different cases of DG types on the short circuit current of the IEEE 30 bus system. Six different scenarios representing different locations on the system under study has been selected after conducting load flow analysis with no DG installed. The load flow analysis has been performed after DG penetration, and it showed that the system was unable to adopt the higher levels of penetration including $42 \%$ and $85 \%$, especially for lower bus voltages.

It is could be concluded that the wind had the most significant impact on the short circuit currents in comparison to the other types of DG used, in particular during the occurrence of LG fault on buses 30, 29, and 26 respectively. The PV maintained the lowest impact on the SCCs through all the scenarios examined. The performance of diesel hybrid and hybrid system seemed to be fluctuating, varying the short circuit currents while varying the DG capacity, location and penetration level. The increase in penetration levels is found to have substantial influence on the short circuit currents with higher penetrations as $42 \%$ and $85 \%$, as occurred in different scenarios examined. The $30 \%$ penetration level showed moderate results, though in case of wind in particular at the occurrence of LG and LLG faults, the results were exceptionally high in comparison to other types of DG used.

The IEC simulated results are found to be more than the ANSI results up to $68 \%$ approximately. This confirms that IEC method is much more conservative than ANSI method.

## Chapter Seven

## 7 Conclusions and Future Work

The main aim of the current research was to investigate the impact of wind, PV, and their mix including diesel generators on the short circuit current in electrical distribution network using different calculation methods such as IEEE/ANSI and IEC.

This research motivation and drive have been presented in chapter one. The increased deployment of distributed generation to meet environmental targets, to ensure diversity of supply, and to meet increasing demand have created enormous technical challenges on the electrical power distribution systems that need to be addressed and tackled.

The introduction of distributed generation into the distribution networks has evolved their principal properties from being passive to being active, and the flow of power from unidirectional to being bi directional. Consequently, this caused some power systems operational issues to occur such as power quality, voltage control and network fault level. Chapter two presented a comprehensive review conducted on the various technical impacts of DG on distributed networks and the simulation studies performed in the existing literature examining the influence of DG on distribution systems parameters in particular short circuit level.

Furthermore, it identified the research gap that previous research have not addressed and investigated. Increased penetration level; diversified DG location; calculation of symmetrical and unsymmetrical faults using different methods were never proposed and implemented. This has led to the proposed main research objectives and contribution to investigate the impact of different types and mixes of DG including Wind, PV, and diesel generators on short circuit level on large distribution systems with considerable number of buses using different calculation methods.

Chapter three attempted to illustrate the relation between the distributed generation, its integration into distribution networks specifically, and the importance of short circuit studies. The penetration of DG (as renewable sources) into distributed
systems is more practical and achievable than connection into transmission systems. Geographical locations of resources are more likely to be near the load; easily accessible and manageable operation and maintenance of generators; and high cost of high voltage transformers and switchgears is avoided; and high cost of high voltage transformers and switchgears is avoided.

Despite the several advantages that DG provides, its integration may have a significant impact on short circuit that as a consequence may affect the protection equipment, relay settings and coordination. As a consequence, the system reliability and robustness will be affected. Therefore, short circuit study is a fundamental examination that should be precisely considered.

In chapter four, the IEC and ANSI methods for short circuit calculations have been presented in details. Both methods require detailed modelling of system components for the short circuit calculations, hence, IEC requires more detailed data to be available than ANSI.

The IEC differentiates between the network types either radial or loop, and distinguishes whether or not the generator location is near or far from the short circuit point in short circuit currents calculations. Whereas, ANSI considers the generator location either to be remote or local depending on the transformation impedance value between the generator and the short circuit location.

In chapter five, the first objective of this thesis has been executed where the modified IEEE 13 bus distribution test system has been modelled in ETAP 12. The simulation included the short circuit analysis using the two standards ANSI/IEEE and IEC. The study considered the impact of different types of DG (wind, PV, hybrid, and diesel hybrid) and the impact of their location. Different penetration levels as $10 \%$; $30 \%$; $42 \%$; and $85 \%$ of diesel hybrid integration into the system were examined.

The results of this investigation show that the 3-ph fault is the highest type of fault in comparison to all types of fault tested for both calculation methods IEC and ANSI. Surprisingly, the LL-G fault is found to be the highest unsymmetrical fault. This finding is contrary to previous studies which have suggested that LG is the common type of fault likely to occur and on this basis it is the most type of fault tested.

The investigation of impact of DG types on the short circuit current finds that wind has the most significant impact on the short circuit currents in particular when connected as the only DG source. Whereas, PV made no significant difference to short circuit current in all scenarios.

The results indicate that the short circuit currents are affected by the location of DG especially when the DG is connected near the utility grid, where the maximum values of SCCs were observed. These findings suggest that in general the optimal location for DG is as far as possible from the utility grid to minimize the impact of DG on short circuit current.

The examination of the different penetration levels shows that there is a direct relation between the penetration level of DG and the SCCs. The results show that as the penetration level increases the short circuit current increases.

The ANSI and IEC simulated results for the same system and scenarios applied are found to be not identical. The results for the IEC method are higher than the results for ANSI method. This finding is expected to be found due to the impedance correction factors and voltage factor c considered by the IEC method.

In chapter six, the main objective was to support the initial findings from the investigations applied in chapter five, however, on larger system as IEEE 30 bus system. Accordingly, more scenarios were examined representing different locations. In this system, there was no utility grid to set as a reference to decide the DG location. Therefore, the criteria came out after conducting load flow analysis with no DG installed. The load flow analysis has been performed after DG penetration, and it showed that the system was unable to adopt the higher levels of penetration including $42 \%$ and $85 \%$, especially for lower bus voltages.

Similarly, the results show that the wind had the most significant impact on the short circuit currents in comparison to the other types of DG used and the PV had no recognised influence on the on the SCCs.

The IEC simulated results are found to be more than the ANSI results up to $68 \%$ approximately. This confirms that IEC method is much more conservative than ANSI method.

The most obvious finding to emerge from this study is that for the short circuit calculations using the IEC method leads to more conservative results than ANSI standard.

The second major finding was that all types of fault are crucial and there is no one type of fault more dominant or more common than the other, in which research has always focused only three phase and single line to ground faults. Though, full short circuit studies should be performed taking into consideration all types of fault for precise results and appropriate equipment sizing, reliable relay settings and coordination.

### 7.1 Future work

A number of proposed future works could be extended from this research such as performing the same study on systems with higher number of busses including the GB grid. The study on existing grid would add to current contributions and assures the research findings significance. Also, a methodology of allocating the DG technologies among the network with less impact is needed to be identified in order to set an appropriate guideline for distribution network operators to facilitate the design and implementation of DG integration. The impact of different short circuit calculations methods on the relay settings and coordination scheme of protection equipment in distributed networks is an opportunity for further studies to be carried out to ensure system protection and reliability. Furthermore, identifying the opportunities on to how to limit the impact of different DG technologies on the short circuit currents when will be located near utility grids. This is a crucial study that could be executed to limit the impact of DG on short circuit currents when connected to the nearest point to the grid, where in real situations could not be avoided. Meanwhile, higher penetration levels are uncertain and have negative impact on the power systems stability and short circuit currents. Therefore, a future prospective could be to identify the maximum permissible penetration level while maintaining system stability.

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## Appendix A

## IEEE 13 Bus Distribution Test System Data



Figure A1 - One Line Diagram of IEEE-13 bus distribution test system

Table A1 - Underground Line Configuration Data

| Configuration | Phasing | Cable | Neutral | Space ID |
| :---: | :---: | :---: | :---: | :---: |
| 606 | A B C N | 250,000 AA, CN | None | 515 |
| 607 | A N | $1 / 0 \mathrm{AA}, \mathrm{TS}$ | $1 / 0 \mathrm{Cu}$ | 520 |

Table A2 - Overhead Line Configuration Data

| Configuration | Phasing | Phase | Neutral | Spacing |
| :---: | :---: | :---: | :---: | :---: |
|  |  | ACSR | ACSR | ID |
| 601 | B A C N | $556,50026 / 7$ | $4 / 06 / 1$ | 500 |
| 602 | C A B N | $4 / 06 / 1$ | $4 / 06 / 1$ | 500 |
| 603 | C B N | $1 / 0$ | $1 / 0$ | 505 |
| 604 | A C N | $1 / 0$ | $1 / 0$ | 505 |
| 605 | C N | $1 / 0$ | $1 / 0$ | 510 |

Table A3 - Transformer Data

|  | kVA | kV-high | kV-low | R - \% | X - \% |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Substation | 5,000 | $115-$ D | 4.16 Gr. Y | 1 | 8 |
| XFM -1 | 500 | $4.16-$ Gr.W | $0.48-$ Gr.W | 1.1 | 2 |

Table A4 - Line Segment Data

| Node A | Node B | Length(ft.) | Configuration |
| :---: | :---: | :---: | :---: |
| 632 | 645 | 500 | 603 |
| 632 | 633 | 500 | 602 |
| 633 | 634 | 0 | XFM-1 |
| 645 | 646 | 300 | 603 |
| 650 | 632 | 2000 | 601 |
| 684 | 652 | 800 | 607 |
| 632 | 671 | 2000 | 601 |
| 671 | 684 | 300 | 604 |
| 671 | 680 | 1000 | 601 |
| 671 | 692 | 0 | Switch |
| 684 | 611 | 300 | 605 |
| 692 | 675 | 500 | 606 |

Table A5 - Capacitor Data

| Node | Ph-A | Ph-B | Ph-C |
| :---: | :---: | :---: | :---: |
|  | kVAr | kVAr | kVAr |
| 675 | 200 | 200 | 200 |
| 611 |  |  | 100 |
| Total | 200 | 200 | 300 |

Table A6 - Regulator Data

| Regulator ID | 1 |  |  |
| :--- | :---: | :---: | :---: |
| Line Segment | $650-632$ |  |  |
| Location | 650 |  |  |
| Phases | A-B-C |  |  |
| Connection | 3-Ph, LG |  |  |
| Monitoring Phase | A-B-C |  |  |
| Bandwidth | 2.0 volts |  |  |
| PT Ratio | 20 |  |  |
| Primary CT Rating | 700 |  |  |
| Compensator Settings | Ph-A | Ph-B | Ph-C |
| R-Setting | 3 | 3 | 3 |
| X-Setting | 9 | 9 | 9 |
| Voltage Level | 122 | 122 | 122 |

Table A7 - Distribution Load Data

| Node A | Node B | Load | Ph-1 | Ph-1 | Ph-2 | Ph-2 | Ph-3 | Ph-3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | kW | kVAr | kW | kVAr | kW | kVAr |
| 632 | 671 | Y-PQ | 17 | 10 | 66 | 38 | 117 | 68 |

Table A8 - Spot Load Data

| Node | Load | Ph-1 | Ph-1 | Ph-2 | Ph-2 | Ph-3 | Ph-3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Model | kW | kVAr | kW | kVAr | kW | kVAr |
| 634 | Y-PQ | 160 | 110 | 120 | 90 | 120 | 90 |
| 645 | Y-PQ | 0 | 0 | 170 | 125 | 0 | 0 |
| 646 | D-Z | 0 | 0 | 230 | 132 | 0 | 0 |
| 652 | Y-Z | 128 | 86 | 0 | 0 | 0 | 0 |
| 671 | D-PQ | 385 | 220 | 385 | 220 | 385 | 220 |
| 675 | Y-PQ | 485 | 190 | 68 | 60 | 290 | 212 |
| 692 | D-I | 0 | 0 | 0 | 0 | 170 | 151 |
| 611 | Y-I | 0 | 0 | 0 | 0 | 170 | 80 |
|  | TOTAL | 1158 | 606 | 973 | 627 | 1135 | 753 |

## Appendix B

## IEEE 30 - Bus Test Data

Table B10 - Load Demand

| Bus | P in MW | Q in Mvar |
| :---: | :---: | :---: |
| 2 | 21.7 | 12.7 |
| 3 | 2.4 | 1.2 |
| 4 | 7.6 | 1.6 |
| 5 | 94.2 | 19.0 |
| 7 | 22.8 | 10.9 |
| 8 | 30.0 | 30.0 |
| 10 | 5.8 | 2.0 |
| 12 | 11.2 | 7.5 |
| 14 | 6.2 | 1.6 |
| 15 | 8.2 | 2.5 |
| 16 | 3.5 | 1.8 |
| 17 | 9.0 | 5.8 |
| 18 | 3.2 | 0.9 |
| 19 | 9.5 | 3.4 |
| 20 | 2.2 | 0.7 |
| 21 | 17.5 | 11.2 |
| 23 | 3.2 | 1.6 |
| 24 | 8.7 | 6.7 |
| 26 | 3.5 | 2.3 |
| 29 | 2.4 | 0.9 |
| 30 | 10.6 | 1.9 |

Table B11 - Generator Controller Setting

| Generator | Bus Type | Voltage per <br> unit | Minimum <br> MVAr | Maximum <br> MVAr |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Slack | 1.05 | N.A. | N.A. |
| 2 | PV | 1.0338 | -20.0 | 60.0 |
| 5 | PV | 1.0058 | -15.0 | 62.5 |
| 8 | PV | 1.0230 | -15.0 | 50.0 |
| 11 | PV | 1.0913 | -10.0 | 40.0 |
| 13 | PV | 1.0883 | -15.0 | 45.0 |

Table B12 - Transformer Data

| Transformer No. | Between Buses | X per unit | Tap Setting |
| :---: | :---: | :---: | :---: |
| 1 | $6-9$ | 0.2080 | 1.0155 |
| 2 | $6-10$ | 0.5560 | 0.9629 |
| 3 | $4-12$ | 0.2560 | 1.0129 |
| 4 | $27-28$ | 0.3960 | 0.9581 |
| 5 | $9-11$ | 0.2080 | 0.0000 |
| 6 | $9-10$ | 0.1100 | 0.0000 |
| 7 | $12-13$ | 0.1400 | 0.0000 |

Table B13 - Line Data

| Line No. | Between Buses | R per unit | X per unit | Susceptance per unit |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 1-2 | 0.0192 | 0.0575 | 0.0528 |
| 2 | 1-3 | 0.0452 | 0.1852 | 0.0408 |
| 3 | 2-4 | 0.0570 | 0.1737 | 0.0368 |
| 4 | 3-4 | 0.0132 | 0.0379 | 0.0084 |
| 5 | 2-5 | 0.0472 | 0.1983 | 0.0418 |
| 6 | 2-6 | 0.0581 | 0.1763 | 0.0374 |
| 7 | 4-6 | 0.0119 | 0.0414 | 0.0090 |
| 8 | 5-7 | 0.0460 | 0.1160 | 0.0204 |
| 9 | 6-7 | 0.0267 | 0.0820 | 0.0170 |
| 10 | 6-8 | 0.0120 | 0.0420 | 0.0090 |
| 11 | 6-9 | 0.0 | 0.2080 | 0.0 |
| 12 | 6-10 | 0.0 | 0.5560 | 0.0 |
| 13 | 9-11 | 0.0 | 0.2080 | 0.0 |
| 14 | 9-10 | 0.0 | 0.1100 | 0.0 |
| 15 | 4-12 | 0.0 | 0.2560 | 0.0 |
| 16 | 12-13 | 0.0 | 0.1400 | 0.0 |
| 17 | 12-14 | 0.1231 | 0.2559 | 0.0 |
| 18 | 12-15 | 0.0662 | 0.1304 | 0.0 |
| 19 | 12-16 | 0.0945 | 0.1987 | 0.0 |
| 20 | 14-15 | 0.2210 | 0.1997 | 0.0 |
| 21 | 16-17 | 0.0824 | 0.1932 | 0.0 |
| 22 | 15-18 | 0.1070 | 0.2185 | 0.0 |
| 23 | 18-19 | 0.0639 | 0.1292 | 0.0 |
| 24 | 19-20 | 0.0340 | 0.0680 | 0.0 |
| 25 | 10-20 | 0.0936 | 0.2090 | 0.0 |
| 26 | 10-17 | 0.0324 | 0.0845 | 0.0 |
| 27 | 10-21 | 0.0348 | 0.0749 | 0.0 |
| 28 | 10-22 | 0.0727 | 0.1499 | 0.0 |
| 29 | 21-22 | 0.0116 | 0.0236 | 0.0 |
| 30 | 15-23 | 0.1000 | 0.2020 | 0.0 |
| 31 | 22-24 | 0.1150 | 0.1790 | 0.0 |
| 32 | 23-24 | 0.1320 | 0.2700 | 0.0 |
| 33 | 24-25 | 0.1885 | 0.3292 | 0.0 |


| 34 | $25-26$ | 0.2544 | 0.3800 | 0.0 |
| :---: | :---: | :---: | :---: | :---: |
| 35 | $25-27$ | 0.1093 | 0.2087 | 0.0 |
| 36 | $27-28$ | 0.0 | 0.3960 | 0.0 |
| 37 | $27-29$ | 0.2198 | 0.4153 | 0.0 |
| 38 | $27-30$ | 0.3202 | 0.6027 | 0.0 |
| 39 | $29-30$ | 0.2399 | 0.4533 | 0.0 |
| 40 | $8-28$ | 0.0636 | 0.2000 | 0.0428 |
| 41 | $6-28$ | 0.0169 | 0.0599 | 0.0130 |

Table B14-Shunt Capacitor Data

| Bus No. | Susceptance per unit |
| :---: | :---: |
| 10 | 0.19 |
| 24 | 0.04 |

Table B15 - Voltage Level of Each Buses

| Bus No. | Voltage Magnitude in kV |
| :---: | :---: |
| 1 | 132 |
| 2 | 132 |
| 3 | 132 |
| 4 | 132 |
| 5 | 132 |
| 6 | 132 |
| 7 | 132 |
| 8 | 132 |
| 9 | 132 |
| 10 | 33 |
| 11 | 18 |
| 12 | 33 |
| 13 | 18 |
| 14 | 33 |
| 15 | 33 |
| 16 | 33 |
| 17 | 33 |
| 18 | 33 |
| 19 | 33 |
| 20 | 33 |
| 21 | 33 |
| 22 | 33 |
| 23 | 33 |
| 24 | 33 |
| 25 | 33 |
| 26 | 33 |
| 27 | 33 |
| 28 | 33 |
| 29 | 33 |
| 30 | 33 |

## Appendix C

Table C1 - Load Flow Simulation Results for IEEE 30 Bus test system with no DG connected.

| Bus |  | Voltage |  | Load Flow |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ID | kV | \%Magnitude | Angle | ID | MW | MVAr | Amp | \%PF |
| Bus 1 | 132.0 | 106.0 | 0.0 | Bus 2 | 173.2 | -21.3 | 720.2 | -99.2 |
|  |  |  |  | Bus 3 | 87.7 | 4.5 | 362.5 | 99.9 |
| Bus 2 | 132.0 | 104.3 | -5.4 | Bus 1 | -168.1 | 31.0 | 716.5 | -98.3 |
|  |  |  |  | Bus 4 | 43.6 | 3.9 | 183.7 | 99.6 |
|  |  |  |  | Bus 5 | 82.4 | 1.8 | 345.5 | 100.0 |
|  |  |  |  | Bus 6 | 60.3 | 0.5 | 253.0 | 100.0 |
| Bus 3 | 132.0 | 102.1 | -7.5 | Bus 1 | -84.6 | 2.4 | 362.7 | -100.0 |
|  |  |  |  | Bus 4 | 82.2 | -3.6 | 352.6 | -99.9 |
| Bus 4 | 132.0 | 101.2 | -9.3 | Bus 2 | -42.6 | -4.7 | 185.3 | 99.4 |
|  |  |  |  | Bus 3 | -81.4 | 5.2 | 352.4 | -99.8 |
|  |  |  |  | Bus 6 | 72.2 | -16.3 | 319.8 | -97.5 |
|  |  |  |  | Bus 12 | 44.2 | 14.2 | 200.8 | 95.2 |
| Bus 5 | 132.0 | 101.0 | -14.2 | Bus 2 | -79.4 | 6.2 | 345.0 | -99.7 |
|  |  |  |  | Bus 7 | -14.8 | 11.7 | 81.5 | -78.4 |
| Bus 6 | 132.0 | 101.0 | -11.1 | Bus 2 | -58.4 | 1.5 | 252.9 | -100.0 |
|  |  |  |  | Bus 4 | -71.5 | 17.6 | 318.9 | -97.1 |
|  |  |  |  | Bus 7 | 38.1 | -3.0 | 165.5 | -99.7 |
|  |  |  |  | Bus 8 | 29.6 | -8.1 | 132.7 | -96.5 |
|  |  |  |  | Bus 28 | 18.7 | 0.0 | 80.8 | 100.0 |
|  |  |  |  | Bus 9 | 27.7 | -8.2 | 125.1 | -95.9 |
|  |  |  |  | Bus 10 | 15.8 | 0.2 | 68.6 | 100.0 |
| Bus 7 | 132.0 | 100.2 | -12.9 | Bus 5 | 14.9 | -13.3 | 87.3 | -74.7 |
|  |  |  |  | Bus 6 | -37.7 | 2.4 | 165.0 | -99.8 |
| Bus 8 | 132.0 | 101.0 | -11.8 | Bus 6 | -29.5 | 7.5 | 131.7 | -96.9 |
|  |  |  |  | Bus 28 | -0.5 | -0.4 | 2.9 | 80.1 |
| Bus 9 | 33.0 | 105.1 | -14.1 | Bus 10 | 27.7 | 5.9 | 471.8 | 97.8 |
|  |  |  |  | Bus 6 | -27.7 | 9.8 | 489.4 | -94.3 |
|  |  |  |  | Bus 11 | 0.0 | -15.7 | 261.8 | 0.0 |
| Bus 10 | 33.0 | 104.5 | -15.7 | Bus 9 | -27.7 | -5.1 | 471.8 | 98.3 |
|  |  |  |  | Bus 17 | 5.3 | 4.4 | 115.9 | 76.9 |
|  |  |  |  | Bus 20 | 9.0 | 7.7 | 163.3 | 92.5 |
|  |  |  |  | Bus 21 | 15.8 | 10.0 | 312.9 | 84.4 |
|  |  |  |  | Bus 22 | 7.6 | 4.6 | 149.0 | 85.6 |
|  |  |  |  | Bus 6 | -15.8 | 1.1 | 265.8 | -99.7 |
| Bus 11 | 11.0 | 108.2 | -14.1 | Bus 9 | 0.0 | 16.2 | 785.3 | 0.0 |
| Bus 12 | 11.0 | 105.7 | -14.9 | Bus 14 | 7.9 | 2.4 | 136.0 | 95.6 |
|  |  |  |  | Bus 15 | 17.9 | 6.8 | 316.9 | 93.5 |
|  |  |  |  | Bus 16 | 7.3 | 3.4 | 132.2 | 90.8 |



## Appendix D

The IEEE 30 Bus system short circuit simulated results for ANSI and IEC calculations are presented in Tables D1 - D43.

Table D1: ANSI Simulated Results for Case 1 at $\mathbf{1 0 \%}$ penetration level and DG located at Bus $\mathbf{7}$

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.714 | 11.927 | 8.566 | 11.275 | 9.698 | 11.891 | 8.551 | 11.235 | 9.720 | 11.914 | 8.572 | 11.259 | 9.735 | 11.928 | 8.585 | 11.272 |
| 2 | 132 | 8.557 | 9.535 | 7.486 | 9.196 | 8.532 | 9.447 | 7.466 | 9.121 | 8.568 | 9.479 | 7.501 | 9.161 | 8.594 | 9.499 | 7.522 | 9.184 |
| 3 | 132 | 5.272 | 5.349 | 4.586 | 5.360 | 5.258 | 5.287 | 4.573 | 5.319 | 5.279 | 5.303 | 4.593 | 5.343 | 5.294 | 5.313 | 4.606 | 5.356 |
| 4 | 132 | 6.736 | 6.720 | 5.865 | 6.820 | 6.709 | 6.592 | 5.840 | 6.475 | 6.750 | 6.622 | 5.880 | 6.792 | 6.781 | 6.640 | 5.905 | 6.819 |
| 5 | 132 | 5.712 | 5.725 | 4.976 | 5.762 | 5.678 | 5.568 | 4.945 | 5.664 | 5.728 | 5.604 | 4.994 | 5.720 | 5.766 | 5.627 | 5.025 | 5.753 |
| 6 | 132 | 7.615 | 7.622 | 6.636 | 7.710 | 7.565 | 7.370 | 6.590 | 7.570 | 7.641 | 7.425 | 6.666 | 7.660 | 7.702 | 7.461 | 6.716 | 7.714 |
| 7 | 132 | 5.101 | 5.267 | 4.438 | 5.217 | 5.022 | 4.798 | 4.362 | 4.926 | 5.156 | 4.892 | 4.497 | 5.094 | 5.273 | 4.959 | 4.595 | 5.203 |
| 8 | 132 | 5.718 | 5.860 | 4.983 | 5.829 | 5.695 | 5.752 | 4.962 | 5.762 | 5.729 | 5.778 | 4.996 | 5.801 | 5.755 | 5.795 | 5.017 | 5.824 |
| 9 | 33 | 12.975 | 13.217 | 11.279 | 13.284 | 12.960 | 13.206 | 11.266 | 13.279 | 12.985 | 13.225 | 11.290 | 13.292 | 13.006 | 13.239 | 11.307 | 13.307 |
| 10 | 33 | 14.620 | 14.140 | 12.694 | 14.634 | 14.606 | 14.131 | 12.680 | 14.629 | 14.630 | 14.147 | 12.704 | 14.642 | 14.650 | 14.159 | 12.720 | 14.657 |
| 11 | 11 | 19.167 | 22.972 | 16.703 | 21.877 | 19.160 | 22.965 | 16.697 | 21.875 | 19.172 | 22.978 | 16.708 | 21.881 | 19.183 | 22.987 | 16.717 | 21.889 |
| 12 | 33 | 12.577 | 12.098 | 10.926 | 12.542 | 12.567 | 12.092 | 10.916 | 12.538 | 12.583 | 12.102 | 10.932 | 12.547 | 12.595 | 12.110 | 10.942 | 12.557 |
| 13 | 11 | 21.025 | 25.755 | 18.341 | 24.916 | 21.084 | 25.748 | 18.335 | 24.913 | 21.096 | 25.761 | 18.346 | 24.920 | 21.106 | 25.770 | 18.354 | 24.928 |
| 14 | 33 | 6.800 | 6.499 | 5.894 | 6.697 | 6.796 | 6.497 | 5.891 | 6.695 | 6.801 | 6.501 | 5.895 | 6.698 | 6.804 | 6.503 | 5.898 | 6.701 |
| 15 | 33 | 10.365 | 9.773 | 8.989 | 10.169 | 10.357 | 9.768 | 8.982 | 10.165 | 10.368 | 9.775 | 8.993 | 10.173 | 10.376 | 9.780 | 8.999 | 10.179 |
| 16 | 33 | 8.423 | 8.159 | 7.304 | 8.379 | 8.418 | 8.155 | 7.299 | 8.376 | 8.426 | 8.161 | 7.307 | 8.381 | 8.432 | 8.164 | 7.312 | 8.385 |
| 17 | 33 | 10.640 | 10.214 | 9.228 | 10.548 | 10.632 | 10.209 | 9.221 | 10.544 | 10.664 | 10.218 | 9.233 | 10.552 | 10.654 | 10.223 | 9.241 | 10.559 |
| 18 | 33 | 7.089 | 6.705 | 6.143 | 6.932 | 7.085 | 6.702 | 6.140 | 6.930 | 7.090 | 6.706 | 6.145 | 6.934 | 7.094 | 6.708 | 6.148 | 6.937 |
| 19 | 33 | 7.382 | 6.923 | 6.398 | 7.177 | 7.378 | 6.920 | 6.394 | 7.174 | 7.384 | 6.924 | 6.400 | 7.179 | 7.388 | 6.926 | 6.403 | 7.182 |
| 20 | 33 | 7.716 | 7.315 | 6.688 | 7.558 | 7.712 | 7.312 | 6.684 | 7.556 | 7.718 | 7.316 | 6.690 | 7.560 | 7.723 | 7.319 | 6.694 | 7.564 |
| 21 | 33 | 11.923 | 11.302 | 10.342 | 11.728 | 11.913 | 11.295 | 10.332 | 11.723 | 11.928 | 11.306 | 10.348 | 11.732 | 11.941 | 11.313 | 10.358 | 11.742 |
| 22 | 33 | 11.680 | 11.129 | 10.131 | 11.529 | 11.670 | 11.122 | 10.121 | 11.524 | 11.686 | 11.133 | 10.136 | 11.534 | 11.698 | 11.140 | 10.146 | 11.543 |
| 23 | 33 | 7.016 | 6.718 | 6.080 | 6.905 | 7.012 | 6.715 | 6.076 | 6.903 | 7.017 | 6.719 | 6.081 | 6.906 | 7.021 | 6.721 | 6.084 | 6.909 |
| 24 | 33 | 8.761 | 8.336 | 7.593 | 8.584 | 8.755 | 8.332 | 7.587 | 8.581 | 8.764 | 8.338 | 7.596 | 8.587 | 8.770 | 8.341 | 7.601 | 8.592 |
| 25 | 33 | 5.673 | 5.576 | 4.916 | 5.657 | 5.670 | 5.574 | 4.913 | 5.656 | 5.675 | 5.577 | 4.917 | 5.658 | 5.678 | 5.579 | 4.920 | 5.661 |
| 26 | 33 | 2.551 | 2.447 | 2.210 | 2.527 | 2.551 | 2.446 | 2.209 | 2.526 | 2.552 | 2.447 | 2.210 | 2.527 | 2.552 | 2.447 | 2.211 | 2.528 |
| 27 | 33 | 6.223 | 6.221 | 5.394 | 6.315 | 6.220 | 6.219 | 5.390 | 6.313 | 6.225 | 6.223 | 5.396 | 6.317 | 6.230 | 6.226 | 5.400 | 6.320 |
| 28 | 132 | 4.469 | 4.398 | 3.884 | 4.470 | 4.453 | 4.318 | 3.869 | 4.425 | 4.477 | 4.336 | 3.893 | 4.453 | 4.496 | 4.347 | 3.908 | 4.469 |
| 29 | 33 | 3.290 | 3.137 | 2.850 | 3.233 | 3.289 | 3.137 | 2.849 | 3.232 | 3.291 | 3.138 | 2.851 | 3.233 | 3.292 | 3.138 | 2.852 | 3.234 |
| 30 | 33 | 3.316 | 3.036 | 2.872 | 3.242 | 3.315 | 3.035 | 2.871 | 3.241 | 3.316 | 3.036 | 2.873 | 3.243 | 3.317 | 3.037 | 2.874 | 3.244 |

Table D2: ANSI Simulated Results for Case 1 at $\mathbf{3 0 \%}$ penetration level and DG located at Bus $\mathbf{7}$

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.779 | 11.993 | 8.625 | 11.333 | 9.698 | 11.891 | 8.551 | 11.235 | 9.758 | 11.955 | 8.609 | 11.288 | 9.735 | 11.928 | 8.585 | 11.272 |
| 2 | 132 | 8.673 | 9.634 | 7.594 | 9.298 | 8.532 | 9.447 | 7.466 | 9.121 | 8.640 | 9.542 | 7.569 | 9.216 | 8.594 | 9.499 | 7.522 | 9.184 |
| 3 | 132 | 5.341 | 5.397 | 4.649 | 5.419 | 5.258 | 5.287 | 4.573 | 5.319 | 5.322 | 5.334 | 4.634 | 5.375 | 5.294 | 5.313 | 4.606 | 5.356 |
| 4 | 132 | 6.875 | 6.816 | 5.992 | 6.945 | 6.709 | 6.592 | 5.840 | 6.745 | 6.839 | 6.683 | 5.965 | 6.863 | 6.781 | 6.640 | 5.905 | 6.819 |
| 5 | 132 | 5.882 | 5.843 | 5.133 | 5.913 | 5.678 | 5.568 | 4.945 | 5.664 | 5.837 | 5.679 | 5.097 | 5.805 | 5.766 | 5.627 | 5.025 | 5.753 |
| 6 | 132 | 7.891 | 7.815 | 6.891 | 7.965 | 7.565 | 7.370 | 6.590 | 7.570 | 7.825 | 7.548 | 6.840 | 7.810 | 7.702 | 7.461 | 6.716 | 7.714 |
| 7 | 132 | 5.671 | 5.684 | 4.970 | 5.704 | 5.022 | 4.798 | 4.362 | 4.926 | 5.555 | 5.144 | 4.879 | 5.437 | 5.273 | 4.959 | 4.595 | 5.203 |
| 8 | 132 | 5.835 | 5.946 | 5.091 | 5.935 | 5.695 | 5.752 | 4.962 | 5.762 | 5.805 | 5.833 | 5.068 | 5.862 | 5.755 | 5.795 | 5.017 | 5.824 |
| 9 | 33 | 13.071 | 13.286 | 11.367 | 13.357 | 12.960 | 13.206 | 11.266 | 13.279 | 13.053 | 13.275 | 11.353 | 13.352 | 13.006 | 13.239 | 11.307 | 13.307 |
| 10 | 33 | 14.713 | 14.200 | 12.778 | 14.706 | 14.606 | 14.131 | 12.680 | 14.629 | 14.694 | 14.191 | 12.764 | 14.700 | 14.650 | 14.159 | 12.720 | 14.657 |
| 11 | 11 | 19.216 | 23.021 | 16.748 | 21.916 | 19.160 | 22.965 | 16.697 | 21.875 | 19.208 | 23.014 | 16.742 | 21.913 | 19.183 | 22.987 | 16.717 | 21.889 |
| 12 | 33 | 12.634 | 12.134 | 10.977 | 12.588 | 12.567 | 12.092 | 10.916 | 12.538 | 12.621 | 12.128 | 10.968 | 12.583 | 12.595 | 12.110 | 10.942 | 12.557 |
| 13 | 11 | 21.136 | 25.802 | 18.382 | 24.954 | 21.084 | 25.748 | 18.335 | 24.913 | 21.127 | 25.794 | 18.376 | 24.950 | 21.106 | 25.770 | 18.354 | 24.928 |
| 14 | 33 | 6.814 | 6.509 | 5.907 | 6.710 | 6.796 | 6.497 | 5.891 | 6.695 | 6.810 | 6.506 | 5.904 | 6.707 | 6.804 | 6.503 | 5.898 | 6.701 |
| 15 | 33 | 10.399 | 9.794 | 9.021 | 10.199 | 10.357 | 9.768 | 8.982 | 10.165 | 10.390 | 9.789 | 9.013 | 10.194 | 10.376 | 9.780 | 8.999 | 10.179 |
| 16 | 33 | 8.449 | 8.176 | 7.328 | 8.400 | 8.418 | 8.155 | 7.299 | 8.376 | 8.443 | 8.172 | 7.323 | 8.397 | 8.432 | 8.164 | 7.312 | 8.385 |
| 17 | 33 | 10.684 | 10.243 | 9.269 | 10.583 | 10.632 | 10.209 | 9.221 | 10.544 | 10.674 | 10.237 | 9.261 | 10.579 | 10.654 | 10.223 | 9.241 | 10.559 |
| 18 | 33 | 7.105 | 6.715 | 6.158 | 6.946 | 7.085 | 6.702 | 6.140 | 6.930 | 7.100 | 6.712 | 6.154 | 6.944 | 7.094 | 6.708 | 6.148 | 6.937 |
| 19 | 33 | 7.400 | 6.934 | 6.414 | 7.192 | 7.378 | 6.920 | 6.394 | 7.174 | 7.395 | 6.931 | 6.410 | 7.188 | 7.388 | 6.926 | 6.403 | 7.182 |
| 20 | 33 | 7.737 | 7.328 | 6.707 | 7.576 | 7.712 | 7.312 | 6.684 | 7.556 | 7.731 | 7.325 | 6.702 | 7.573 | 7.723 | 7.319 | 6.694 | 7.564 |
| 21 | 33 | 11.979 | 11.337 | 10.392 | 11.772 | 11.913 | 11.295 | 10.332 | 11.723 | 11.965 | 11.330 | 10.382 | 11.767 | 11.941 | 11.313 | 10.358 | 11.742 |
| 22 | 33 | 11.734 | 11.163 | 10.180 | 11.573 | 11.670 | 11.122 | 10.121 | 11.524 | 11.721 | 11.156 | 10.170 | 11.567 | 11.698 | 11.140 | 10.146 | 11.543 |
| 23 | 33 | 7.032 | 6.728 | 6.094 | 6.919 | 7.012 | 6.715 | 6.076 | 6.903 | 7.027 | 6.725 | 6.091 | 6.916 | 7.021 | 6.721 | 6.084 | 6.909 |
| 24 | 33 | 8.789 | 8.353 | 7.618 | 8.608 | 8.755 | 8.332 | 7.587 | 8.581 | 8.781 | 8.349 | 7.612 | 8.604 | 8.770 | 8.341 | 7.601 | 8.592 |
| 25 | 33 | 5.688 | 5.586 | 4.929 | 5.669 | 5.670 | 5.574 | 4.913 | 5.656 | 5.684 | 5.584 | 4.926 | 5.667 | 5.678 | 5.579 | 4.920 | 5.661 |
| 26 | 33 | 2.554 | 2.448 | 2.212 | 2.529 | 2.551 | 2.446 | 2.209 | 2.526 | 2.553 | 2.448 | 2.211 | 2.528 | 2.552 | 2.447 | 2.211 | 2.528 |
| 27 | 33 | 6.244 | 6.236 | 5.413 | 6.331 | 6.220 | 6.219 | 5.390 | 6.313 | 6.240 | 6.234 | 5.410 | 6.330 | 6.230 | 6.226 | 5.400 | 6.320 |
| 28 | 132 | 4.553 | 4.454 | 3.960 | 4.545 | 4.453 | 4.318 | 3.869 | 4.425 | 4.531 | 4.372 | 3.944 | 4.496 | 4.496 | 4.347 | 3.908 | 4.469 |
| 29 | 33 | 3.295 | 3.141 | 2.855 | 3.237 | 3.289 | 3.137 | 2.849 | 3.232 | 3.294 | 3.140 | 2.854 | 3.236 | 3.292 | 3.138 | 2.852 | 3.234 |
| 30 | 33 | 3.320 | 3.038 | 2.876 | 3.246 | 3.315 | 3.035 | 2.871 | 3.241 | 3.319 | 3.038 | 2.875 | 3.245 | 3.317 | 3.037 | 2.874 | 3.244 |

Table D3: ANSI Simulated Results for Case 2 at $\mathbf{3 0 \%}$ penetration level and DG located at Bus 26

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.724 | 11.916 | 8.574 | 11.262 | 9.700 | 11.892 | 8.553 | 11.240 | 9.715 | 11.908 | 8.567 | 11.254 | 9.711 | 11.903 | 8.563 | 11.252 |
| 2 | 132 | 8.568 | 9.477 | 7.498 | 9.160 | 8.531 | 9.446 | 7.464 | 9.128 | 8.555 | 9.466 | 7.486 | 9.150 | 8.548 | 9.460 | 7.479 | 9.145 |
| 3 | 132 | 5.293 | 5.311 | 4.604 | 5.353 | 5.259 | 5.288 | 4.574 | 5.324 | 5.281 | 5.303 | 4.594 | 5.343 | 5.274 | 5.298 | 4.587 | 5.339 |
| 4 | 132 | 6.781 | 6.640 | 5.904 | 6.815 | 6.711 | 6.593 | 5.841 | 6.753 | 6.756 | 6.624 | 5.882 | 6.794 | 6.739 | 6.613 | 5.867 | 6.783 |
| 5 | 132 | 5.680 | 5.570 | 4.947 | 5.681 | 5.667 | 5.561 | 4.935 | 5.670 | 5.676 | 5.567 | 4.943 | 5.677 | 5.673 | 5.565 | 4.940 | 5.676 |
| 6 | 132 | 7.685 | 7.447 | 6.698 | 7.692 | 7.563 | 7.369 | 6.588 | 7.583 | 7.640 | 7.420 | 6.659 | 7.655 | 7.610 | 7.400 | 6.631 | 7.634 |
| 7 | 132 | 4.979 | 4.773 | 4.325 | 4.937 | 4.951 | 4.755 | 4.300 | 4.913 | 4.969 | 4.767 | 4.316 | 4.929 | 4.963 | 4.763 | 4.310 | 4.925 |
| 8 | 132 | 5.761 | 5.797 | 5.021 | 5.826 | 5.698 | 5.754 | 4.965 | 5.770 | 5.738 | 5.782 | 5.001 | 5.807 | 5.723 | 5.771 | 4.987 | 5.796 |
| 9 | 33 | 13.120 | 13.366 | 11.409 | 13.417 | 12.967 | 13.211 | 11.272 | 13.294 | 13.065 | 13.283 | 11.362 | 13.377 | 13.033 | 13.258 | 11.330 | 13.340 |
| 10 | 33 | 14.896 | 14.435 | 12.940 | 14.883 | 14.614 | 14.137 | 12.687 | 14.661 | 14.795 | 14.257 | 12.855 | 14.825 | 14.746 | 14.221 | 12.805 | 14.761 |
| 11 | 11 | 19.244 | 23.047 | 16.772 | 21.954 | 19.165 | 22.969 | 16.701 | 21.884 | 19.216 | 23.020 | 16.748 | 21.928 | 19.198 | 23.002 | 16.730 | 21.908 |
| 12 | 33 | 12.691 | 12.214 | 11.027 | 12.639 | 12.567 | 12.092 | 10.917 | 12.548 | 12.647 | 12.144 | 10.990 | 12.621 | 12.627 | 12.129 | 10.970 | 12.594 |
| 13 | 11 | 21.187 | 25.853 | 18.427 | 25.022 | 21.086 | 25.751 | 18.337 | 24.923 | 21.151 | 25.819 | 18.397 | 24.985 | 21.133 | 25.798 | 18.379 | 24.962 |
| 14 | 33 | 6.833 | 6.535 | 5.923 | 6.722 | 6.793 | 6.496 | 5.888 | 6.696 | 6.819 | 6.512 | 5.912 | 6.722 | 6.815 | 6.509 | 5.907 | 6.714 |
| 15 | 33 | 10.493 | 9.914 | 9.103 | 10.284 | 10.363 | 9.772 | 8.988 | 10.183 | 10.447 | 9.825 | 9.065 | 10.258 | 10.425 | 9.809 | 9.043 | 10.230 |
| 16 | 33 | 8.481 | 8.220 | 7.355 | 8.426 | 8.417 | 8.155 | 7.299 | 8.381 | 8.458 | 8.182 | 7.337 | 8.419 | 8.449 | 8.175 | 7.327 | 8.406 |
| 17 | 33 | 10.756 | 10.338 | 9.332 | 10.647 | 10.631 | 10.209 | 9.211 | 10.555 | 10.712 | 10.262 | 9.295 | 10.629 | 10.693 | 10.248 | 9.275 | 10.603 |
| 18 | 33 | 7.137 | 6.759 | 6.186 | 6.973 | 7.085 | 6.702 | 6.140 | 6.935 | 7.119 | 6.724 | 6.171 | 6.967 | 7.112 | 6.719 | 6.164 | 6.956 |
| 19 | 33 | 7.432 | 6.979 | 6.442 | 7.241 | 7.377 | 6.920 | 6.393 | 7.178 | 7.413 | 6.942 | 6.426 | 7.212 | 7.406 | 6.937 | 6.418 | 7.201 |
| 20 | 33 | 7.774 | 7.378 | 6.739 | 7.606 | 7.711 | 7.311 | 6.683 | 7.561 | 7.752 | 7.337 | 6.721 | 7.600 | 7.743 | 7.331 | 6.712 | 7.587 |
| 21 | 33 | 12.187 | 11.591 | 10.577 | 11.969 | 11.926 | 11.304 | 10.344 | 11.760 | 12.093 | 11.410 | 10.499 | 11.910 | 12.048 | 11.379 | 10.453 | 11.853 |
| 22 | 33 | 11.977 | 11.456 | 10.395 | 11.804 | 11.688 | 11.134 | 10.137 | 11.569 | 11.873 | 11.253 | 10.308 | 11.734 | 11.822 | 11.217 | 10.257 | 11.669 |
| 23 | 33 | 7.172 | 6.900 | 6.220 | 7.056 | 7.027 | 6.725 | 6.090 | 6.931 | 7.120 | 6.785 | 6.175 | 7.012 | 7.092 | 6.766 | 6.148 | 6.978 |
| 24 | 33 | 9.390 | 9.055 | 8.159 | 9.261 | 8.840 | 8.384 | 7.661 | 8.709 | 9.185 | 8.602 | 7.982 | 8.997 | 9.064 | 8.522 | 7.864 | 8.861 |
| 25 | 33 | 7.720 | 8.057 | 6.784 | 7.936 | 5.991 | 5.784 | 5.191 | 6.066 | 6.986 | 6.407 | 6.127 | 6.854 | 6.532 | 6.122 | 5.690 | 6.391 |
| 26 | 33 | 4.542 | 10.148 | 7.136 | 9.221 | 3.052 | 2.743 | 2.644 | 3.062 | 5.008 | 3.645 | 4.544 | 4.811 | 3.803 | 3.136 | 3.354 | 3.705 |
| 27 | 33 | 7.086 | 7.235 | 6.172 | 7.210 | 6.340 | 6.303 | 5.495 | 6.491 | 6.798 | 6.617 | 5.922 | 6.873 | 6.626 | 6.494 | 5.755 | 6.683 |
| 28 | 132 | 4.561 | 4.388 | 3.966 | 4.524 | 4.470 | 4.329 | 3.884 | 4.438 | 4.527 | 4.367 | 3.936 | 4.494 | 4.502 | 4.350 | 3.913 | 4.476 |
| 29 | 33 | 3.458 | 3.331 | 3.001 | 3.429 | 3.305 | 3.146 | 2.863 | 3.237 | 3.402 | 3.208 | 2.953 | 3.322 | 3.373 | 3.189 | 2.924 | 3.293 |
| 30 | 33 | 3.460 | 3.201 | 3.001 | 3.411 | 3.327 | 3.041 | 2.881 | 3.236 | 3.412 | 3.091 | 2.960 | 3.308 | 3.387 | 3.076 | 2.936 | 3.294 |

Table D4: ANSI Simulated Results for Case 3 at $\mathbf{3 0 \%}$ penetration level and DG located at Bus 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.733 | 11.925 | 8.583 | 11.270 | 9.700 | 11.893 | 8.553 | 11.240 | 9.721 | 11.913 | 8.572 | 11.259 | 9.714 | 11.906 | 8.565 | 11.255 |
| 2 | 132 | 8.583 | 9.489 | 7.511 | 9.174 | 8.532 | 9.447 | 7.465 | 9.128 | 8.563 | 9.474 | 7.494 | 9.157 | 8.552 | 9.463 | 7.483 | 9.150 |
| 3 | 132 | 5.304 | 5.319 | 4.614 | 5.363 | 5.260 | 5.289 | 4.575 | 5.324 | 5.287 | 5.308 | 4.600 | 5.349 | 5.277 | 5.300 | 4.590 | 5.342 |
| 4 | 132 | 6.803 | 6.655 | 5.925 | 6.837 | 6.712 | 6.594 | 5.843 | 6.753 | 6.768 | 6.633 | 5.894 | 6.806 | 6.746 | 6.617 | 5.873 | 6.789 |
| 5 | 132 | 5.686 | 5.573 | 4.952 | 5.686 | 5.668 | 5.562 | 4.935 | 5.670 | 5.679 | 5.569 | 4.946 | 5.680 | 5.675 | 5.566 | 4.942 | 5.678 |
| 6 | 132 | 7.738 | 7.483 | 6.748 | 7.746 | 7.570 | 7.373 | 6.594 | 7.585 | 7.674 | 7.442 | 6.690 | 7.687 | 7.628 | 7.411 | 6.647 | 7.651 |
| 7 | 132 | 4.991 | 4.781 | 4.336 | 4.948 | 4.953 | 4.756 | 4.301 | 4.913 | 4.977 | 4.771 | 4.323 | 4.936 | 4.967 | 4.765 | 4.314 | 4.929 |
| 8 | 132 | 5.794 | 5.821 | 5.052 | 5.858 | 5.703 | 5.757 | 4.969 | 5.772 | 5.759 | 5.797 | 5.021 | 5.826 | 5.734 | 5.779 | 4.997 | 5.808 |
| 9 | 33 | 13.094 | 13.320 | 11.386 | 13.384 | 12.961 | 13.207 | 11.266 | 13.284 | 13.043 | 13.267 | 11.342 | 13.352 | 13.013 | 13.243 | 11.312 | 13.319 |
| 10 | 33 | 14.805 | 14.305 | 12.860 | 14.787 | 14.601 | 14.129 | 12.676 | 14.637 | 14.727 | 14.212 | 12.793 | 14.750 | 14.689 | 14.184 | 12.755 | 14.704 |
| 11 | 11 | 19.230 | 23.033 | 16.759 | 21.937 | 19.161 | 22.966 | 16.698 | 21.878 | 19.204 | 23.009 | 16.737 | 21.914 | 19.187 | 22.991 | 16.721 | 21.896 |
| 12 | 33 | 12.660 | 12.167 | 11.000 | 12.609 | 12.564 | 12.090 | 10.913 | 12.540 | 12.623 | 12.129 | 10.969 | 12.594 | 12.606 | 12.116 | 10.951 | 12.572 |
| 13 | 11 | 21.161 | 25.827 | 18.404 | 24.990 | 21.082 | 25.747 | 18.334 | 24.915 | 21.131 | 25.798 | 18.378 | 24.961 | 21.115 | 25.780 | 18.363 | 24.942 |
| 14 | 33 | 6.822 | 6.518 | 5.914 | 6.714 | 6.793 | 6.496 | 5.888 | 6.694 | 6.811 | 6.507 | 5.905 | 6.712 | 6.808 | 6.505 | 5.901 | 6.706 |
| 15 | 33 | 10.445 | 9.847 | 9.061 | 10.236 | 10.355 | 9.767 | 8.981 | 10.170 | 10.411 | 9.802 | 9.032 | 10.221 | 10.396 | 9.792 | 9.017 | 10.202 |
| 16 | 33 | 8.464 | 8.194 | 7.341 | 8.410 | 8.416 | 8.154 | 7.297 | 8.377 | 8.446 | 8.174 | 7.325 | 8.404 | 8.438 | 8.168 | 7.317 | 8.394 |
| 17 | 33 | 10.719 | 10.283 | 9.300 | 10.611 | 10.628 | 10.207 | 9.218 | 10.546 | 10.684 | 10.244 | 9.270 | 10.598 | 10.669 | 10.233 | 9.254 | 10.578 |
| 18 | 33 | 7.120 | 6.733 | 6.171 | 6.957 | 7.083 | 6.701 | 6.138 | 6.931 | 7.106 | 6.716 | 6.159 | 6.953 | 7.101 | 6.712 | 6.154 | 6.945 |
| 19 | 33 | 7.415 | 6.952 | 6.427 | 7.215 | 7.376 | 6.919 | 6.392 | 7.174 | 7.400 | 6.934 | 6.415 | 7.197 | 7.395 | 6.930 | 6.409 | 7.189 |
| 20 | 33 | 7.755 | 7.349 | 6.722 | 7.588 | 7.709 | 7.310 | 6.682 | 7.557 | 7.737 | 7.328 | 6.708 | 7.583 | 7.731 | 7.323 | 6.701 | 7.574 |
| 21 | 33 | 12.081 | 11.450 | 10.484 | 11.861 | 11.909 | 11.294 | 10.330 | 11.733 | 12.015 | 11.361 | 10.428 | 11.830 | 11.986 | 11.341 | 10.398 | 11.792 |
| 22 | 33 | 11.853 | 11.295 | 10.286 | 11.676 | 11.668 | 11.121 | 10.119 | 11.537 | 11.782 | 11.195 | 10.225 | 11.641 | 11.750 | 11.172 | 10.193 | 11.601 |
| 23 | 33 | 7.098 | 6.805 | 6.154 | 6.978 | 7.012 | 6.716 | 6.077 | 6.911 | 7.065 | 6.750 | 6.126 | 6.959 | 7.051 | 6.740 | 6.111 | 6.941 |
| 24 | 33 | 9.059 | 8.663 | 7.862 | 8.892 | 8.766 | 8.339 | 7.597 | 8.618 | 8.945 | 8.454 | 7.764 | 8.779 | 8.891 | 8.417 | 7.709 | 8.712 |
| 25 | 33 | 6.443 | 6.504 | 5.616 | 6.503 | 5.733 | 5.616 | 4.967 | 5.773 | 6.153 | 5.899 | 5.361 | 6.135 | 6.000 | 5.790 | 5.210 | 5.963 |
| 26 | 33 | 2.667 | 2.586 | 2.315 | 2.668 | 2.554 | 2.448 | 2.213 | 2.518 | 2.623 | 2.493 | 2.277 | 2.575 | 2.603 | 2.479 | 2.256 | 2.563 |
| 27 | 33 | 8.420 | 9.044 | 7.421 | 8.748 | 6.447 | 6.380 | 5.588 | 6.656 | 7.545 | 7.106 | 6.625 | 7.572 | 7.063 | 6.780 | 6.153 | 7.065 |
| 28 | 132 | 4.635 | 4.436 | 4.035 | 4.597 | 4.484 | 4.337 | 3.896 | 4.446 | 4.577 | 4.399 | 3.982 | 4.541 | 4.531 | 4.369 | 3.939 | 4.503 |
| 29 | 33 | 8.342 | 11.025 | 7.836 | 10.047 | 3.705 | 3.390 | 3.210 | 3.737 | 5.745 | 4.396 | 5.188 | 5.436 | 4.564 | 3.848 | 4.015 | 4.386 |
| 30 | 33 | 4.680 | 4.772 | 4.135 | 4.840 | 3.467 | 3.118 | 3.003 | 3.354 | 4.133 | 3.479 | 3.633 | 3.917 | 3.826 | 3.315 | 3.333 | 3.674 |

Table D5: ANSI Simulated Results for Case 4 at $\mathbf{3 0 \%}$ penetration level and DG located at Bus 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.728 | 11.920 | 8.578 | 11.266 | 9.699 | 11.892 | 8.552 | 11.240 | 9.717 | 11.910 | 8.569 | 11.256 | 9.711 | 11.904 | 8.563 | 11.252 |
| 2 | 132 | 8.575 | 9.482 | 7.504 | 9.167 | 8.530 | 9.446 | 7.464 | 9.128 | 8.558 | 9.469 | 7.489 | 9.153 | 8.548 | 9.460 | 7.480 | 9.146 |
| 3 | 132 | 5.297 | 5.314 | 4.608 | 5.357 | 5.258 | 5.288 | 4.573 | 5.323 | 5.282 | 5.305 | 4.595 | 5.345 | 5.274 | 5.298 | 4.587 | 5.339 |
| 4 | 132 | 6.789 | 6.645 | 5.912 | 6.824 | 6.709 | 6.592 | 5.840 | 6.751 | 6.758 | 6.626 | 5.885 | 6.797 | 6.739 | 6.612 | 5.867 | 6.783 |
| 5 | 132 | 5.683 | 5.572 | 4.949 | 5.683 | 5.667 | 5.561 | 4.935 | 5.670 | 5.677 | 5.568 | 4.944 | 5.679 | 5.674 | 5.566 | 4.941 | 5.677 |
| 6 | 132 | 7.711 | 7.466 | 6.723 | 7.720 | 7.563 | 7.369 | 6.588 | 7.581 | 7.654 | 7.430 | 6.673 | 7.669 | 7.616 | 7.403 | 6.636 | 7.639 |
| 7 | 132 | 4.985 | 4.777 | 4.300 | 4.943 | 4.951 | 4.755 | 4.300 | 4.912 | 4.972 | 4.769 | 4.319 | 4.932 | 4.964 | 4.763 | 4.312 | 4.926 |
| 8 | 132 | 5.779 | 5.811 | 5.038 | 5.844 | 5.699 | 5.754 | 4.965 | 5.769 | 5.748 | 5.790 | 5.011 | 5.817 | 5.728 | 5.775 | 4.991 | 5.801 |
| 9 | 33 | 13.072 | 13.303 | 11.367 | 13.366 | 12.957 | 13.204 | 11.262 | 13.279 | 13.028 | 13.256 | 11.329 | 13.339 | 13.003 | 13.236 | 11.304 | 13.311 |
| 10 | 33 | 14.773 | 14.279 | 12.831 | 14.760 | 14.596 | 14.126 | 12.672 | 14.631 | 14.705 | 14.198 | 12.773 | 14.730 | 14.674 | 14.175 | 12.741 | 14.691 |
| 11 | 11 | 19.219 | 23.023 | 16.750 | 21.928 | 19.159 | 22.964 | 16.695 | 21.875 | 19.196 | 23.001 | 16.730 | 21.907 | 19.182 | 22.986 | 16.716 | 21.892 |
| 12 | 33 | 12.645 | 12.156 | 10.987 | 12.596 | 12.561 | 12.088 | 10.912 | 12.537 | 12.613 | 12.122 | 10.959 | 12.584 | 12.599 | 12.112 | 10.945 | 12.566 |
| 13 | 11 | 21.148 | 25.814 | 18.393 | 24.979 | 21.080 | 25.745 | 18.332 | 24.912 | 21.123 | 25.789 | 18.371 | 24.953 | 21.110 | 25.774 | 18.358 | 24.937 |
| 14 | 33 | 6.818 | 6.515 | 5.910 | 6.710 | 6.793 | 6.496 | 5.888 | 6.694 | 6.808 | 6.506 | 5.902 | 6.709 | 6.806 | 6.503 | 5.899 | 6.704 |
| 15 | 33 | 10.431 | 9.836 | 9.049 | 10.224 | 10.354 | 9.766 | 8.979 | 10.167 | 10.402 | 9.796 | 9.024 | 10.212 | 10.389 | 9.788 | 9.011 | 10.196 |
| 16 | 33 | 8.457 | 8.188 | 7.334 | 8.404 | 8.415 | 8.153 | 7.297 | 8.375 | 8.441 | 8.171 | 7.320 | 8.400 | 8.434 | 8.166 | 7.314 | 8.391 |
| 17 | 33 | 10.705 | 10.272 | 9.287 | 10.599 | 10.626 | 10.206 | 9.216 | 10.543 | 10.675 | 10.238 | 9.261 | 10.589 | 10.662 | 10.228 | 9.248 | 10.572 |
| 18 | 33 | 7.114 | 6.729 | 6.166 | 6.952 | 7.083 | 6.701 | 6.138 | 6.930 | 7.102 | 6.713 | 6.156 | 6.949 | 7.098 | 6.710 | 6.151 | 6.943 |
| 19 | 33 | 7.409 | 6.947 | 6.422 | 7.209 | 7.375 | 6.919 | 6.392 | 7.173 | 7.396 | 6.932 | 6.411 | 7.193 | 7.392 | 6.929 | 6.406 | 7.187 |
| 20 | 33 | 7.748 | 7.343 | 6.716 | 7.582 | 7.709 | 7.310 | 6.681 | 7.556 | 7.733 | 7.325 | 6.703 | 7.579 | 7.727 | 7.321 | 6.698 | 7.571 |
| 21 | 33 | 12.054 | 11.428 | 10.460 | 11.837 | 11.906 | 11.292 | 10.327 | 11.728 | 11.997 | 11.350 | 10.411 | 11.813 | 11.973 | 11.333 | 10.387 | 11.781 |
| 22 | 33 | 11.824 | 11.271 | 10.260 | 11.651 | 11.664 | 11.119 | 10.116 | 11.531 | 11.763 | 11.183 | 10.208 | 11.623 | 11.737 | 11.164 | 10.181 | 11.588 |
| 23 | 33 | 7.085 | 6.793 | 6.142 | 6.966 | 7.011 | 6.715 | 6.075 | 6.908 | 7.056 | 6.745 | 6.118 | 6.951 | 7.045 | 6.736 | 6.106 | 6.935 |
| 24 | 33 | 9.012 | 8.620 | 7.820 | 8.844 | 8.759 | 8.335 | 7.591 | 8.608 | 8.914 | 8.435 | 7.735 | 8.749 | 8.870 | 8.403 | 7.690 | 8.693 |
| 25 | 33 | 6.320 | 6.377 | 5.504 | 6.371 | 5.714 | 5.604 | 4.951 | 5.749 | 6.075 | 5.848 | 5.289 | 6.065 | 5.949 | 5.758 | 5.164 | 5.920 |
| 26 | 33 | 2.649 | 2.568 | 2.298 | 2.649 | 2.552 | 2.447 | 2.210 | 2.517 | 2.611 | 2.486 | 2.266 | 2.566 | 2.595 | 2.474 | 2.249 | 2.557 |
| 27 | 33 | 8.031 | 8.591 | 7.056 | 8.342 | 6.392 | 6.342 | 5.540 | 6.591 | 7.321 | 6.966 | 6.415 | 7.376 | 6.932 | 6.696 | 6.034 | 6.959 |
| 28 | 132 | 4.610 | 4.420 | 4.012 | 4.572 | 4.477 | 4.333 | 3.889 | 4.441 | 4.559 | 4.387 | 3.966 | 4.524 | 4.520 | 4.361 | 3.929 | 4.492 |
| 29 | 33 | 4.634 | 4.912 | 4.095 | 4.836 | 3.432 | 3.224 | 2.973 | 3.411 | 4.094 | 3.615 | 3.598 | 3.949 | 3.792 | 3.437 | 3.304 | 3.651 |
| 30 | 33 | 8.381 | 11.033 | 7.870 | 10.043 | 3.716 | 3.255 | 3.219 | 3.658 | 5.768 | 4.179 | 5.209 | 5.452 | 4.593 | 3.688 | 4.040 | 4.399 |

Table D6: ANSI Simulated Results for Case 5 at $\mathbf{3 0 \%}$ penetration level and DG located at Bus 7 and 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.794 | 12.021 | 8.642 | 11.357 | 9.698 | 11.890 | 8.551 | 11.236 | 9.739 | 11.934 | 8.590 | 11.273 | 9.729 | 11.922 | 8.879 | 11.267 |
| 2 | 132 | 8.694 | 9.692 | 7.621 | 9.341 | 8.529 | 9.445 | 7.463 | 9.122 | 8.601 | 9.508 | 7.531 | 9.186 | 8.581 | 9.488 | 7.510 | 9.173 |
| 3 | 132 | 5.365 | 5.444 | 4.675 | 5.454 | 5.257 | 5.287 | 4.572 | 5.320 | 5.303 | 5.320 | 4.616 | 5.361 | 5.291 | 5.310 | 4.603 | 5.353 |
| 4 | 132 | 6.928 | 6.915 | 6.050 | 7.019 | 6.707 | 6.591 | 5.839 | 6.746 | 6.802 | 6.657 | 5.928 | 6.832 | 6.774 | 6.637 | 5.900 | 6.813 |
| 5 | 132 | 5.869 | 5.913 | 5.131 | 5.941 | 5.671 | 5.563 | 4.938 | 5.665 | 5.760 | 5.626 | 5.024 | 5.744 | 5.728 | 5.602 | 4.990 | 5.721 |
| 6 | 132 | 7.992 | 8.018 | 7.004 | 8.112 | 7.562 | 7.368 | 6.588 | 7.572 | 7.747 | 7.493 | 6.763 | 7.744 | 7.687 | 7.451 | 6.702 | 7.701 |
| 7 | 132 | 5.609 | 5.939 | 4.952 | 5.795 | 4.982 | 4.773 | 4.327 | 4.914 | 5.264 | 4.961 | 4.599 | 5.184 | 5.139 | 4.876 | 4.473 | 5.082 |
| 8 | 132 | 5.894 | 6.043 | 5.153 | 6.012 | 5.696 | 5.752 | 4.963 | 5.764 | 5.780 | 5.814 | 5.042 | 5.841 | 5.755 | 5.795 | 5.018 | 5.825 |
| 9 | 33 | 13.160 | 13.372 | 11.454 | 13.434 | 12.957 | 13.204 | 11.263 | 13.280 | 13.043 | 13.267 | 11.343 | 13.349 | 13.022 | 13.251 | 11.322 | 13.325 |
| 10 | 33 | 14.850 | 14.336 | 12.909 | 14.819 | 14.597 | 14.126 | 12.673 | 14.629 | 14.701 | 14.195 | 12.769 | 14.717 | 14.686 | 14.183 | 12.753 | 14.697 |
| 11 | 11 | 19.263 | 23.071 | 16.793 | 21.960 | 19.159 | 22.964 | 16.696 | 21.876 | 19.204 | 23.009 | 16.737 | 21.912 | 19.192 | 22.996 | 16.725 | 21.899 |
| 12 | 33 | 12.696 | 12.192 | 11.038 | 12.638 | 12.562 | 12.089 | 10.912 | 12.537 | 12.618 | 12.125 | 10.964 | 12.585 | 12.609 | 12.118 | 10.954 | 12.573 |
| 13 | 11 | 21.188 | 25.859 | 18.432 | 25.009 | 21.081 | 25.745 | 18.332 | 24.913 | 21.126 | 25.792 | 18.374 | 24.953 | 21.117 | 25.782 | 18.365 | 24.942 |
| 14 | 33 | 6.831 | 6.525 | 5.923 | 6.722 | 6.794 | 6.496 | 5.889 | 6.694 | 6.809 | 6.506 | 5.903 | 6.708 | 6.808 | 6.505 | 5.902 | 6.706 |
| 15 | 33 | 10.459 | 9.856 | 9.077 | 10.248 | 10.353 | 9.766 | 8.979 | 10.166 | 10.396 | 9.793 | 9.018 | 10.204 | 10.393 | 9.790 | 9.015 | 10.197 |
| 16 | 33 | 8.480 | 8.205 | 7.357 | 8.423 | 8.415 | 8.154 | 7.297 | 8.375 | 8.442 | 8.171 | 7.322 | 8.399 | 8.439 | 8.169 | 7.318 | 8.394 |
| 17 | 33 | 10.743 | 10.300 | 9.326 | 10.630 | 10.627 | 10.206 | 9.217 | 10.543 | 10.675 | 10.238 | 9.261 | 10.585 | 10.669 | 10.233 | 9.255 | 10.576 |
| 18 | 33 | 7.128 | 6.738 | 6.180 | 6.964 | 7.083 | 6.701 | 6.138 | 6.930 | 7.101 | 6.713 | 6.155 | 6.946 | 7.100 | 6.712 | 6.153 | 6.944 |
| 19 | 33 | 7.424 | 6.958 | 6.437 | 7.224 | 7.376 | 6.919 | 6.392 | 7.173 | 7.395 | 6.931 | 6.410 | 7.191 | 7.394 | 6.930 | 6.409 | 7.188 |
| 20 | 33 | 7.765 | 7.356 | 6.734 | 7.597 | 7.709 | 7.310 | 6.682 | 7.555 | 7.732 | 7.325 | 6.703 | 7.576 | 7.730 | 7.323 | 6.701 | 7.573 |
| 21 | 33 | 12.095 | 11.459 | 10.503 | 11.870 | 11.906 | 11.292 | 10.327 | 11.724 | 11.982 | 11.340 | 10.396 | 11.791 | 11.976 | 11.335 | 10.390 | 11.780 |
| 22 | 33 | 11.861 | 11.299 | 10.299 | 11.681 | 11.664 | 11.119 | 10.116 | 11.527 | 11.742 | 11.169 | 10.188 | 11.596 | 11.737 | 11.165 | 10.182 | 11.586 |
| 23 | 33 | 7.092 | 6.800 | 6.151 | 6.973 | 7.010 | 6.714 | 6.074 | 6.905 | 7.041 | 6.735 | 6.104 | 6.934 | 7.042 | 6.734 | 6.103 | 6.931 |
| 24 | 33 | 9.004 | 8.618 | 7.819 | 8.843 | 8.753 | 8.331 | 7.586 | 8.594 | 8.847 | 8.390 | 7.672 | 8.677 | 8.850 | 8.392 | 7.674 | 8.672 |
| 25 | 33 | 6.228 | 6.313 | 5.434 | 6.298 | 5.688 | 5.586 | 4.928 | 5.706 | 5.876 | 5.712 | 5.100 | 8.564 | 5.880 | 5.715 | 5.105 | 5.852 |
| 26 | 33 | 2.638 | 2.561 | 2.290 | 2.640 | 2.550 | 2.446 | 2.208 | 2.519 | 2.582 | 2.466 | 2.238 | 2.545 | 2.585 | 2.468 | 2.240 | 2.551 |
| 27 | 33 | 7.691 | 8.309 | 6.783 | 8.031 | 6.307 | 6.282 | 5.466 | 6.469 | 6.753 | 6.583 | 5.784 | 6.829 | 6.737 | 6.574 | 5.866 | 6.775 |
| 28 | 132 | 4.673 | 4.576 | 4.078 | 4.674 | 4.465 | 4.326 | 3.880 | 4.432 | 4.549 | 4.382 | 3.958 | 4.511 | 4.527 | 4.367 | 3.937 | 4.499 |
| 29 | 33 | 5.802 | 7.248 | 5.337 | 6.747 | 3.467 | 3.245 | 3.003 | 3.451 | 4.080 | 3.596 | 3.565 | 3.910 | 4.001 | 3.563 | 3.508 | 3.879 |
| 30 | 33 | 4.200 | 4.299 | 3.711 | 4.340 | 3.376 | 3.068 | 2.924 | 3.247 | 3.637 | 3.215 | 3.162 | 3.491 | 3.624 | 3.211 | 3.155 | 3.506 |

Table D7: ANSI Simulated Results for Case 6 at $\mathbf{3 0 \%}$ penetration level and DG located at Bus 26 and 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.736 | 11.929 | 8.585 | 11.272 | 9.698 | 11.891 | 8.551 | 11.239 | 9.720 | 11.913 | 8.572 | 11.259 | 9.730 | 11.922 | 8.579 | 11.267 |
| 2 | 132 | 8.587 | 9.493 | 7.515 | 9.177 | 8.529 | 9.445 | 7.463 | 9.126 | 8.563 | 9.474 | 7.494 | 9.156 | 8.578 | 9.484 | 7.506 | 9.169 |
| 3 | 132 | 5.309 | 5.323 | 4.619 | 5.367 | 5.257 | 5.287 | 4.573 | 5.322 | 5.288 | 5.308 | 4.600 | 5.349 | 5.301 | 5.316 | 4.611 | 5.360 |
| 4 | 132 | 6.814 | 6.663 | 5.936 | 6.845 | 6.707 | 6.591 | 5.838 | 6.749 | 6.770 | 6.634 | 5.896 | 6.807 | 6.797 | 6.650 | 5.918 | 6.830 |
| 5 | 132 | 5.687 | 5.574 | 4.953 | 5.687 | 5.667 | 5.561 | 4.935 | 5.669 | 5.679 | 5.569 | 4.946 | 5.680 | 5.684 | 5.572 | 4.950 | 5.684 |
| 6 | 132 | 7.749 | 7.492 | 6.760 | 7.755 | 7.560 | 7.366 | 6.585 | 7.577 | 7.671 | 7.441 | 6.689 | 7.683 | 7.720 | 7.469 | 6.728 | 7.725 |
| 7 | 132 | 4.994 | 4.782 | 4.339 | 4.950 | 4.950 | 4.754 | 4.299 | 4.911 | 4.976 | 4.771 | 4.323 | 4.935 | 4.987 | 4.777 | 4.332 | 4.944 |
| 8 | 132 | 5.797 | 5.824 | 5.056 | 5.860 | 5.696 | 5.753 | 4.963 | 5.767 | 5.755 | 5.795 | 5.018 | 5.823 | 5.782 | 5.811 | 5.039 | 5.845 |
| 9 | 33 | 13.149 | 13.393 | 11.438 | 13.440 | 12.957 | 13.205 | 11.263 | 13.284 | 13.070 | 13.287 | 11.368 | 13.380 | 13.120 | 13.318 | 11.407 | 13.421 |
| 10 | 33 | 14.926 | 14.470 | 12.973 | 14.905 | 14.595 | 14.125 | 12.671 | 14.640 | 14.788 | 14.255 | 12.852 | 14.817 | 14.875 | 14.302 | 12.919 | 14.891 |
| 11 | 11 | 19.259 | 23.063 | 16.787 | 21.966 | 19.159 | 22.964 | 16.696 | 21.878 | 19.218 | 23.024 | 16.751 | 21.929 | 19.244 | 23.046 | 16.771 | 21.952 |
| 12 | 33 | 12.708 | 12.232 | 11.045 | 12.652 | 12.559 | 12.087 | 10.910 | 12.539 | 12.647 | 12.145 | 10.991 | 12.620 | 12.685 | 12.166 | 11.021 | 12.653 |
| 13 | 11 | 21.201 | 25.869 | 18.441 | 25.033 | 21.080 | 25.744 | 18.331 | 24.915 | 21.151 | 25.820 | 18.398 | 24.984 | 21.182 | 25.847 | 18.422 | 25.014 |
| 14 | 33 | 6.838 | 6.540 | 5.928 | 6.726 | 6.791 | 6.495 | 5.887 | 6.694 | 6.818 | 6.512 | 5.912 | 6.721 | 6.830 | 6.519 | 5.921 | 6.732 |
| 15 | 33 | 10.503 | 9.928 | 9.115 | 10.293 | 10.354 | 9.766 | 8.979 | 10.172 | 10.441 | 9.822 | 9.061 | 10.253 | 10.480 | 9.842 | 9.091 | 10.286 |
| 16 | 33 | 8.489 | 8.229 | 7.364 | 8.432 | 8.413 | 8.153 | 7.295 | 8.376 | 8.458 | 8.182 | 7.337 | 8.418 | 8.477 | 8.193 | 7.352 | 8.436 |
| 17 | 33 | 10.771 | 10.354 | 9.347 | 10.658 | 10.624 | 10.205 | 9.214 | 10.546 | 10.710 | 10.261 | 9.294 | 10.627 | 10.748 | 10.282 | 9.324 | 10.660 |
| 18 | 33 | 7.142 | 6.766 | 6.192 | 6.976 | 7.081 | 6.700 | 6.137 | 6.931 | 7.117 | 6.723 | 6.170 | 6.965 | 7.133 | 6.731 | 6.182 | 6.979 |
| 19 | 33 | 7.438 | 6.985 | 6.448 | 7.250 | 7.374 | 6.918 | 6.390 | 7.174 | 7.411 | 6.941 | 6.425 | 7.210 | 7.428 | 6.950 | 6.438 | 7.225 |
| 20 | 33 | 7.781 | 7.386 | 6.746 | 7.611 | 7.707 | 7.309 | 6.680 | 7.557 | 7.750 | 7.337 | 6.720 | 7.598 | 7.769 | 7.347 | 6.735 | 7.615 |
| 21 | 33 | 12.203 | 11.617 | 10.597 | 11.981 | 11.907 | 11.292 | 10.327 | 11.738 | 12.079 | 11.403 | 10.489 | 11.897 | 12.157 | 11.444 | 10.549 | 11.963 |
| 22 | 33 | 11.991 | 11.483 | 10.415 | 11.815 | 11.666 | 11.121 | 10.118 | 11.544 | 11.855 | 11.244 | 10.295 | 11.718 | 11.940 | 11.289 | 10.361 | 11.790 |
| 23 | 33 | 7.173 | 6.910 | 6.224 | 7.057 | 7.014 | 6.717 | 6.079 | 6.917 | 7.107 | 6.778 | 6.165 | 7.000 | 7.149 | 6.800 | 6.198 | 7.035 |
| 24 | 33 | 9.373 | 9.084 | 8.154 | 9.278 | 8.785 | 8.351 | 7.614 | 8.651 | 9.122 | 8.567 | 7.930 | 8.944 | 9.278 | 8.649 | 8.053 | 9.071 |
| 25 | 33 | 7.549 | 8.097 | 6.671 | 7.905 | 5.823 | 5.676 | 5.046 | 5.896 | 6.734 | 6.269 | 5.911 | 6.647 | 7.227 | 6.520 | 6.309 | 7.034 |
| 26 | 33 | 5.072 | 6.486 | 4.702 | 6.020 | 2.773 | 2.581 | 2.402 | 2.757 | 3.817 | 3.159 | 3.412 | 3.690 | 4.541 | 3.448 | 4.028 | 4.377 |
| 27 | 33 | 8.076 | 8.809 | 7.130 | 8.469 | 6.334 | 6.302 | 5.490 | 6.525 | 7.253 | 6.930 | 6.363 | 7.313 | 7.751 | 7.196 | 6.764 | 7.714 |
| 28 | 132 | 4.629 | 4.434 | 4.031 | 4.591 | 4.471 | 4.329 | 3.884 | 4.436 | 4.563 | 4.391 | 3.971 | 4.528 | 4.605 | 4.415 | 4.004 | 4.565 |
| 29 | 33 | 4.262 | 4.542 | 3.767 | 4.452 | 3.352 | 3.175 | 2.904 | 3.315 | 3.826 | 3.469 | 3.354 | 3.709 | 4.089 | 3.597 | 3.568 | 3.913 |
| 30 | 33 | 5.937 | 7.355 | 5.458 | 6.839 | 3.490 | 3.131 | 3.023 | 3.394 | 4.606 | 3.714 | 4.102 | 4.385 | 5.375 | 4.004 | 4.752 | 5.090 |

Table D8: ANSI Simulated Results for Case 1 at 42\% penetration level and DG located at Bus 7

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.872 | 12.130 | 8.716 | 11.458 | 9.705 | 11.899 | 8.559 | 11.221 | 9.784 | 11.982 | 8.634 | 11.308 | 9.837 | 12.029 | 8.676 | 11.355 |
| 2 | 132 | 8.845 | 9.920 | 7.764 | 9.548 | 8.558 | 9.469 | 7.491 | 9.108 | 8.688 | 9.584 | 7.615 | 9.254 | 8.782 | 9.654 | 7.692 | 9.335 |
| 3 | 132 | 5.442 | 5.575 | 4.748 | 5.564 | 5.275 | 5.299 | 4.589 | 5.313 | 5.350 | 5.355 | 4.661 | 5.398 | 5.406 | 5.389 | 4.706 | 5.445 |
| 4 | 132 | 7.089 | 7.198 | 6.203 | 7.248 | 6.754 | 6.621 | 5.881 | 6.743 | 6.900 | 6.725 | 6.023 | 6.912 | 7.014 | 6.792 | 6.116 | 7.010 |
| 5 | 132 | 6.148 | 6.330 | 5.397 | 6.308 | 5.729 | 5.601 | 4.991 | 5.683 | 5.911 | 5.730 | 5.169 | 5.865 | 6.053 | 5.812 | 5.286 | 5.986 |
| 6 | 132 | 8.337 | 8.646 | 7.337 | 8.611 | 7.672 | 7.435 | 6.685 | 7.580 | 7.950 | 7.632 | 6.961 | 7.916 | 8.184 | 7.764 | 7.153 | 8.120 |
| 7 | 132 | 6.809 | 8.113 | 6.157 | 7.633 | 5.277 | 4.956 | 4.585 | 5.287 | 5.850 | 5.327 | 5.170 | 5.702 | 6.417 | 5.612 | 5.649 | 6.222 |
| 8 | 132 | 6.016 | 6.278 | 5.270 | 6.198 | 5.734 | 5.779 | 4.998 | 5.760 | 5.857 | 5.871 | 5.118 | 5.903 | 5.953 | 5.930 | 5.196 | 5.986 |
| 9 | 33 | 13.219 | 13.399 | 11.511 | 13.481 | 13.016 | 13.246 | 11.315 | 13.354 | 13.098 | 13.309 | 11.395 | 13.391 | 13.173 | 13.356 | 11.456 | 13.446 |
| 10 | 33 | 14.854 | 14.298 | 12.915 | 14.826 | 14.655 | 14.164 | 12.724 | 14.697 | 14.737 | 14.219 | 12.804 | 14.737 | 14.809 | 14.260 | 12.862 | 14.790 |
| 11 | 11 | 19.292 | 23.101 | 16.821 | 21.979 | 19.192 | 22.996 | 16.725 | 21.918 | 19.231 | 23.038 | 16.764 | 21.934 | 19.269 | 23.071 | 16.794 | 21.963 |
| 12 | 33 | 12.719 | 12.193 | 11.061 | 12.663 | 12.592 | 12.108 | 10.939 | 12.576 | 12.647 | 12.145 | 10.992 | 12.606 | 12.691 | 12.170 | 11.028 | 12.639 |
| 13 | 11 | 21.204 | 25.877 | 18.448 | 25.016 | 21.109 | 25.774 | 18.357 | 24.949 | 21.148 | 25.816 | 18.395 | 24.970 | 21.183 | 25.848 | 18.423 | 24.999 |
| 14 | 33 | 6.835 | 6.523 | 5.928 | 6.730 | 6.798 | 6.499 | 5.893 | 6.701 | 6.815 | 6.510 | 5.909 | 6.713 | 6.827 | 6.517 | 5.919 | 6.723 |
| 15 | 33 | 10.450 | 9.828 | 9.070 | 10.246 | 10.367 | 9.774 | 8.991 | 10.184 | 10.405 | 9.799 | 9.027 | 10.208 | 10.432 | 9.814 | 9.050 | 10.230 |
| 16 | 33 | 8.488 | 8.202 | 7.365 | 8.434 | 8.427 | 8.162 | 7.308 | 8.392 | 8.454 | 8.180 | 7.333 | 8.407 | 8.475 | 8.192 | 7.350 | 8.423 |
| 17 | 33 | 10.751 | 10.288 | 9.334 | 10.642 | 10.650 | 10.221 | 9.238 | 10.573 | 10.694 | 10.251 | 9.280 | 10.597 | 10.729 | 10.270 | 9.308 | 10.624 |
| 18 | 33 | 7.127 | 6.730 | 6.180 | 6.968 | 7.088 | 6.705 | 6.143 | 6.938 | 7.106 | 6.716 | 6.160 | 6.950 | 7.119 | 6.723 | 6.171 | 6.960 |
| 19 | 33 | 7.425 | 6.950 | 6.439 | 7.215 | 7.383 | 6.923 | 6.398 | 7.183 | 7.402 | 6.936 | 6.417 | 7.195 | 7.416 | 6.943 | 6.428 | 7.206 |
| 20 | 33 | 7.767 | 7.348 | 6.736 | 7.603 | 7.718 | 7.316 | 6.689 | 7.567 | 7.740 | 7.330 | 6.711 | 7.581 | 7.757 | 7.339 | 6.724 | 7.594 |
| 21 | 33 | 12.062 | 11.392 | 10.473 | 11.846 | 11.935 | 11.310 | 10.353 | 11.758 | 11.990 | 11.346 | 10.406 | 11.789 | 12.034 | 11.370 | 10.441 | 11.822 |
| 22 | 33 | 11.814 | 11.217 | 10.258 | 11.644 | 11.691 | 11.136 | 10.140 | 11.558 | 11.745 | 11.172 | 10.192 | 11.589 | 11.787 | 11.195 | 10.226 | 11.621 |
| 23 | 33 | 7.055 | 6.744 | 6.117 | 6.941 | 7.015 | 6.717 | 6.079 | 6.910 | 7.033 | 6.730 | 6.097 | 6.923 | 7.046 | 6.737 | 6.107 | 6.933 |
| 24 | 33 | 8.828 | 8.380 | 7.657 | 8.645 | 8.761 | 8.336 | 7.593 | 8.594 | 8.792 | 8.356 | 7.623 | 8.615 | 8.814 | 8.369 | 7.640 | 8.632 |
| 25 | 33 | 5.709 | 5.601 | 4.950 | 5.689 | 5.674 | 5.577 | 4.917 | 5.664 | 5.690 | 5.588 | 4.932 | 5.673 | 5.702 | 5.595 | 4.941 | 5.682 |
| 26 | 33 | 2.557 | 2.451 | 2.216 | 2.532 | 2.551 | 2.446 | 2.209 | 2.526 | 2.554 | 2.448 | 2.212 | 2.529 | 2.556 | 2.450 | 2.214 | 2.530 |
| 27 | 33 | 6.276 | 6.260 | 5.444 | 6.359 | 6.230 | 6.227 | 5.400 | 6.329 | 6.249 | 6.241 | 5.419 | 6.338 | 6.266 | 6.251 | 5.432 | 6.351 |
| 28 | 132 | 4.680 | 4.687 | 4.086 | 4.726 | 4.481 | 4.336 | 3.894 | 4.425 | 4.568 | 4.397 | 3.979 | 4.526 | 4.636 | 4.435 | 4.034 | 4.584 |
| 29 | 33 | 3.302 | 3.145 | 2.862 | 3.243 | 3.291 | 3.138 | 2.851 | 3.231 | 3.296 | 3.141 | 2.856 | 3.237 | 3.300 | 3.143 | 2.859 | 3.240 |
| 30 | 33 | 3.326 | 3.042 | 2.882 | 3.251 | 3.316 | 3.036 | 2.872 | 3.241 | 3.321 | 3.039 | 2.877 | 3.246 | 3.324 | 3.041 | 2.880 | 3.249 |

Table D9: ANSI Simulated Results for Case 2 at 42\% penetration level and DG located at Bus 26

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.727 | 11.918 | 8.576 | 11.263 | 9.711 | 11.903 | 8.563 | 11.247 | 9.719 | 11.911 | 8.570 | 11.257 | 9.724 | 11.916 | 8.574 | 11.261 |
| 2 | 132 | 8.572 | 9.480 | 7.501 | 9.163 | 8.550 | 9.462 | 7.481 | 9.140 | 8.561 | 9.471 | 7.491 | 9.154 | 8.568 | 9.476 | 7.497 | 9.160 |
| 3 | 132 | 5.297 | 5.314 | 4.608 | 5.355 | 5.278 | 5.301 | 4.590 | 5.335 | 5.286 | 5.307 | 4.599 | 5.347 | 5.293 | 5.311 | 4.604 | 5.352 |
| 4 | 132 | 6.790 | 6.645 | 5.912 | 6.821 | 6.752 | 6.619 | 5.877 | 6.779 | 6.767 | 6.631 | 5.893 | 6.803 | 6.782 | 6.639 | 5.904 | 6.814 |
| 5 | 132 | 5.682 | 5.570 | 4.948 | 5.682 | 5.674 | 5.565 | 4.941 | 5.674 | 5.678 | 5.568 | 4.944 | 5.679 | 5.680 | 5.569 | 4.946 | 5.681 |
| 6 | 132 | 7.701 | 7.457 | 6.711 | 7.703 | 7.640 | 7.416 | 6.655 | 7.634 | 7.661 | 7.433 | 6.677 | 7.671 | 7.687 | 7.447 | 6.697 | 7.691 |
| 7 | 132 | 4.982 | 4.774 | 4.327 | 4.939 | 4.967 | 4.765 | 4.314 | 4.923 | 4.973 | 4.769 | 4.320 | 4.932 | 4.979 | 4.772 | 4.324 | 4.936 |
| 8 | 132 | 5.769 | 5.803 | 5.028 | 5.831 | 5.737 | 5.780 | 4.998 | 5.795 | 4.748 | 5.789 | 5.011 | 5.815 | 5.762 | 5.797 | 5.021 | 5.825 |
| 9 | 33 | 13.138 | 13.379 | 11.423 | 13.434 | 13.050 | 13.270 | 11.344 | 13.385 | 13.089 | 13.299 | 11.383 | 13.401 | 13.121 | 13.318 | 11.406 | 13.428 |
| 10 | 33 | 14.925 | 14.455 | 12.964 | 14.911 | 14.745 | 14.221 | 12.801 | 14.816 | 14.836 | 14.283 | 12.891 | 14.867 | 14.895 | 14.313 | 12.934 | 14.918 |
| 11 | 11 | 19.254 | 23.056 | 16.780 | 21.965 | 19.211 | 23.013 | 16.741 | 21.935 | 19.228 | 23.033 | 16.759 | 21.941 | 19.245 | 23.046 | 16.771 | 21.956 |
| 12 | 33 | 12.703 | 12.222 | 11.036 | 12.650 | 12.621 | 12.127 | 10.964 | 12.614 | 12.664 | 12.155 | 11.005 | 12.639 | 12.689 | 12.168 | 11.024 | 12.661 |
| 13 | 11 | 21.198 | 25.863 | 18.436 | 25.035 | 21.135 | 25.800 | 18.380 | 24.984 | 21.166 | 25.833 | 18.410 | 25.002 | 21.187 | 25.851 | 18.425 | 25.022 |
| 14 | 33 | 6.835 | 6.537 | 5.925 | 6.725 | 6.806 | 6.503 | 5.899 | 6.714 | 6.824 | 6.515 | 5.916 | 6.727 | 6.831 | 6.519 | 5.922 | 6.734 |
| 15 | 33 | 10.506 | 9.923 | 9.114 | 10.296 | 10.421 | 9.807 | 9.038 | 10.252 | 10.465 | 9.835 | 9.081 | 10.278 | 10.492 | 9.849 | 9.100 | 10.300 |
| 16 | 33 | 8.486 | 8.224 | 7.360 | 8.432 | 8.443 | 8.171 | 7.321 | 8.414 | 8.467 | 8.188 | 7.344 | 8.429 | 8.480 | 8.194 | 7.353 | 8.440 |
| 17 | 33 | 10.768 | 10.346 | 9.341 | 10.658 | 10.684 | 10.242 | 9.266 | 10.620 | 10.729 | 10.272 | 9.310 | 10.648 | 10.754 | 10.285 | 9.328 | 10.670 |
| 18 | 33 | 7.141 | 6.763 | 6.190 | 6.977 | 7.105 | 6.714 | 6.157 | 6.961 | 7.125 | 6.728 | 6.177 | 6.975 | 7.136 | 6.733 | 6.185 | 6.984 |
| 19 | 33 | 7.437 | 6.982 | 6.446 | 7.245 | 7.398 | 6.932 | 6.411 | 7.205 | 7.420 | 6.946 | 6.432 | 7.220 | 7.431 | 6.952 | 6.440 | 7.229 |
| 20 | 33 | 7.779 | 7.382 | 6.743 | 7.611 | 7.735 | 7.326 | 6.704 | 7.593 | 7.760 | 7.342 | 6.728 | 7.609 | 7.773 | 7.349 | 6.737 | 7.620 |
| 21 | 33 | 12.214 | 11.609 | 10.599 | 11.994 | 12.045 | 11.377 | 10.448 | 11.901 | 12.131 | 11.433 | 10.532 | 11.950 | 12.185 | 11.460 | 10.571 | 11.996 |
| 22 | 33 | 12.007 | 11.478 | 10.420 | 11.833 | 11.823 | 11.217 | 10.254 | 11.726 | 11.915 | 11.278 | 10.345 | 11.778 | 11.975 | 11.309 | 10.389 | 11.829 |
| 23 | 33 | 7.188 | 6.912 | 6.233 | 7.071 | 7.100 | 6.770 | 6.153 | 7.013 | 7.142 | 6.798 | 6.195 | 7.034 | 7.172 | 6.814 | 6.217 | 7.059 |
| 24 | 33 | 9.461 | 9.110 | 8.217 | 9.322 | 9.142 | 8.565 | 7.923 | 9.031 | 9.275 | 8.655 | 8.061 | 9.085 | 9.396 | 8.715 | 8.151 | 9.183 |
| 25 | 33 | 8.046 | 8.343 | 7.058 | 8.241 | 6.991 | 6.392 | 6.057 | 7.099 | 7.323 | 6.595 | 6.429 | 7.165 | 7.778 | 6.802 | 6.778 | 7.523 |
| 26 | 33 | 9.952 | 13.985 | 9.555 | 12.572 | 5.099 | 3.731 | 4.416 | 5.190 | 6.196 | 4.024 | 5.701 | 5.956 | 8.267 | 4.470 | 7.446 | 7.835 |
| 27 | 33 | 7.192 | 7.322 | 6.259 | 7.310 | 6.752 | 6.577 | 5.852 | 6.935 | 6.925 | 6.699 | 6.035 | 6.998 | 7.097 | 6.790 | 6.163 | 7.140 |
| 28 | 132 | 4.574 | 4.395 | 3.977 | 4.533 | 4.532 | 4.367 | 3.938 | 4.482 | 4.544 | 4.377 | 3.951 | 4.507 | 4.563 | 4.387 | 3.966 | 4.523 |
| 29 | 33 | 3.475 | 3.344 | 3.015 | 3.443 | 3.378 | 3.190 | 2.927 | 3.321 | 3.425 | 3.222 | 2.973 | 3.345 | 3.458 | 3.238 | 2.997 | 3.373 |
| 30 | 33 | 3.474 | 3.211 | 3.013 | 3.423 | 3.389 | 3.075 | 2.936 | 3.269 | 3.431 | 3.102 | 2.978 | 3.321 | 3.459 | 3.115 | 2.998 | 3.340 |

Table D10: ANSI Simulated Results for Case 3 at 42\% penetration level and DG located at Bus 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.738 | 11.930 | 8.586 | 11.274 | 9.716 | 11.908 | 8.567 | 11.250 | 9.726 | 11.919 | 8.577 | 11.264 | 9.734 | 11.925 | 8.582 | 11.270 |
| 2 | 132 | 8.590 | 9.495 | 7.517 | 9.179 | 8.559 | 9.469 | 7.489 | 9.145 | 8.572 | 9.481 | 7.502 | 9.164 | 8.584 | 9.489 | 7.511 | 9.174 |
| 3 | 132 | 5.311 | 5.324 | 4.620 | 5.368 | 5.285 | 5.305 | 4.596 | 5.339 | 5.295 | 5.131 | 4.607 | 5.355 | 5.305 | 5.319 | 4.614 | 5.363 |
| 4 | 132 | 6.818 | 6.664 | 5.937 | 6.848 | 6.768 | 6.629 | 5.891 | 6.789 | 6.785 | 6.643 | 5.909 | 6.820 | 6.806 | 6.655 | 5.925 | 6.837 |
| 5 | 132 | 5.689 | 5.575 | 4.954 | 5.688 | 5.677 | 5.567 | 4.943 | 5.675 | 5.682 | 5.571 | 4.948 | 5.682 | 5.686 | 5.573 | 4.952 | 5.686 |
| 6 | 132 | 7.767 | 7.501 | 6.772 | 7.768 | 7.682 | 7.442 | 6.692 | 7.661 | 7.706 | 7.463 | 6.719 | 7.713 | 7.745 | 7.484 | 6.749 | 7.747 |
| 7 | 132 | 4.997 | 4.784 | 4.341 | 4.953 | 4.976 | 4.770 | 4.321 | 4.928 | 4.983 | 4.776 | 4.329 | 4.941 | 4.992 | 4.780 | 4.336 | 4.948 |
| 8 | 132 | 5.809 | 5.831 | 5.065 | 5.870 | 5.762 | 5.797 | 5.021 | 5.812 | 5.776 | 5.809 | 5.036 | 5.840 | 5.797 | 5.821 | 5.052 | 5.858 |
| 9 | 33 | 13.114 | 13.334 | 11.403 | 13.402 | 13.034 | 13.258 | 11.330 | 13.365 | 13.066 | 13.283 | 11.362 | 13.374 | 13.097 | 13.301 | 11.385 | 13.398 |
| 10 | 33 | 14.832 | 14.323 | 12.883 | 14.812 | 14.690 | 14.185 | 12.753 | 14.746 | 14.759 | 14.233 | 12.821 | 14.783 | 14.806 | 14.258 | 12.856 | 14.822 |
| 11 | 11 | 12.240 | 23.043 | 16.768 | 21.948 | 19.201 | 23.004 | 16.733 | 21.923 | 19.216 | 23.020 | 16.747 | 21.926 | 19.232 | 23.033 | 16.759 | 21.940 |
| 12 | 33 | 12.673 | 12.175 | 11.011 | 12.621 | 12.604 | 12.116 | 10.949 | 12.590 | 12.638 | 12.138 | 10.982 | 12.609 | 12.661 | 12.150 | 10.999 | 12.628 |
| 13 | 11 | 21.171 | 25.837 | 18.413 | 25.002 | 21.119 | 25.784 | 18.366 | 24.962 | 21.144 | 25.810 | 18.390 | 24.975 | 21.162 | 25.826 | 18.403 | 24.992 |
| 14 | 33 | 6.825 | 6.520 | 5.917 | 6.717 | 6.801 | 6.500 | 5.895 | 6.706 | 6.815 | 6.510 | 5.908 | 6.716 | 6.822 | 6.513 | 5.913 | 6.722 |
| 15 | 33 | 10.456 | 9.854 | 9.071 | 10.247 | 10.389 | 9.788 | 9.010 | 10.214 | 10.424 | 9.810 | 9.044 | 10.235 | 10.445 | 9.821 | 9.059 | 10.253 |
| 16 | 33 | 8.470 | 8.197 | 7.346 | 8.416 | 8.434 | 8.165 | 7.313 | 8.401 | 8.453 | 8.178 | 7.331 | 8.412 | 8.464 | 8.184 | 7.339 | 8.421 |
| 17 | 33 | 10.731 | 10.291 | 9.309 | 10.621 | 10.663 | 10.229 | 9.248 | 10.592 | 10.698 | 10.253 | 9.282 | 10.613 | 10.719 | 10.264 | 9.298 | 10.630 |
| 18 | 33 | 7.124 | 6.736 | 6.175 | 6.961 | 7.095 | 6.708 | 6.148 | 6.948 | 7.111 | 6.719 | 6.164 | 6.959 | 7.120 | 6.723 | 6.170 | 6.966 |
| 19 | 33 | 7.420 | 6.955 | 6.431 | 7.219 | 7.388 | 6.926 | 6.403 | 7.192 | 7.406 | 6.937 | 6.419 | 7.203 | 7.415 | 6.942 | 6.426 | 7.211 |
| 20 | 33 | 7.760 | 7.352 | 6.727 | 7.593 | 7.724 | 7.319 | 6.695 | 7.578 | 7.744 | 7.332 | 6.713 | 7.590 | 7.754 | 7.337 | 6.721 | 7.599 |
| 21 | 33 | 12.103 | 11.465 | 10.502 | 11.881 | 11.976 | 11.335 | 10.388 | 11.819 | 12.042 | 11.377 | 10.451 | 11.857 | 12.081 | 11.398 | 10.480 | 11.890 |
| 22 | 33 | 11.876 | 11.311 | 10.305 | 11.698 | 11.740 | 11.166 | 10.182 | 11.629 | 11.810 | 11.213 | 10.250 | 11.671 | 11.853 | 11.234 | 10.282 | 11.707 |
| 23 | 33 | 7.109 | 6.813 | 6.163 | 6.988 | 7.045 | 6.736 | 6.105 | 6.953 | 7.078 | 6.758 | 6.137 | 6.973 | 7.098 | 6.769 | 6.152 | 6.990 |
| 24 | 33 | 9.099 | 8.693 | 7.895 | 8.926 | 8.889 | 8.414 | 7.704 | 8.769 | 8.992 | 8.483 | 7.805 | 8.826 | 9.061 | 8.518 | 7.857 | 8.883 |
| 25 | 33 | 6.560 | 6.604 | 5.715 | 6.611 | 6.066 | 5.832 | 5.256 | 6.161 | 6.279 | 5.977 | 5.473 | 6.258 | 6.457 | 6.070 | 5.609 | 6.404 |
| 26 | 33 | 2.683 | 2.599 | 2.327 | 2.681 | 2.600 | 2.476 | 2.252 | 2.549 | 2.641 | 2.504 | 2.293 | 2.587 | 2.668 | 2.518 | 2.312 | 2.606 |
| 27 | 33 | 8.850 | 9.458 | 7.791 | 9.173 | 7.413 | 7.021 | 6.425 | 7.749 | 7.937 | 7.341 | 6.982 | 7.944 | 8.502 | 7.612 | 7.419 | 8.395 |
| 28 | 132 | 4.664 | 4.453 | 4.059 | 4.620 | 4.597 | 4.407 | 3.994 | 4.527 | 4.608 | 4.418 | 4.010 | 4.568 | 4.644 | 4.438 | 4.037 | 4.599 |
| 29 | 33 | 10.757 | 14.903 | 10.261 | 13.429 | 5.523 | 4.390 | 4.784 | 5.757 | 6.934 | 4.828 | 6.349 | 6.558 | 9.048 | 5.349 | 8.124 | 8.456 |
| 30 | 33 | 4.964 | 5.042 | 4.382 | 5.128 | 4.083 | 3.441 | 3.537 | 4.014 | 4.383 | 3.597 | 3.862 | 4.122 | 4.741 | 3.732 | 4.140 | 4.410 |

Table D11: ANSI Simulated Results for Case 4 at 42\% penetration level and DG located at Bus 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.732 | 11.924 | 8.581 | 11.269 | 9.713 | 11.905 | 8.564 | 11.247 | 9.722 | 11.914 | 8.573 | 11.260 | 9.728 | 11.920 | 8.578 | 11.266 |
| 2 | 132 | 8.581 | 9.487 | 7.509 | 9.172 | 8.553 | 9.464 | 7.484 | 9.141 | 8.565 | 9.475 | 7.496 | 9.158 | 8.576 | 9.482 | 7.503 | 9.167 |
| 3 | 132 | 5.303 | 5.318 | 4.613 | 5.361 | 5.280 | 5.302 | 4.592 | 5.336 | 5.289 | 5.309 | 4.601 | 5.350 | 5.298 | 5.314 | 4.608 | 5.357 |
| 4 | 132 | 6.801 | 6.653 | 5.922 | 6.833 | 6.756 | 6.622 | 5.881 | 6.781 | 6.773 | 6.635 | 5.898 | 6.809 | 6.791 | 6.645 | 5.912 | 6.824 |
| 5 | 132 | 5.685 | 5.573 | 4.951 | 5.685 | 5.675 | 5.566 | 4.942 | 5.674 | 5.680 | 5.569 | 4.946 | 5.680 | 5.683 | 5.571 | 4.949 | 5.683 |
| 6 | 132 | 7.736 | 7.481 | 6.744 | 7.739 | 7.659 | 7.427 | 6.671 | 7.644 | 7.682 | 7.447 | 6.697 | 7.692 | 7.717 | 7.466 | 6.724 | 7.721 |
| 7 | 132 | 4.990 | 4.780 | 4.335 | 4.947 | 4.971 | 4.767 | 4.317 | 4.924 | 4.978 | 4.772 | 4.325 | 4.936 | 4.986 | 4.777 | 4.330 | 4.943 |
| 8 | 132 | 5.792 | 5.819 | 5.049 | 5.854 | 5.750 | 5.788 | 5.010 | 5.803 | 5.763 | 5.800 | 5.024 | 5.829 | 5.782 | 5.811 | 5.039 | 5.844 |
| 9 | 33 | 13.090 | 13.315 | 11.381 | 13.382 | 13.018 | 13.247 | 11.316 | 13.348 | 13.048 | 13.270 | 11.346 | 13.358 | 13.075 | 13.286 | 11.366 | 13.380 |
| 10 | 33 | 14.796 | 14.295 | 12.850 | 14.781 | 14.669 | 14.172 | 12.735 | 14.723 | 14.733 | 14.216 | 12.798 | 14.758 | 14.774 | 14.237 | 12.828 | 14.793 |
| 11 | 11 | 19.228 | 23.031 | 16.757 | 21.937 | 19.193 | 22.996 | 16.725 | 21.914 | 19.207 | 23.011 | 16.739 | 21.917 | 19.220 | 23.023 | 16.749 | 21.930 |
| 12 | 33 | 12.656 | 12.162 | 10.996 | 12.606 | 12.595 | 12.110 | 10.941 | 12.579 | 12.626 | 12.130 | 10.971 | 12.597 | 12.645 | 12.141 | 10.985 | 12.613 |
| 13 | 11 | 21.158 | 25.823 | 18.401 | 24.989 | 21.111 | 25.775 | 18.358 | 24.952 | 21.133 | 25.800 | 18.380 | 24.965 | 21.149 | 25.813 | 18.392 | 24.980 |
| 14 | 33 | 6.820 | 6.517 | 5.912 | 6.712 | 6.799 | 6.499 | 5.893 | 6.704 | 6.812 | 6.508 | 5.905 | 6.713 | 6.817 | 6.510 | 5.909 | 6.718 |
| 15 | 33 | 10.441 | 9.842 | 9.057 | 10.233 | 10.381 | 9.783 | 9.003 | 10.204 | 10.413 | 9.803 | 9.034 | 10.224 | 10.431 | 9.812 | 9.047 | 10.239 |
| 16 | 33 | 8.462 | 8.191 | 7.338 | 8.409 | 8.429 | 8.163 | 7.309 | 8.395 | 8.447 | 8.174 | 7.326 | 8.406 | 8.456 | 8.180 | 7.333 | 8.414 |
| 17 | 33 | 10.715 | 10.278 | 9.295 | 10.608 | 10.654 | 10.224 | 9.241 | 10.582 | 10.687 | 10.245 | 9.272 | 10.601 | 10.705 | 10.255 | 9.285 | 10.617 |
| 18 | 33 | 7.118 | 6.731 | 6.169 | 6.955 | 7.092 | 6.707 | 6.146 | 6.944 | 7.107 | 6.716 | 6.160 | 6.954 | 7.114 | 6.720 | 6.165 | 6.960 |
| 19 | 33 | 7.413 | 6.950 | 6.425 | 7.212 | 7.385 | 6.924 | 6.400 | 7.188 | 7.401 | 6.935 | 6.415 | 7.199 | 7.409 | 6.938 | 6.421 | 7.205 |
| 20 | 33 | 7.752 | 7.346 | 6.720 | 7.586 | 7.720 | 7.317 | 6.691 | 7.573 | 7.738 | 7.329 | 6.708 | 7.585 | 7.747 | 7.333 | 6.715 | 7.592 |
| 21 | 33 | 12.073 | 11.441 | 10.475 | 11.854 | 11.960 | 11.325 | 10.374 | 11.800 | 12.020 | 11.364 | 10.431 | 11.836 | 12.054 | 11.381 | 10.456 | 11.865 |
| 22 | 33 | 11.844 | 11.284 | 10.276 | 11.669 | 11.722 | 11.155 | 10.167 | 11.609 | 11.787 | 11.198 | 10.229 | 11.648 | 11.823 | 11.217 | 10.256 | 11.679 |
| 23 | 33 | 7.094 | 6.800 | 6.150 | 6.975 | 7.037 | 6.731 | 6.098 | 6.944 | 7.067 | 6.752 | 6.128 | 6.962 | 7.085 | 6.760 | 6.140 | 6.977 |
| 24 | 33 | 9.046 | 8.645 | 7.848 | 8.873 | 8.860 | 8.396 | 7.679 | 8.737 | 8.954 | 8.459 | 7.771 | 8.790 | 9.013 | 8.489 | 7.815 | 8.840 |
| 25 | 33 | 6.417 | 6.458 | 5.585 | 6.459 | 5.990 | 5.784 | 5.190 | 6.077 | 6.180 | 5.914 | 5.383 | 6.168 | 6.331 | 5.993 | 5.497 | 6.292 |
| 26 | 33 | 2.662 | 2.579 | 2.309 | 2.660 | 2.589 | 2.469 | 2.243 | 2.537 | 2.627 | 2.495 | 2.279 | 2.575 | 2.649 | 2.507 | 2.296 | 2.592 |
| 27 | 33 | 8.365 | 8.907 | 7.342 | 8.665 | 7.187 | 6.875 | 6.229 | 7.502 | 7.637 | 7.160 | 6.702 | 7.678 | 8.091 | 7.385 | 7.052 | 8.043 |
| 28 | 132 | 4.635 | 4.435 | 4.033 | 4.592 | 4.574 | 4.393 | 3.974 | 4.509 | 4.586 | 4.404 | 3.990 | 4.547 | 4.617 | 4.421 | 4.014 | 4.574 |
| 29 | 33 | 4.915 | 5.185 | 4.339 | 5.121 | 4.038 | 3.577 | 3.498 | 4.073 | 4.340 | 3.744 | 3.824 | 4.177 | 4.694 | 3.892 | 4.100 | 4.450 |
| 30 | 33 | 10.797 | 14.924 | 10.296 | 13.435 | 5.503 | 4.148 | 4.767 | 5.626 | 6.957 | 4.564 | 6.370 | 6.578 | 9.081 | 5.028 | 8.152 | 8.477 |

Table D12: ANSI Simulated Results for Case 5 at $\mathbf{4 2 \%}$ penetration level and DG located at Bus 7 and 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.826 | 12.067 | 8.673 | 11.398 | 9.706 | 11.900 | 8.560 | 11.230 | 9.762 | 11.959 | 8.613 | 11.291 | 9.800 | 11.993 | 8.643 | 11.326 |
| 2 | 132 | 8.754 | 9.783 | 7.677 | 9.422 | 8.553 | 9.465 | 7.485 | 9.118 | 8.642 | 9.544 | 7.571 | 9.218 | 8.709 | 9.593 | 7.625 | 9.276 |
| 3 | 132 | 5.403 | 5.502 | 4.711 | 5.503 | 5.277 | 5.300 | 4.590 | 5.321 | 5.332 | 5.342 | 4.644 | 5.384 | 5.374 | 5.67 | 4.678 | 5.420 |
| 4 | 132 | 7.007 | 7.039 | 6.125 | 7.120 | 6.756 | 6.622 | 5.882 | 6.756 | 6.863 | 6.699 | 5.987 | 6.883 | 6.950 | 6.750 | 6.057 | 6.957 |
| 5 | 132 | 5.950 | 6.057 | 5.210 | 6.058 | 5.696 | 5.580 | 4.961 | 5.658 | 5.806 | 5.658 | 5.069 | 5.781 | 5.892 | 5.709 | 5.139 | 5.854 |
| 6 | 132 | 8.156 | 8.284 | 7.161 | 8.326 | 7.672 | 7.435 | 6.684 | 7.604 | 7.869 | 7.577 | 6.881 | 7.850 | 8.041 | 7.675 | 7.022 | 8.001 |
| 7 | 132 | 5.914 | 6.564 | 5.261 | 6.312 | 5.114 | 4.854 | 4.442 | 5.054 | 5.423 | 5.065 | 4.756 | 5.325 | 5.715 | 5.224 | 5.003 | 5.593 |
| 8 | 132 | 5.964 | 6.153 | 5.219 | 6.103 | 5.746 | 5.786 | 5.007 | 5.778 | 5.837 | 5.856 | 5.097 | 5.889 | 5.913 | 5.903 | 5.159 | 5.955 |
| 9 | 33 | 13.225 | 13.421 | 11.515 | 13.489 | 13.019 | 13.249 | 11.318 | 13.364 | 13.107 | 13.315 | 11.404 | 13.407 | 13.179 | 13.361 | 11.462 | 13.462 |
| 10 | 33 | 14.922 | 14.386 | 12.975 | 14.880 | 14.657 | 14.166 | 12.726 | 14.721 | 14.780 | 14.249 | 12.845 | 14.795 | 14.867 | 14.298 | 12.913 | 14.863 |
| 11 | 11 | 19.296 | 23.104 | 16.824 | 21.990 | 19.195 | 22.999 | 16.728 | 21.923 | 19.237 | 23.043 | 16.769 | 21.943 | 19.274 | 23.075 | 16.798 | 21.973 |
| 12 | 33 | 12.735 | 12.218 | 11.074 | 12.671 | 12.590 | 12.108 | 10.937 | 12.582 | 12.658 | 12.153 | 11.002 | 12.624 | 12.705 | 12.179 | 11.040 | 12.662 |
| 13 | 11 | 21.219 | 25.892 | 18.461 | 25.040 | 21.109 | 25.774 | 18.357 | 24.955 | 21.159 | 25.828 | 18.405 | 24.987 | 21.196 | 25.862 | 18.435 | 25.020 |
| 14 | 33 | 6.841 | 6.531 | 5.932 | 6.731 | 6.795 | 6.497 | 5.890 | 6.702 | 6.819 | 6.513 | 5.913 | 6.719 | 6.832 | 6.520 | 5.923 | 6.731 |
| 15 | 33 | 10.486 | 9.874 | 9.102 | 10.272 | 10.369 | 9.776 | 8.994 | 10.197 | 10.427 | 9.813 | 9.049 | 10.236 | 10.463 | 9.832 | 9.077 | 10.266 |
| 16 | 33 | 8.498 | 8.217 | 7.373 | 8.439 | 8.426 | 8.161 | 7.306 | 8.395 | 8.461 | 8.184 | 7.340 | 8.418 | 8.483 | 8.197 | 7.357 | 8.436 |
| 17 | 33 | 10.776 | 10.322 | 9.356 | 10.658 | 10.648 | 10.220 | 9.236 | 10.580 | 10.710 | 10.261 | 9.295 | 10.620 | 10.750 | 10.284 | 9.327 | 10.653 |
| 18 | 33 | 7.139 | 6.746 | 6.190 | 6.974 | 7.087 | 6.704 | 6.142 | 6.941 | 7.114 | 6.721 | 6.167 | 6.960 | 7.129 | 6.729 | 6.179 | 6.973 |
| 19 | 33 | 7.437 | 6.966 | 6.448 | 7.234 | 7.381 | 6.922 | 6.397 | 7.186 | 7.409 | 6.940 | 6.424 | 7.206 | 7.426 | 6.949 | 6.437 | 7.219 |
| 20 | 33 | 7.780 | 7.366 | 6.747 | 7.610 | 7.716 | 7.315 | 6.688 | 7.571 | 7.748 | 7.336 | 6.718 | 7.593 | 7.768 | 7.346 | 6.734 | 7.609 |
| 21 | 33 | 12.144 | 11.493 | 10.547 | 11.913 | 11.941 | 11.314 | 10.358 | 11.785 | 12.040 | 11.379 | 10.453 | 11.851 | 12.104 | 11.413 | 10.503 | 11.902 |
| 22 | 33 | 11.911 | 11.335 | 10.345 | 11.725 | 11.700 | 11.142 | 10.148 | 11.590 | 11.804 | 11.211 | 10.248 | 11.659 | 11.869 | 11.246 | 10.299 | 11.713 |
| 23 | 33 | 7.111 | 6.814 | 6.168 | 6.990 | 7.022 | 6.722 | 6.086 | 6.930 | 7.067 | 6.752 | 6.129 | 6.961 | 7.094 | 6.767 | 6.149 | 6.983 |
| 24 | 33 | 9.061 | 8.665 | 7.869 | 8.897 | 8.805 | 8.363 | 7.631 | 8.681 | 8.932 | 8.448 | 7.755 | 8.765 | 9.011 | 8.489 | 7.815 | 8.830 |
| 25 | 33 | 6.362 | 6.443 | 5.552 | 6.437 | 5.842 | 5.689 | 5.062 | 5.922 | 6.078 | 5.853 | 5.297 | 6.062 | 6.250 | 5.946 | 5.430 | 6.202 |
| 26 | 33 | 2.657 | 2.579 | 2.306 | 2.659 | 2.567 | 2.456 | 2.224 | 2.519 | 2.613 | 2.487 | 2.268 | 2.568 | 2.639 | 2.501 | 2.288 | 2.588 |
| 27 | 33 | 8.111 | 8.779 | 7.163 | 8.475 | 6.768 | 6.603 | 5.866 | 7.064 | 7.306 | 6.965 | 6.416 | 7.347 | 7.784 | 7.215 | 6.795 | 7.726 |
| 28 | 132 | 4.743 | 4.667 | 4.143 | 4.754 | 4.543 | 4.374 | 3.948 | 4.469 | 4.619 | 4.429 | 4.025 | 4.575 | 4.694 | 4.471 | 4.086 | 4.640 |
| 29 | 33 | 7.003 | 9.257 | 6.548 | 8.492 | 4.242 | 3.713 | 3.675 | 4.382 | 5.116 | 4.141 | 4.607 | 4.879 | 6.170 | 4.522 | 5.489 | 5.839 |
| 30 | 33 | 4.461 | 4.594 | 3.949 | 4.640 | 3.669 | 3.229 | 3.178 | 3.594 | 3.974 | 3.404 | 3.493 | 3.791 | 4.262 | 3.527 | 3.723 | 4.031 |

Table D13: ANSI Simulated Results for Case 6 at 42\% penetration level and DG located at Bus 26 and 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.742 | 11.935 | 8.591 | 11.277 | 9.712 | 11.904 | 8.563 | 11.245 | 9.727 | 11.920 | 8.578 | 11.264 | 9.736 | 11.928 | 8.585 | 11.272 |
| 2 | 132 | 8.597 | 9.501 | 7.524 | 9.184 | 8.553 | 9.464 | 7.484 | 9.137 | 8.573 | 9.482 | 7.503 | 9.164 | 8.588 | 9.493 | 7.515 | 9.177 |
| 3 | 132 | 5.318 | 5.329 | 4.627 | 5.374 | 5.280 | 5.302 | 4.592 | 5.333 | 5.297 | 5.315 | 4.609 | 5.356 | 5.310 | 5.323 | 4.619 | 5.367 |
| 4 | 132 | 6.834 | 6.675 | 5.953 | 6.861 | 6.759 | 6.624 | 5.883 | 6.777 | 6.790 | 6.647 | 5.914 | 6.823 | 6.818 | 6.663 | 5.936 | 6.845 |
| 5 | 132 | 5.691 | 5.577 | 4.956 | 5.689 | 5.674 | 5.566 | 4.941 | 5.673 | 5.682 | 5.571 | 4.949 | 5.682 | 5.687 | 5.574 | 4.953 | 5.686 |
| 6 | 132 | 7.788 | 7.516 | 6.794 | 7.786 | 7.661 | 7.429 | 6.674 | 7.637 | 7.708 | 7.465 | 6.723 | 7.714 | 7.759 | 7.493 | 6.762 | 7.756 |
| 7 | 132 | 5.002 | 4.787 | 4.346 | 4.956 | 4.970 | 4.767 | 4.317 | 4.922 | 4.984 | 4.776 | 4.330 | 4.941 | 4.995 | 4.782 | 4.339 | 4.950 |
| 8 | 132 | 5.817 | 5.837 | 5.073 | 5.876 | 5.749 | 5.788 | 5.009 | 5.798 | 5.775 | 5.809 | 5.036 | 5.839 | 5.802 | 5.825 | 5.057 | 5.861 |
| 9 | 33 | 13.184 | 13.419 | 11.468 | 13.471 | 13.040 | 13.263 | 11.335 | 13.384 | 13.104 | 13.312 | 11.399 | 13.414 | 13.154 | 13.342 | 11.437 | 13.455 |
| 10 | 33 | 14.981 | 14.510 | 13.019 | 14.954 | 14.703 | 14.196 | 12.766 | 14.788 | 14.843 | 14.290 | 12.901 | 14.874 | 14.930 | 14.337 | 12.967 | 14.947 |
| 11 | 11 | 19.277 | 23.080 | 16.802 | 21.984 | 19.206 | 23.009 | 16.737 | 21.935 | 19.236 | 23.042 | 16.767 | 21.947 | 19.262 | 23.063 | 16.787 | 21.970 |
| 12 | 33 | 12.732 | 12.248 | 11.065 | 12.673 | 12.605 | 12.117 | 10.950 | 12.604 | 12.671 | 12.161 | 11.013 | 12.645 | 12.709 | 12.181 | 11.042 | 12.678 |
| 13 | 11 | 21.221 | 25.889 | 18.458 | 25.056 | 21.123 | 25.788 | 18.369 | 24.976 | 21.171 | 25.841 | 18.416 | 25.006 | 21.202 | 25.867 | 18.439 | 25.037 |
| 14 | 33 | 6.844 | 6.544 | 5.933 | 6.731 | 6.798 | 6.499 | 5.893 | 6.709 | 6.825 | 6.516 | 5.918 | 6.728 | 6.837 | 6.523 | 5.926 | 6.739 |
| 15 | 33 | 10.527 | 9.946 | 9.135 | 10.314 | 10.398 | 9.793 | 9.018 | 10.235 | 10.465 | 9.837 | 9.083 | 10.278 | 10.504 | 9.857 | 9.112 | 10.311 |
| 16 | 33 | 8.501 | 8.237 | 7.374 | 8.443 | 8.433 | 8.165 | 7.313 | 8.407 | 8.469 | 8.190 | 7.347 | 8.431 | 8.489 | 8.201 | 7.362 | 8.448 |
| 17 | 33 | 10.793 | 10.371 | 9.367 | 10.678 | 10.664 | 10.231 | 9.250 | 10.607 | 10.733 | 10.276 | 9.315 | 10.652 | 10.771 | 10.296 | 9.344 | 10.684 |
| 18 | 33 | 7.151 | 6.772 | 6.199 | 6.984 | 7.095 | 6.709 | 6.149 | 6.954 | 7.126 | 6.729 | 6.178 | 6.975 | 7.142 | 6.737 | 6.190 | 6.989 |
| 19 | 33 | 7.447 | 6.992 | 6.456 | 7.258 | 7.388 | 6.926 | 6.403 | 7.198 | 7.421 | 6.947 | 6.434 | 7.221 | 7.437 | 6.956 | 6.446 | 7.235 |
| 20 | 33 | 7.791 | 7.394 | 6.755 | 7.620 | 7.724 | 7.319 | 6.695 | 7.585 | 7.761 | 7.344 | 6.730 | 7.610 | 7.780 | 7.353 | 6.744 | 7.627 |
| 21 | 33 | 12.251 | 11.653 | 10.638 | 12.024 | 11.998 | 11.349 | 10.407 | 11.866 | 12.128 | 11.434 | 10.533 | 11.948 | 12.205 | 11.473 | 10.591 | 12.013 |
| 22 | 33 | 12.045 | 11.524 | 10.459 | 11.864 | 11.768 | 11.185 | 10.207 | 11.685 | 11.909 | 11.277 | 10.343 | 11.773 | 11.994 | 11.321 | 10.408 | 11.845 |
| 23 | 33 | 7.200 | 6.932 | 6.246 | 7.082 | 7.068 | 6.751 | 6.125 | 6.989 | 7.134 | 6.795 | 6.189 | 7.028 | 7.175 | 6.817 | 6.221 | 7.062 |
| 24 | 33 | 9.483 | 9.177 | 8.248 | 9.382 | 9.013 | 8.490 | 7.812 | 8.933 | 9.227 | 8.632 | 8.026 | 9.047 | 9.387 | 8.713 | 8.148 | 9.177 |
| 25 | 33 | 8.009 | 8.566 | 7.078 | 8.392 | 6.544 | 6.141 | 5.670 | 6.736 | 7.093 | 6.482 | 6.244 | 6.985 | 7.645 | 6.743 | 6.678 | 7.418 |
| 26 | 33 | 6.274 | 8.459 | 5.912 | 7.747 | 3.719 | 3.113 | 3.221 | 3.806 | 4.424 | 3.430 | 4.003 | 4.269 | 5.457 | 3.773 | 4.872 | 5.228 |
| 27 | 33 | 8.537 | 9.301 | 7.539 | 8.965 | 6.981 | 6.751 | 6.050 | 7.330 | 7.607 | 7.154 | 6.693 | 7.656 | 8.167 | 7.434 | 7.132 | 8.105 |
| 28 | 132 | 4.664 | 4.455 | 4.062 | 4.620 | 4.567 | 4.389 | 3.968 | 4.498 | 4.597 | 4.412 | 4.001 | 4.556 | 4.639 | 4.436 | 4.034 | 4.593 |
| 29 | 33 | 4.529 | 4.844 | 4.009 | 4.755 | 3.691 | 3.382 | 3.197 | 3.726 | 4.019 | 3.578 | 3.535 | 3.890 | 4.324 | 3.717 | 3.777 | 4.125 |
| 30 | 33 | 7.154 | 9.396 | 6.682 | 8.615 | 4.302 | 3.576 | 3.727 | 4.356 | 5.220 | 3.980 | 4.702 | 4.955 | 6.303 | 4.326 | 5.607 | 5.933 |

Table D14: ANSI Simulated Results for Case 1 at $\mathbf{8 5 \%}$ penetration level and DG located at Bus $\mathbf{7}$

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.935 | 12.189 | 8.769 | 11.510 | 9.748 | 11.942 | 8.598 | 11.268 | 9.839 | 12.037 | 8.683 | 11.353 | 9.894 | 12.083 | 8.725 | 11.403 |
| 2 | 132 | 8.965 | 10.014 | 7.864 | 9.645 | 8.648 | 9.541 | 7.570 | 9.158 | 8.792 | 9.669 | 7.709 | 9.337 | 8.891 | 9.737 | 7.783 | 9.421 |
| 3 | 132 | 5.514 | 5.622 | 4.808 | 5.620 | 5.329 | 5.335 | 4.637 | 5.341 | 5.412 | 5.397 | 4.717 | 5.447 | 5.470 | 5.430 | 4.760 | 5.495 |
| 4 | 132 | 7.242 | 7.296 | 6.332 | 7.371 | 6.874 | 6.696 | 5.985 | 6.807 | 7.031 | 6.809 | 6.140 | 7.019 | 7.151 | 6.874 | 6.232 | 7.120 |
| 5 | 132 | 6.343 | 6.459 | 5.562 | 6.464 | 5.870 | 5.690 | 5.114 | 5.847 | 6.073 | 5.832 | 5.315 | 5.995 | 6.226 | 5.913 | 5.432 | 6.122 |
| 6 | 132 | 8.673 | 8.871 | 7.622 | 8.889 | 7.925 | 7.592 | 6.906 | 7.832 | 8.226 | 7.802 | 7.211 | 8.147 | 8.479 | 7.933 | 7.405 | 8.362 |
| 7 | 132 | 7.906 | 9.067 | 7.147 | 8.572 | 5.844 | 5.296 | 5.078 | 5.929 | 6.575 | 5.718 | 5.842 | 6.346 | 7.296 | 6.025 | 6.415 | 6.987 |
| 8 | 132 | 6.146 | 6.366 | 5.379 | 6.303 | 5.837 | 5.847 | 5.087 | 5.870 | 5.968 | 5.946 | 5.217 | 5.994 | 6.070 | 6.004 | 5.295 | 6.079 |
| 9 | 33 | 13.323 | 13.466 | 11.597 | 13.565 | 13.121 | 13.320 | 11.406 | 13.464 | 13.192 | 13.374 | 11.478 | 13.469 | 13.267 | 13.418 | 11.536 | 13.523 |
| 10 | 33 | 14.952 | 14.355 | 12.997 | 14.906 | 14.754 | 14.226 | 12.810 | 14.800 | 14.826 | 14.275 | 12.883 | 14.812 | 14.899 | 14.314 | 12.938 | 14.864 |
| 11 | 11 | 19.345 | 23.148 | 16.865 | 22.024 | 19.250 | 23.051 | 16.775 | 21.979 | 19.280 | 23.084 | 16.806 | 21.975 | 19.317 | 23.115 | 16.834 | 22.005 |
| 12 | 33 | 12.779 | 12.227 | 11.109 | 12.712 | 12.648 | 12.143 | 10.988 | 12.636 | 12.700 | 12.178 | 11.039 | 12.652 | 12.745 | 12.202 | 11.073 | 12.685 |
| 13 | 11 | 21.251 | 25.920 | 18.487 | 25.059 | 21.157 | 25.821 | 18.399 | 25.003 | 21.191 | 25.859 | 18.433 | 25.009 | 21.226 | 25.889 | 18.459 | 25.039 |
| 14 | 33 | 6.849 | 6.531 | 5.939 | 6.743 | 6.808 | 6.505 | 5.902 | 6.714 | 6.828 | 6.518 | 5.920 | 6.725 | 6.840 | 6.525 | 5.930 | 6.734 |
| 15 | 33 | 10.485 | 9.847 | 9.099 | 10.276 | 10.396 | 9.792 | 9.017 | 10.217 | 10.436 | 9.818 | 9.055 | 10.236 | 10.464 | 9.832 | 9.076 | 10.257 |
| 16 | 33 | 8.514 | 8.218 | 7.387 | 8.457 | 8.451 | 8.177 | 7.328 | 8.418 | 8.478 | 8.195 | 7.354 | 8.428 | 8.499 | 8.206 | 7.370 | 8.444 |
| 17 | 33 | 10.797 | 10.315 | 9.372 | 10.680 | 10.693 | 10.248 | 9.275 | 10.619 | 10.735 | 10.276 | 9.316 | 10.633 | 10.771 | 10.295 | 9.343 | 10.659 |
| 18 | 33 | 7.143 | 6.739 | 6.193 | 6.981 | 7.101 | 6.712 | 6.154 | 6.952 | 7.120 | 6.725 | 6.173 | 6.963 | 7.133 | 6.732 | 6.182 | 6.972 |
| 19 | 33 | 7.443 | 6.960 | 6.453 | 7.230 | 7.397 | 6.931 | 6.410 | 7.199 | 7.418 | 6.945 | 6.431 | 7.209 | 7.432 | 6.952 | 6.441 | 7.220 |
| 20 | 33 | 7.788 | 7.359 | 6.753 | 7.621 | 7.735 | 7.326 | 6.704 | 7.587 | 7.759 | 7.342 | 6.727 | 7.598 | 7.775 | 7.350 | 6.740 | 7.610 |
| 21 | 33 | 12.119 | 11.424 | 10.521 | 11.894 | 11.988 | 11.342 | 10.398 | 11.815 | 12.042 | 11.377 | 10.451 | 11.834 | 12.086 | 11.400 | 10.485 | 11.866 |
| 22 | 33 | 11.870 | 11.248 | 10.303 | 11.690 | 11.741 | 11.167 | 10.184 | 11.612 | 11.794 | 11.202 | 10.236 | 11.632 | 11.838 | 11.225 | 10.269 | 11.664 |
| 23 | 33 | 7.070 | 6.753 | 6.130 | 6.954 | 7.027 | 6.725 | 6.090 | 6.924 | 7.047 | 6.739 | 6.109 | 6.935 | 7.061 | 6.745 | 6.119 | 6.946 |
| 24 | 33 | 8.856 | 8.396 | 7.679 | 8.669 | 8.782 | 8.349 | 7.611 | 8.619 | 8.816 | 8.371 | 7.644 | 8.637 | 8.839 | 8.383 | 7.661 | 8.654 |
| 25 | 33 | 5.724 | 5.610 | 4.962 | 5.702 | 5.687 | 5.585 | 4.928 | 5.678 | 5.703 | 5.597 | 4.943 | 5.685 | 5.715 | 5.603 | 4.952 | 5.694 |
| 26 | 33 | 2.560 | 2.452 | 2.218 | 2.534 | 2.553 | 2.447 | 2.211 | 2.526 | 2.556 | 2.450 | 2.214 | 2.530 | 2.558 | 2.451 | 2.216 | 2.532 |
| 27 | 33 | 6.298 | 6.274 | 5.462 | 6.377 | 6.252 | 6.241 | 5.419 | 6.352 | 6.269 | 6.254 | 5.436 | 6.355 | 6.286 | 6.264 | 5.449 | 6.367 |
| 28 | 132 | 4.771 | 4.745 | 4.162 | 4.798 | 4.554 | 4.381 | 3.958 | 4.486 | 4.646 | 4.446 | 4.049 | 4.589 | 4.718 | 4.483 | 4.103 | 4.649 |
| 29 | 33 | 3.307 | 3.148 | 2.866 | 3.247 | 3.295 | 3.140 | 2.854 | 3.233 | 3.300 | 3.144 | 2.860 | 3.241 | 3.304 | 3.146 | 2.863 | 3.244 |
| 30 | 33 | 3.331 | 3.044 | 2.886 | 3.254 | 3.319 | 3.038 | 2.875 | 3.243 | 3.325 | 3.041 | 2.880 | 3.249 | 3.328 | 3.043 | 2.883 | 3.252 |

Table D15: ANSI Simulated Results for Case 2 at $\mathbf{8 5 \%}$ penetration level and DG located at Bus 26

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.730 | 11.921 | 8.579 | 11.265 | 9.720 | 11.911 | 8.570 | 11.254 | 9.724 | 11.916 | 8.574 | 11.261 | 9.728 | 11.919 | 8.577 | 11.264 |
| 2 | 132 | 8.578 | 9.484 | 7.505 | 9.166 | 8.564 | 9.493 | 7.493 | 9.151 | 8.569 | 9.477 | 7.498 | 9.160 | 8.575 | 9.481 | 7.503 | 9.164 |
| 3 | 132 | 5.302 | 5.317 | 4.611 | 5.358 | 5.290 | 5.309 | 4.601 | 5.345 | 5.294 | 5.312 | 4.605 | 5.353 | 5.300 | 5.315 | 4.609 | 5.357 |
| 4 | 132 | 6.801 | 6.651 | 5.921 | 6.828 | 6.778 | 6.636 | 5.899 | 6.801 | 6.785 | 6.642 | 5.907 | 6.815 | 6.796 | 6.648 | 5.915 | 6.824 |
| 5 | 132 | 5.683 | 5.571 | 4.949 | 5.682 | 5.678 | 5.568 | 4.945 | 5.677 | 5.681 | 5.570 | 4.947 | 5.680 | 5.682 | 5.571 | 4.948 | 5.682 |
| 6 | 132 | 7.722 | 7.468 | 6.728 | 7.717 | 7.685 | 7.444 | 6.693 | 7.672 | 7.693 | 7.452 | 6.704 | 7.695 | 7.712 | 7.462 | 6.718 | 7.710 |
| 7 | 132 | 4.987 | 4.777 | 4.331 | 4.941 | 4.977 | 4.771 | 4.322 | 4.931 | 4.980 | 4.773 | 4.326 | 4.937 | 4.985 | 4.775 | 4.329 | 4.940 |
| 8 | 132 | 5.779 | 5.809 | 5.036 | 5.838 | 5.760 | 5.795 | 5.018 | 5.815 | 5.765 | 5.800 | 5.024 | 5.827 | 5.775 | 5.805 | 5.031 | 5.834 |
| 9 | 33 | 13.161 | 13.394 | 11.441 | 13.456 | 13.105 | 13.307 | 11.391 | 13.434 | 13.126 | 13.324 | 11.413 | 13.437 | 13.149 | 13.337 | 11.430 | 13.457 |
| 10 | 33 | 14.961 | 14.478 | 12.991 | 14.946 | 14.843 | 14.282 | 12.886 | 14.908 | 14.898 | 14.320 | 12.492 | 14.932 | 14.941 | 14.342 | 12.972 | 14.969 |
| 11 | 11 | 19.266 | 23.066 | 16.790 | 21.978 | 19.239 | 23.040 | 16.765 | 21.961 | 19.248 | 23.050 | 16.775 | 21.961 | 19.260 | 23.060 | 16.784 | 21.972 |
| 12 | 33 | 12.717 | 12.231 | 11.048 | 12.665 | 12.664 | 12.153 | 11.000 | 12.654 | 12.690 | 12.170 | 11.027 | 12.666 | 12.709 | 12.180 | 11.040 | 12.683 |
| 13 | 11 | 21.210 | 25.875 | 18.446 | 25.050 | 21.170 | 25.834 | 18.410 | 25.019 | 21.188 | 25.855 | 18.428 | 25.027 | 21.203 | 25.867 | 18.439 | 25.042 |
| 14 | 33 | 6.839 | 6.538 | 5.928 | 6.728 | 6.818 | 6.511 | 5.910 | 6.727 | 6.831 | 6.519 | 5.922 | 6.735 | 6.836 | 6.522 | 5.926 | 6.740 |
| 15 | 33 | 10.521 | 9.933 | 9.126 | 10.312 | 10.466 | 9.833 | 9.077 | 10.294 | 10.493 | 9.851 | 9.104 | 10.306 | 10.512 | 9.861 | 9.118 | 10.323 |
| 16 | 33 | 8.493 | 8.228 | 7.365 | 8.438 | 8.464 | 8.185 | 7.339 | 8.434 | 8.480 | 8.195 | 7.354 | 8.442 | 8.489 | 8.200 | 7.361 | 8.451 |
| 17 | 33 | 10.782 | 10.355 | 9.352 | 10.672 | 10.726 | 10.268 | 9.303 | 10.661 | 10.755 | 10.287 | 9.331 | 10.675 | 10.773 | 10.297 | 9.344 | 10.691 |
| 18 | 33 | 7.147 | 6.766 | 6.194 | 6.982 | 7.122 | 6.725 | 6.172 | 6.978 | 7.136 | 6.734 | 6.185 | 6.986 | 7.143 | 6.737 | 6.191 | 6.992 |
| 19 | 33 | 7.442 | 6.985 | 6.450 | 7.248 | 7.416 | 6.943 | 6.427 | 7.223 | 7.431 | 6.952 | 6.441 | 7.231 | 7.439 | 6.956 | 6.447 | 7.238 |
| 20 | 33 | 7.786 | 7.386 | 6.784 | 7.617 | 7.756 | 7.338 | 6.722 | 7.613 | 7.772 | 7.349 | 6.738 | 7.622 | 7.781 | 7.354 | 6.744 | 7.630 |
| 21 | 33 | 12.246 | 11.630 | 10.625 | 12.026 | 12.136 | 11.430 | 10.526 | 11.985 | 12.188 | 11.465 | 10.579 | 12.008 | 12.228 | 11.485 | 10.607 | 12.042 |
| 22 | 33 | 12.044 | 11.501 | 10.449 | 11.869 | 11.923 | 11.277 | 10.341 | 11.819 | 11.979 | 11.315 | 10.398 | 11.843 | 12.023 | 11.337 | 10.429 | 11.881 |
| 23 | 33 | 7.208 | 6.925 | 6.248 | 7.090 | 7.151 | 6.800 | 6.197 | 7.059 | 7.175 | 6.818 | 6.222 | 7.067 | 7.197 | 6.829 | 6.238 | 7.086 |
| 24 | 33 | 9.551 | 9.169 | 8.287 | 9.389 | 9.344 | 8.683 | 8.098 | 9.210 | 9.416 | 8.733 | 8.178 | 9.220 | 9.508 | 8.777 | 8.245 | 9.294 |
| 25 | 33 | 8.500 | 8.682 | 7.420 | 8.609 | 7.745 | 6.795 | 6.710 | 7.762 | 7.910 | 6.892 | 6.928 | 7.703 | 8.299 | 7.055 | 7.219 | 8.010 |
| 26 | 33 | 17.355 | 24.727 | 16.187 | 21.976 | 8.264 | 4.647 | 7.158 | 8.153 | 9.843 | 4.759 | 9.178 | 9.412 | 13.979 | 5.211 | 12.660 | 13.071 |
| 27 | 33 | 7.328 | 7.419 | 6.366 | 7.441 | 7.036 | 6.755 | 6.097 | 7.190 | 7.130 | 6.821 | 6.205 | 7.195 | 7.263 | 6.889 | 6.303 | 7.306 |
| 28 | 132 | 4.591 | 4.405 | 3.990 | 4.545 | 4.567 | 4.388 | 3.968 | 4.513 | 4.569 | 4.392 | 3.972 | 4.527 | 4.584 | 4.400 | 3.983 | 4.539 |
| 29 | 33 | 3.496 | 3.357 | 3.031 | 3.458 | 3.433 | 3.223 | 2.973 | 3.370 | 3.461 | 3.242 | 3.003 | 3.381 | 3.485 | 3.254 | 3.020 | 3.402 |
| 30 | 33 | 3.492 | 3.222 | 3.027 | 3.436 | 3.346 | 3.101 | 2.976 | 3.303 | 3.462 | 3.117 | 3.002 | 3.340 | 3.482 | 3.127 | 3.017 | 3.354 |

Table D16: ANSI Simulated Results for Case 3 at $\mathbf{8 5 \%}$ penetration level and DG located at Bus $\mathbf{2 9}$

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.744 | 11.935 | 8.591 | 11.279 | 9.730 | 11.921 | 8.579 | 11.262 | 9.735 | 11.927 | 8.584 | 11.271 | 9.741 | 11.932 | 8.588 | 11.276 |
| 2 | 132 | 8.601 | 9.502 | 7.526 | 9.187 | 8.581 | 9.486 | 7.508 | 9.163 | 8.587 | 9.492 | 7.514 | 9.175 | 8.596 | 9.498 | 7.521 | 9.183 |
| 3 | 132 | 5.320 | 5.329 | 4.627 | 5.375 | 5.304 | 5.318 | 4.613 | 5.355 | 5.308 | 5.322 | 4.617 | 5.365 | 5.316 | 5.326 | 4.623 | 5.371 |
| 4 | 132 | 6.838 | 6.676 | 5.954 | 6.863 | 6.808 | 6.655 | 5.926 | 6.823 | 6.813 | 6.660 | 5.932 | 6.841 | 6.830 | 6.669 | 5.945 | 6.855 |
| 5 | 132 | 5.692 | 5.577 | 4.957 | 5.690 | 5.685 | 5.572 | 4.950 | 5.681 | 5.687 | 5.574 | 4.953 | 5.686 | 5.691 | 5.576 | 4.955 | 5.689 |
| 6 | 132 | 7.808 | 7.523 | 6.805 | 7.798 | 7.760 | 7.490 | 6.759 | 7.729 | 7.760 | 7.495 | 6.765 | 7.757 | 7.792 | 7.512 | 6.788 | 7.783 |
| 7 | 132 | 5.006 | 4.789 | 4.348 | 4.959 | 4.993 | 4.780 | 4.336 | 4.942 | 4.995 | 4.783 | 4.339 | 4.950 | 5.002 | 4.786 | 4.344 | 4.956 |
| 8 | 132 | 5.831 | 5.844 | 5.082 | 5.886 | 5.804 | 5.824 | 5.057 | 5.848 | 5.805 | 5.828 | 5.060 | 5.864 | 5.822 | 5.837 | 5.073 | 5.878 |
| 9 | 33 | 13.141 | 13.352 | 11.425 | 13.427 | 13.092 | 13.297 | 11.379 | 13.415 | 13.105 | 13.309 | 11.395 | 13.409 | 13.129 | 13.323 | 11.413 | 13.429 |
| 10 | 33 | 14.869 | 14.345 | 12.912 | 14.847 | 14.773 | 14.237 | 12.825 | 14.824 | 14.813 | 14.265 | 12.867 | 14.836 | 14.851 | 14.285 | 12.894 | 14.868 |
| 11 | 11 | 19.255 | 23.056 | 16.780 | 21.962 | 19.231 | 23.032 | 16.758 | 21.951 | 19.236 | 23.039 | 16.765 | 21.946 | 19.249 | 23.049 | 16.774 | 21.957 |
| 12 | 33 | 12.690 | 12.185 | 11.024 | 12.637 | 12.644 | 12.140 | 10.983 | 12.627 | 12.664 | 12.153 | 11.003 | 12.634 | 12.681 | 12.163 | 11.016 | 12.649 |
| 13 | 11 | 21.186 | 25.850 | 18.425 | 25.019 | 21.152 | 25.816 | 18.394 | 24.995 | 21.165 | 25.831 | 18.407 | 24.998 | 21.179 | 25.843 | 18.418 | 25.011 |
| 14 | 33 | 6.829 | 6.522 | 5.920 | 6.720 | 6.811 | 6.507 | 5.904 | 6.717 | 6.821 | 6.513 | 5.914 | 6.723 | 6.827 | 6.516 | 5.917 | 6.728 |
| 15 | 33 | 10.471 | 9.863 | 9.082 | 10.261 | 10.425 | 9.809 | 9.041 | 10.248 | 10.447 | 9.823 | 9.063 | 10.258 | 10.463 | 9.831 | 9.075 | 10.272 |
| 16 | 33 | 8.478 | 8.202 | 7.352 | 8.423 | 8.453 | 8.177 | 7.300 | 8.419 | 8.465 | 8.186 | 7.341 | 8.424 | 8.474 | 8.190 | 7.348 | 8.432 |
| 17 | 33 | 10.746 | 10.300 | 9.321 | 10.636 | 10.700 | 10.252 | 9.280 | 10.627 | 10.721 | 10.266 | 9.302 | 10.636 | 10.738 | 10.275 | 9.314 | 10.650 |
| 18 | 33 | 7.130 | 6.739 | 6.179 | 6.966 | 7.109 | 6.717 | 6.161 | 6.962 | 7.120 | 6.724 | 6.171 | 6.968 | 7.126 | 6.727 | 6.176 | 6.973 |
| 19 | 33 | 7.425 | 6.958 | 6.435 | 7.222 | 7.403 | 6.935 | 6.416 | 7.207 | 7.415 | 6.943 | 6.427 | 7.213 | 7.422 | 6.946 | 6.432 | 7.219 |
| 20 | 33 | 7.767 | 7.356 | 6.732 | 7.599 | 7.742 | 7.330 | 6.710 | 7.595 | 7.755 | 7.338 | 6.722 | 7.602 | 7.763 | 7.342 | 6.728 | 7.608 |
| 21 | 33 | 12.132 | 11.482 | 10.525 | 11.908 | 12.045 | 11.376 | 10.447 | 11.885 | 12.085 | 11.403 | 10.487 | 11.901 | 12.117 | 11.418 | 10.510 | 11.927 |
| 22 | 33 | 11.908 | 11.330 | 10.330 | 11.728 | 11.814 | 11.211 | 10.246 | 11.701 | 11.857 | 11.240 | 10.290 | 11.718 | 11.891 | 11.257 | 10.314 | 11.747 |
| 23 | 33 | 7.123 | 6.823 | 6.174 | 7.002 | 7.079 | 6.757 | 6.135 | 6.986 | 7.100 | 6.771 | 6.156 | 6.995 | 7.116 | 6.779 | 6.167 | 7.008 |
| 24 | 33 | 9.153 | 8.728 | 7.938 | 8.965 | 9.009 | 8.486 | 7.808 | 8.883 | 9.071 | 8.528 | 7.871 | 8.903 | 9.126 | 8.555 | 7.912 | 8.949 |
| 25 | 33 | 6.725 | 6.724 | 5.847 | 6.740 | 6.377 | 6.022 | 5.525 | 6.450 | 6.497 | 6.105 | 5.658 | 6.467 | 6.648 | 6.179 | 5.770 | 6.590 |
| 26 | 33 | 2.703 | 2.613 | 2.344 | 2.697 | 2.646 | 2.504 | 2.292 | 2.593 | 2.671 | 2.521 | 2.318 | 2.606 | 2.693 | 2.532 | 2.333 | 2.621 |
| 27 | 33 | 9.508 | 9.990 | 8.327 | 9.784 | 8.387 | 7.586 | 7.268 | 8.661 | 8.684 | 7.744 | 7.627 | 8.639 | 9.218 | 7.978 | 8.030 | 9.065 |
| 28 | 132 | 4.705 | 4.476 | 4.092 | 4.651 | 4.671 | 4.452 | 4.058 | 4.593 | 4.660 | 4.449 | 4.054 | 4.611 | 4.690 | 4.465 | 4.076 | 4.636 |
| 29 | 33 | 18.166 | 25.661 | 17.529 | 22.848 | 8.550 | 5.531 | 7.406 | 8.706 | 10.581 | 5.717 | 9.828 | 9.967 | 14.768 | 6.283 | 13.345 | 13.662 |
| 30 | 33 | 5.414 | 5.387 | 4.751 | 5.521 | 4.714 | 3.724 | 4.083 | 4.583 | 4.871 | 3.799 | 4.285 | 4.559 | 5.221 | 3.916 | 4.551 | 4.826 |

Table D17: ANSI Simulated Results for Case $\mathbf{4}$ at $\mathbf{8 5 \%}$ penetration level and DG located at Bus $\mathbf{3 0}$

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.737 | 11.929 | 8.586 | 11.273 | 9.725 | 11.916 | 8.574 | 11.258 | 9.735 | 11.926 | 8.583 | 11.271 | 9.729 | 11.922 | 8.579 | 11.266 |
| 2 | 132 | 8.590 | 9.494 | 7.516 | 9.178 | 8.572 | 9.479 | 7.501 | 9.157 | 8.586 | 9.490 | 7.512 | 9.174 | 8.578 | 9.485 | 7.506 | 9.168 |
| 3 | 132 | 5.311 | 5.323 | 4.619 | 5.367 | 5.297 | 5.313 | 4.606 | 5.349 | 5.307 | 5.320 | 4.616 | 5.364 | 5.300 | 5.316 | 4.611 | 5.358 |
| 4 | 132 | 6.819 | 6.663 | 5.936 | 6.846 | 6.792 | 6.644 | 5.911 | 6.810 | 6.811 | 6.658 | 5.929 | 6.839 | 6.797 | 6.650 | 5.918 | 6.827 |
| 5 | 132 | 5.688 | 5.575 | 4.953 | 5.687 | 5.682 | 5.570 | 4.947 | 5.679 | 5.687 | 5.574 | 4.952 | 5.686 | 5.684 | 5.572 | 4.950 | 5.684 |
| 6 | 132 | 7.771 | 7.500 | 6.772 | 7.765 | 7.727 | 7.470 | 6.730 | 7.703 | 7.757 | 7.490 | 6.758 | 7.752 | 7.729 | 7.475 | 6.737 | 7.729 |
| 7 | 132 | 4.998 | 4.784 | 4.341 | 4.952 | 4.986 | 4.776 | 4.330 | 4.937 | 4.995 | 4.782 | 4.338 | 4.949 | 4.988 | 4.778 | 4.333 | 4.944 |
| 8 | 132 | 5.811 | 5.831 | 5.064 | 5.868 | 5.786 | 5.813 | 5.041 | 5.834 | 5.803 | 5.825 | 5.057 | 5.861 | 5.788 | 5.816 | 5.046 | 5.849 |
| 9 | 33 | 13.114 | 13.330 | 11.400 | 13.404 | 13.069 | 13.281 | 11.359 | 13.393 | 13.103 | 13.305 | 11.390 | 13.407 | 13.082 | 13.292 | 11.374 | 13.389 |
| 10 | 33 | 14.828 | 14.314 | 12.875 | 14.811 | 14.742 | 14.218 | 12.799 | 14.792 | 14.812 | 14.260 | 12.860 | 14.832 | 14.779 | 14.244 | 12.836 | 14.804 |
| 11 | 11 | 19.241 | 23.042 | 16.767 | 21.950 | 19.219 | 23.021 | 16.748 | 21.938 | 19.235 | 23.036 | 16.762 | 21.944 | 19.224 | 23.027 | 16.754 | 21.935 |
| 12 | 33 | 12.670 | 12.171 | 11.007 | 12.620 | 12.629 | 12.131 | 10.970 | 12.612 | 12.663 | 12.151 | 11.000 | 12.632 | 12.648 | 12.143 | 10.989 | 12.619 |
| 13 | 11 | 21.170 | 25.834 | 18.411 | 25.003 | 21.139 | 25.803 | 18.383 | 24.981 | 21.164 | 25.828 | 18.405 | 24.996 | 21.152 | 25.817 | 18.396 | 24.984 |
| 14 | 33 | 6.824 | 6.518 | 5.915 | 6.716 | 6.808 | 6.505 | 5.901 | 6.713 | 6.821 | 6.513 | 5.913 | 6.723 | 4.817 | 6.511 | 5.910 | 6.719 |
| 15 | 33 | 10.453 | 9.849 | 9.067 | 10.245 | 10.412 | 9.801 | 9.030 | 10.235 | 10.446 | 9.821 | 9.060 | 10.256 | 10.432 | 9.814 | 9.050 | 10.244 |
| 16 | 33 | 8.468 | 8.195 | 7.343 | 8.415 | 8.446 | 8.173 | 7.324 | 8.412 | 8.465 | 8.185 | 7.340 | 8.423 | 8.457 | 8.181 | 7.334 | 8.417 |
| 17 | 33 | 10.728 | 10.286 | 9.305 | 10.620 | 10.687 | 10.243 | 9.269 | 10.613 | 10.721 | 10.264 | 9.299 | 10.634 | 10.706 | 10.257 | 9.288 | 10.622 |
| 18 | 33 | 7.122 | 6.734 | 6.173 | 6.960 | 7.104 | 6.714 | 6.157 | 6.957 | 7.120 | 6.723 | 6.170 | 6.967 | 7.114 | 6.720 | 6.166 | 6.962 |
| 19 | 33 | 7.418 | 6.952 | 6.429 | 7.215 | 7.398 | 6.932 | 6.412 | 7.201 | 7.415 | 6.942 | 6.426 | 7.212 | 7.409 | 6.939 | 6.422 | 7.207 |
| 20 | 33 | 7.758 | 7.349 | 6.724 | 7.592 | 7.736 | 7.326 | 6.705 | 7.588 | 7.755 | 7.337 | 6.721 | 7.600 | 7.747 | 7.334 | 6.716 | 7.594 |
| 21 | 33 | 12.098 | 11.455 | 10.495 | 11.878 | 12.020 | 11.361 | 10.426 | 11.858 | 12.084 | 11.399 | 10.482 | 11.897 | 12.057 | 11.385 | 10.462 | 11.874 |
| 22 | 33 | 11.871 | 11.300 | 10.298 | 11.695 | 11.787 | 11.195 | 10.223 | 11.672 | 11.856 | 11.236 | 10.284 | 11.714 | 11.827 | 11.221 | 10.263 | 11.689 |
| 23 | 33 | 7.106 | 6.808 | 6.159 | 6.987 | 7.067 | 6.749 | 6.124 | 6.973 | 7.100 | 6.769 | 6.153 | 6.993 | 7.086 | 6.762 | 6.143 | 6.981 |
| 24 | 33 | 9.092 | 8.675 | 7.884 | 8.906 | 8.965 | 8.459 | 7.769 | 8.836 | 9.068 | 8.521 | 7.861 | 8.896 | 9.021 | 8.497 | 7.827 | 8.857 |
| 25 | 33 | 6.552 | 6.556 | 5.694 | 6.565 | 6.255 | 5.948 | 5.420 | 6.325 | 6.489 | 6.085 | 5.630 | 6.447 | 6.362 | 6.022 | 5.537 | 6.344 |
| 26 | 33 | 2.680 | 2.590 | 2.323 | 2.673 | 2.629 | 2.494 | 2.277 | 2.575 | 2.670 | 2.519 | 2.314 | 2.605 | 2.652 | 2.510 | 2.301 | 2.592 |
| 27 | 33 | 8.866 | 9.308 | 7.749 | 9.142 | 7.982 | 7.349 | 6.917 | 8.246 | 8.644 | 7.681 | 7.523 | 8.565 | 8.227 | 7.490 | 7.210 | 8.232 |
| 28 | 132 | 4.670 | 4.454 | 4.061 | 4.619 | 4.638 | 4.432 | 4.030 | 4.566 | 4.657 | 4.445 | 4.047 | 4.606 | 4.631 | 4.431 | 4.028 | 4.584 |
| 29 | 33 | 5.362 | 5.542 | 4.706 | 5.510 | 4.670 | 3.892 | 4.045 | 4.650 | 5.171 | 4.096 | 4.508 | 4.879 | 4.824 | 3.967 | 4.244 | 4.613 |
| 30 | 33 | 18.209 | 25.687 | 17.567 | 22.859 | 8.514 | 5.162 | 7.375 | 8.536 | 14.802 | 5.838 | 13.375 | 13.686 | 10.603 | 5.344 | 9.849 | 9.995 |

Table D18: ANSI Simulated Results for Case $\mathbf{5}$ at $\mathbf{8 5 \%}$ penetration level and DG located at Bus 7 and 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.906 | 12.163 | 8.746 | 11.485 | 9.726 | 11.920 | 8.578 | 11.237 | 9.811 | 12.010 | 8.659 | 11.330 | 9.866 | 12.058 | 8.702 | 11.379 |
| 2 | 132 | 8.900 | 9.966 | 7.812 | 9.592 | 8.595 | 9.499 | 7.523 | 9.128 | 8.733 | 9.621 | 7.656 | 9.289 | 8.830 | 9.691 | 7.733 | 9.372 |
| 3 | 132 | 5.494 | 5.611 | 4.793 | 5.604 | 5.309 | 5.321 | 4.618 | 5.332 | 5.391 | 5.382 | 4.698 | 5.429 | 5.451 | 5.418 | 4.745 | 5.479 |
| 4 | 132 | 7.202 | 7.275 | 6.304 | 7.340 | 6.829 | 6.668 | 5.946 | 6.787 | 6.988 | 6.782 | 6.102 | 6.983 | 7.113 | 6.852 | 6.201 | 7.089 |
| 5 | 132 | 6.166 | 6.342 | 5.413 | 6.321 | 5.743 | 5.610 | 5.003 | 5.699 | 5.929 | 5.741 | 5.185 | 5.878 | 6.065 | 5.817 | 5.294 | 5.993 |
| 6 | 132 | 8.573 | 8.814 | 7.549 | 8.812 | 7.827 | 7.531 | 6.820 | 7.712 | 8.128 | 7.743 | 7.123 | 8.065 | 8.387 | 7.883 | 7.330 | 8.288 |
| 7 | 132 | 6.875 | 8.173 | 6.216 | 7.696 | 5.316 | 4.980 | 4.619 | 5.329 | 5.905 | 5.356 | 5.219 | 5.747 | 6.448 | 5.624 | 5.670 | 6.240 |
| 8 | 132 | 6.135 | 6.364 | 5.376 | 6.298 | 5.816 | 5.834 | 5.069 | 5.840 | 5.948 | 5.933 | 5.200 | 5.979 | 6.058 | 5.998 | 5.287 | 6.072 |
| 9 | 33 | 13.373 | 13.526 | 11.648 | 13.613 | 13.110 | 13.313 | 11.397 | 13.465 | 13.216 | 13.393 | 11.502 | 13.505 | 13.311 | 13.451 | 11.577 | 13.576 |
| 10 | 33 | 15.077 | 14.486 | 13.113 | 15.013 | 14.760 | 14.232 | 12.816 | 14.839 | 14.901 | 14.327 | 12.954 | 14.908 | 15.009 | 14.385 | 13.037 | 14.991 |
| 11 | 11 | 19.372 | 23.177 | 16.892 | 22.055 | 19.245 | 23.047 | 16.772 | 21.980 | 19.294 | 23.099 | 16.820 | 21.995 | 19.341 | 23.139 | 16.857 | 22.033 |
| 12 | 33 | 12.822 | 12.273 | 11.151 | 12.746 | 12.641 | 12.140 | 10.981 | 12.642 | 12.723 | 12.194 | 11.061 | 12.685 | 12.783 | 12.226 | 11.107 | 12.732 |
| 13 | 11 | 21.289 | 25.962 | 18.523 | 25.106 | 21.154 | 25.819 | 18.396 | 25.010 | 21.212 | 25.883 | 18.453 | 25.040 | 21.259 | 25.924 | 18.489 | 25.081 |
| 14 | 33 | 6.862 | 6.544 | 5.951 | 6.750 | 6.804 | 6.503 | 5.898 | 6.715 | 6.834 | 6.523 | 5.927 | 6.736 | 6.851 | 6.531 | 5.939 | 6.749 |
| 15 | 33 | 10.544 | 9.910 | 9.153 | 10.324 | 10.404 | 9.797 | 9.024 | 10.240 | 10.472 | 9.841 | 9.089 | 10.281 | 10.516 | 9.864 | 9.123 | 10.316 |
| 16 | 33 | 8.537 | 8.242 | 7.408 | 8.473 | 8.448 | 8.175 | 7.326 | 8.422 | 8.490 | 8.204 | 7.366 | 8.447 | 8.518 | 8.219 | 7.388 | 8.469 |
| 17 | 33 | 10.846 | 10.367 | 9.418 | 10.719 | 10.691 | 10.247 | 9.273 | 10.632 | 10.764 | 10.296 | 9.343 | 10.672 | 10.814 | 10.323 | 9.382 | 10.711 |
| 18 | 33 | 7.163 | 6.761 | 6.212 | 6.996 | 7.100 | 6.712 | 6.154 | 6.959 | 7.132 | 6.733 | 6.184 | 6.979 | 7.151 | 6.743 | 6.198 | 6.995 |
| 19 | 33 | 7.463 | 6.983 | 6.472 | 7.255 | 7.395 | 6.931 | 6.409 | 7.205 | 7.430 | 6.953 | 6.442 | 7.226 | 7.450 | 6.963 | 6.458 | 7.243 |
| 20 | 33 | 7.812 | 7.385 | 6.775 | 7.639 | 7.733 | 7.325 | 6.703 | 7.593 | 7.772 | 7.351 | 6.740 | 7.617 | 7.796 | 7.363 | 6.759 | 7.637 |
| 21 | 33 | 12.245 | 11.556 | 10.636 | 12.002 | 12.010 | 11.356 | 10.418 | 11.868 | 12.122 | 11.429 | 10.527 | 11.931 | 12.198 | 11.468 | 10.584 | 11.991 |
| 22 | 33 | 12.013 | 11.400 | 10.434 | 11.815 | 11.772 | 11.187 | 10.211 | 11.676 | 11.888 | 11.263 | 10.323 | 11.742 | 11.965 | 11.303 | 10.382 | 11.803 |
| 23 | 33 | 7.147 | 6.838 | 6.199 | 7.023 | 7.051 | 6.740 | 6.111 | 6.964 | 7.099 | 6.772 | 6.157 | 6.994 | 7.129 | 6.788 | 6.180 | 7.018 |
| 24 | 33 | 9.163 | 8.735 | 7.956 | 8.979 | 8.902 | 8.422 | 7.715 | 8.791 | 9.029 | 8.507 | 7.840 | 8.862 | 9.113 | 8.549 | 7.903 | 8.931 |
| 25 | 33 | 6.594 | 6.628 | 5.746 | 6.639 | 6.079 | 5.842 | 5.268 | 6.178 | 6.303 | 5.993 | 5.496 | 6.281 | 6.486 | 6.087 | 5.634 | 6.430 |
| 26 | 33 | 2.687 | 2.602 | 2.332 | 2.685 | 2.602 | 2.477 | 2.254 | 2.552 | 2.645 | 2.506 | 2.296 | 2.589 | 2.672 | 2.520 | 2.316 | 2.609 |
| 27 | 33 | 8.919 | 9.512 | 7.854 | 9.235 | 7.448 | 7.044 | 6.456 | 7.788 | 7.991 | 7.372 | 7.030 | 7.991 | 8.560 | 7.643 | 7.471 | 8.444 |
| 28 | 132 | 4.898 | 4.834 | 4.282 | 4.918 | 6.638 | 4.432 | 4.030 | 4.561 | 4.732 | 4.500 | 4.128 | 4.668 | 4.831 | 4.553 | 4.206 | 4.752 |
| 29 | 33 | 10.835 | 14.992 | 10.333 | 13.509 | 5.563 | 4.408 | 4.819 | 5.797 | 7.008 | 4.850 | 6.416 | 6.626 | 9.109 | 5.362 | 8.177 | 8.509 |
| 30 | 33 | 4.977 | 5.050 | 4.392 | 5.138 | 4.096 | 3.447 | 3.548 | 4.026 | 4.400 | 3.604 | 3.876 | 4.136 | 4.752 | 3.737 | 4.150 | 4.418 |

Table D19: ANSI Simulated Results for Case 6 at $85 \%$ penetration level and DG located at Bus 26 and 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 9.752 | 11.943 | 8.599 | 11.284 | 9.728 | 11.920 | 8.578 | 11.258 | 9.739 | 11.931 | 8.588 | 11.273 | 9.747 | 11.938 | 8.594 | 11.281 |
| 2 | 132 | 8.613 | 9.513 | 7.537 | 9.196 | 8.579 | 9.485 | 7.507 | 9.157 | 8.592 | 9.497 | 7.520 | 9.179 | 8.606 | 9.506 | 7.530 | 9.190 |
| 3 | 132 | 5.333 | 5.338 | 4.639 | 5.384 | 5.305 | 5.318 | 4.613 | 5.352 | 5.315 | 5.326 | 4.624 | 5.369 | 5.326 | 5.333 | 4.633 | 5.379 |
| 4 | 132 | 6.866 | 6.694 | 5.979 | 6.884 | 6.811 | 6.656 | 5.929 | 6.818 | 6.828 | 6.671 | 5.947 | 6.852 | 6.853 | 6.684 | 5.965 | 6.872 |
| 5 | 132 | 5.696 | 5.580 | 4.960 | 5.693 | 5.683 | 5.571 | 4.949 | 5.679 | 5.689 | 5.575 | 4.954 | 5.687 | 5.693 | 5.578 | 4.958 | 5.691 |
| 6 | 132 | 7.849 | 7.551 | 6.843 | 7.831 | 7.760 | 7.490 | 6.759 | 7.715 | 7.780 | 7.509 | 6.784 | 7.771 | 7.825 | 7.533 | 6.818 | 7.808 |
| 7 | 132 | 5.014 | 4.794 | 4.356 | 4.965 | 4.992 | 4.779 | 4.335 | 4.938 | 4.999 | 4.785 | 4.343 | 4.952 | 5.009 | 4.791 | 4.350 | 4.960 |
| 8 | 132 | 5.849 | 5.857 | 5.099 | 5.900 | 5.801 | 5.822 | 5.054 | 5.838 | 5.812 | 5.833 | 5.068 | 5.868 | 5.836 | 5.847 | 5.086 | 5.888 |
| 9 | 33 | 13.236 | 13.455 | 11.510 | 13.519 | 13.129 | 13.324 | 11.412 | 13.469 | 13.169 | 13.356 | 11.454 | 13.475 | 13.213 | 13.381 | 11.486 | 13.511 |
| 10 | 33 | 15.061 | 14.562 | 13.083 | 15.029 | 14.842 | 14.283 | 12.886 | 14.930 | 14.946 | 14.353 | 12.989 | 14.977 | 15.021 | 14.392 | 13.044 | 15.041 |
| 11 | 11 | 19.305 | 23.105 | 16.825 | 22.012 | 19.253 | 23.054 | 16.778 | 21.981 | 19.271 | 23.073 | 16.796 | 21.981 | 19.293 | 23.091 | 16.813 | 22.000 |
| 12 | 33 | 12.767 | 12.270 | 11.093 | 12.706 | 12.667 | 12.155 | 11.003 | 12.667 | 12.716 | 12.188 | 11.051 | 12.691 | 12.749 | 12.205 | 11.076 | 12.719 |
| 13 | 11 | 21.250 | 25.916 | 18.482 | 25.088 | 21.175 | 25.840 | 18.414 | 25.033 | 21.209 | 25.877 | 18.448 | 25.047 | 21.236 | 25.900 | 18.468 | 25.073 |
| 14 | 33 | 6.852 | 6.549 | 5.940 | 6.740 | 6.815 | 6.509 | 5.907 | 6.728 | 6.837 | 6.524 | 5.928 | 6.742 | 6.847 | 6.529 | 5.935 | 6.751 |
| 15 | 33 | 10.561 | 9.968 | 9.163 | 10.346 | 10.459 | 9.829 | 9.071 | 10.298 | 10.510 | 9.863 | 9.121 | 10.324 | 10.543 | 9.879 | 9.146 | 10.352 |
| 16 | 33 | 8.517 | 8.248 | 7.387 | 8.458 | 8.463 | 8.184 | 7.339 | 8.439 | 8.491 | 8.203 | 7.366 | 8.454 | 8.508 | 8.212 | 7.378 | 8.468 |
| 17 | 33 | 10.826 | 10.391 | 9.393 | 10.709 | 10.723 | 10.267 | 9.301 | 10.668 | 10.776 | 10.302 | 9.352 | 10.696 | 10.809 | 10.319 | 9.376 | 10.724 |
| 18 | 33 | 7.163 | 6.780 | 6.209 | 6.996 | 7.118 | 6.722 | 6.169 | 6.979 | 7.143 | 6.739 | 6.193 | 6.993 | 7.156 | 6.745 | 6.202 | 7.005 |
| 19 | 33 | 7.460 | 7.000 | 6.466 | 7.267 | 7.412 | 6.940 | 6.424 | 7.224 | 7.439 | 6.957 | 6.449 | 7.240 | 7.453 | 6.964 | 6.459 | 7.252 |
| 20 | 33 | 7.807 | 7.403 | 6.768 | 7.635 | 7.752 | 7.336 | 6.719 | 7.615 | 7.782 | 7.356 | 6.747 | 7.632 | 7.798 | 7.364 | 6.759 | 7.646 |
| 21 | 33 | 12.321 | 11.698 | 10.694 | 12.090 | 12.119 | 11.422 | 10.512 | 11.990 | 12.218 | 11.486 | 10.609 | 12.039 | 12.285 | 11.520 | 10.659 | 12.096 |
| 22 | 33 | 12.122 | 11.575 | 10.522 | 11.937 | 11.902 | 11.266 | 10.323 | 11.822 | 12.008 | 11.336 | 10.429 | 11.874 | 12.083 | 11.373 | 10.483 | 11.937 |
| 23 | 33 | 7.239 | 6.959 | 6.278 | 7.118 | 7.135 | 6.791 | 6.183 | 7.056 | 7.183 | 6.824 | 6.232 | 7.077 | 7.220 | 6.843 | 6.259 | 7.107 |
| 24 | 33 | 9.650 | 9.294 | 8.383 | 9.515 | 9.275 | 8.645 | 8.038 | 9.187 | 9.429 | 8.747 | 8.198 | 9.240 | 9.572 | 8.817 | 8.305 | 9.357 |
| 25 | 33 | 8.809 | 9.236 | 7.745 | 9.106 | 7.416 | 6.647 | 6.425 | 7.594 | 7.867 | 6.892 | 6.926 | 7.702 | 8.457 | 7.142 | 7.378 | 8.168 |
| 26 | 33 | 10.102 | 14.162 | 9.692 | 12.744 | 5.222 | 3.780 | 4.523 | 5.313 | 6.336 | 4.060 | 5.828 | 6.074 | 8.401 | 4.492 | 7.564 | 7.942 |
| 27 | 33 | 9.360 | 10.028 | 8.232 | 9.712 | 7.836 | 7.288 | 6.792 | 8.209 | 8.383 | 7.595 | 7.379 | 8.391 | 8.993 | 7.872 | 7.847 | 8.881 |
| 28 | 132 | 4.721 | 4.487 | 4.108 | 4.664 | 4.657 | 4.443 | 4.046 | 4.570 | 4.661 | 4.451 | 4.056 | 4.610 | 4.700 | 4.471 | 4.086 | 4.643 |
| 29 | 33 | 5.046 | 5.312 | 4.452 | 5.249 | 4.165 | 3.646 | 3.608 | 4.205 | 4.463 | 3.804 | 3.933 | 4.296 | 4.822 | 3.949 | 4.211 | 4.573 |
| 30 | 33 | 11.002 | 15.159 | 10.480 | 13.666 | 5.671 | 4.217 | 4.912 | 5.792 | 7.144 | 4.613 | 6.539 | 6.734 | 9.267 | 5.062 | 8.316 | 8.626 |

Table D20: IEC Simulated Results for Case 1 at $\mathbf{1 0 \%}$ penetration level and DG located at Bus $\mathbf{7}$

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.559 | 12.825 | 9.299 | 12.112 | 10.545 | 12.789 | 9.288 | 12.072 | 10.567 | 12.809 | 9.306 | 12.094 | 10.577 | 12.819 | 9.315 | 12.103 |
| 2 | 132 | 10.082 | 11.048 | 8.814 | 10.701 | 10.058 | 10.949 | 8.793 | 10.623 | 10.097 | 10.979 | 8.827 | 10.662 | 10.117 | 10.994 | 8.844 | 10.679 |
| 3 | 132 | 6.153 | 6.124 | 5.348 | 6.190 | 6.139 | 6.053 | 5.336 | 6.149 | 6.163 | 6.068 | 5.356 | 6.171 | 6.174 | 6.075 | 5.366 | 6.181 |
| 4 | 132 | 8.170 | 7.900 | 7.105 | 8.156 | 8.141 | 7.745 | 7.080 | 8.076 | 8.191 | 7.775 | 7.122 | 8.124 | 8.215 | 7.790 | 7.144 | 8.147 |
| 5 | 132 | 7.546 | 7.181 | 6.565 | 7.452 | 7.506 | 6.971 | 6.531 | 7.340 | 7.573 | 7.009 | 6.589 | 7.406 | 7.607 | 7.029 | 6.619 | 7.436 |
| 6 | 132 | 9.577 | 9.216 | 8.333 | 9.527 | 9.519 | 8.890 | 8.283 | 9.370 | 9.622 | 8.949 | 8.372 | 9.476 | 9.676 | 8.981 | 8.420 | 9.526 |
| 7 | 132 | 6.325 | 6.331 | 5.489 | 6.372 | 6.215 | 5.712 | 5.393 | 6.009 | 6.427 | 5.830 | 5.577 | 6.235 | 6.546 | 5.897 | 5.683 | 6.351 |
| 8 | 132 | 7.160 | 7.105 | 6.233 | 7.186 | 7.135 | 6.969 | 6.212 | 7.113 | 7.178 | 6.996 | 6.249 | 7.156 | 7.199 | 7.010 | 6.268 | 7.175 |
| 9 | 33 | 15.988 | 16.092 | 13.890 | 16.259 | 15.972 | 16.082 | 13.877 | 16.253 | 16.003 | 16.102 | 13.903 | 16.271 | 16.019 | 16.113 | 13.918 | 16.283 |
| 10 | 33 | 19.227 | 18.037 | 16.683 | 19.029 | 19.210 | 18.028 | 16.669 | 19.021 | 19.241 | 18.046 | 16.695 | 19.040 | 19.258 | 18.056 | 16.710 | 19.053 |
| 11 | 11 | 23.035 | 27.526 | 20.069 | 26.200 | 23.028 | 27.520 | 20.063 | 26.197 | 23.043 | 27.533 | 20.075 | 26.206 | 23.051 | 27.541 | 20.082 | 26.212 |
| 12 | 33 | 16.126 | 15.077 | 14.001 | 15.914 | 16.116 | 15.072 | 13.993 | 15.909 | 16.134 | 15.082 | 14.008 | 15.921 | 16.143 | 15.088 | 14.016 | 15.928 |
| 13 | 11 | 25.527 | 30.855 | 22.192 | 29.812 | 25.520 | 30.849 | 22.187 | 29.808 | 25.533 | 30.860 | 22.197 | 29.817 | 25.539 | 30.867 | 22.203 | 29.822 |
| 14 | 33 | 8.259 | 7.711 | 7.157 | 8.058 | 8.256 | 7.709 | 7.154 | 8.056 | 8.260 | 7.712 | 7.158 | 8.059 | 8.262 | 7.713 | 7.160 | 8.061 |
| 15 | 33 | 13.089 | 11.941 | 11.347 | 12.687 | 13.082 | 11.938 | 11.341 | 12.683 | 13.094 | 11.944 | 11.351 | 12.691 | 13.099 | 11.947 | 11.356 | 12.696 |
| 16 | 33 | 10.241 | 9.725 | 8.877 | 10.107 | 10.237 | 9.722 | 8.873 | 10.105 | 10.245 | 9.727 | 8.880 | 10.110 | 10.248 | 9.729 | 8.883 | 10.113 |
| 17 | 33 | 13.397 | 12.514 | 11.614 | 13.138 | 13.389 | 12.509 | 11.607 | 13.134 | 13.403 | 12.517 | 11.619 | 13.143 | 13.410 | 12.522 | 11.626 | 13.149 |
| 18 | 33 | 8.671 | 7.980 | 7.512 | 8.386 | 8.668 | 7.979 | 7.509 | 8.384 | 8.672 | 7.981 | 7.513 | 8.387 | 8.675 | 7.983 | 7.515 | 8.389 |
| 19 | 33 | 9.164 | 8.317 | 7.939 | 8.821 | 9.161 | 8.315 | 7.937 | 8.818 | 9.166 | 8.318 | 7.941 | 8.823 | 9.169 | 8.320 | 7.943 | 8.825 |
| 20 | 33 | 9.510 | 8.768 | 8.240 | 9.210 | 9.506 | 8.766 | 8.237 | 9.208 | 9.513 | 8.769 | 8.242 | 9.212 | 9.516 | 8.771 | 8.245 | 9.215 |
| 21 | 33 | 15.422 | 14.109 | 13.370 | 14.959 | 15.411 | 14.103 | 13.361 | 14.953 | 15.430 | 14.113 | 13.377 | 14.966 | 15.439 | 14.119 | 13.385 | 14.973 |
| 22 | 33 | 14.969 | 13.811 | 12.977 | 14.596 | 14.959 | 13.805 | 12.968 | 14.591 | 14.977 | 13.815 | 12.983 | 14.603 | 14.986 | 13.820 | 12.991 | 14.610 |
| 23 | 33 | 8.475 | 7.937 | 7.343 | 8.264 | 8.472 | 7.935 | 7.340 | 8.263 | 8.477 | 7.938 | 7.344 | 8.266 | 8.479 | 7.939 | 7.346 | 8.268 |
| 24 | 33 | 10.907 | 10.075 | 9.449 | 10.551 | 10.901 | 10.072 | 9.445 | 10.548 | 10.910 | 10.077 | 9.452 | 10.554 | 10.914 | 10.079 | 9.456 | 10.557 |
| 25 | 33 | 6.941 | 6.721 | 6.013 | 6.879 | 6.938 | 6.720 | 6.011 | 6.877 | 6.943 | 6.722 | 6.015 | 6.880 | 6.945 | 6.724 | 6.017 | 6.882 |
| 26 | 33 | 3.060 | 2.870 | 2.651 | 3.017 | 3.060 | 2.870 | 2.650 | 3.017 | 3.061 | 2.870 | 2.651 | 3.018 | 3.061 | 2.870 | 2.651 | 3.018 |
| 27 | 33 | 7.997 | 7.913 | 6.929 | 8.099 | 7.993 | 7.911 | 6.926 | 8.098 | 8.000 | 7.915 | 6.932 | 8.102 | 8.004 | 7.918 | 6.936 | 8.105 |
| 28 | 132 | 5.371 | 5.146 | 4.662 | 5.306 | 5.354 | 5.051 | 4.648 | 5.259 | 5.383 | 5.068 | 4.673 | 5.288 | 5.397 | 5.077 | 4.686 | 5.301 |
| 29 | 33 | 4.081 | 3.799 | 3.535 | 3.977 | 4.080 | 3.799 | 3.534 | 3.976 | 4.082 | 3.800 | 3.535 | 3.978 | 4.082 | 3.800 | 3.536 | 3.978 |
| 30 | 33 | 4.282 | 3.751 | 3.709 | 4.148 | 4.282 | 3.751 | 3.708 | 4.147 | 4.283 | 3.752 | 3.710 | 4.148 | 4.284 | 3.752 | 3.710 | 4.149 |

Table D21: IEC Simulated Results for Case 2 at $\mathbf{1 0 \%}$ penetration level and DG located at Bus 26

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.551 | 12.794 | 9.292 | 12.081 | 10.547 | 12.790 | 9.289 | 12.077 | 10.553 | 12.796 | 9.294 | 12.083 | 10.555 | 12.798 | 9.296 | 12.085 |
| 2 | 132 | 10.064 | 10.953 | 8.798 | 10.636 | 10.057 | 10.948 | 8.793 | 10.629 | 10.067 | 10.956 | 8.801 | 10.639 | 10.071 | 10.959 | 8.804 | 10.642 |
| 3 | 132 | 6.145 | 6.057 | 5.341 | 6.158 | 6.140 | 6.054 | 5.336 | 6.152 | 6.149 | 6.059 | 5.344 | 6.161 | 6.152 | 6.061 | 5.347 | 6.164 |
| 4 | 132 | 8.152 | 7.752 | 7.089 | 8.095 | 8.142 | 7.746 | 7.080 | 8.082 | 8.160 | 7.757 | 7.096 | 8.101 | 8.168 | 7.762 | 7.103 | 8.108 |
| 5 | 132 | 7.499 | 6.968 | 6.525 | 7.350 | 7.497 | 6.966 | 6.523 | 7.347 | 7.500 | 6.968 | 6.526 | 7.351 | 7.502 | 6.969 | 6.527 | 7.352 |
| 6 | 132 | 9.532 | 8.898 | 8.294 | 9.404 | 9.514 | 8.887 | 8.279 | 9.380 | 9.548 | 8.907 | 8.308 | 9.417 | 9.563 | 8.916 | 8.321 | 9.431 |
| 7 | 132 | 6.141 | 5.671 | 5.329 | 6.000 | 6.136 | 5.668 | 5.325 | 5.995 | 6.144 | 5.672 | 5.331 | 6.002 | 6.147 | 5.674 | 5.334 | 6.005 |
| 8 | 132 | 7.146 | 6.976 | 6.222 | 7.132 | 7.137 | 6.970 | 6.214 | 7.120 | 7.154 | 6.981 | 6.229 | 7.138 | 7.162 | 6.986 | 6.235 | 7.145 |
| 9 | 33 | 15.997 | 16.135 | 13.898 | 16.268 | 15.973 | 16.083 | 13.878 | 16.259 | 16.013 | 16.109 | 13.912 | 16.285 | 16.029 | 16.120 | 13.926 | 16.299 |
| 10 | 33 | 19.268 | 18.171 | 16.718 | 19.055 | 19.209 | 18.029 | 16.668 | 19.040 | 19.299 | 18.080 | 16.745 | 19.106 | 19.332 | 18.100 | 16.774 | 19.136 |
| 11 | 11 | 23.040 | 27.531 | 20.073 | 26.207 | 23.029 | 27.521 | 20.064 | 26.201 | 23.048 | 27.538 | 20.080 | 26.214 | 23.056 | 27.546 | 20.087 | 26.221 |
| 12 | 33 | 16.137 | 15.123 | 14.011 | 15.913 | 16.113 | 15.070 | 13.990 | 15.913 | 16.149 | 15.091 | 14.021 | 15.940 | 16.162 | 15.099 | 14.032 | 15.952 |
| 13 | 11 | 25.536 | 30.864 | 22.200 | 29.823 | 25.520 | 30.849 | 22.187 | 29.813 | 25.545 | 30.872 | 22.208 | 29.832 | 25.554 | 30.881 | 22.216 | 29.841 |
| 14 | 33 | 8.262 | 7.726 | 7.159 | 8.054 | 8.253 | 7.708 | 7.152 | 8.056 | 8.265 | 7.715 | 7.162 | 8.065 | 8.268 | 7.717 | 7.165 | 8.069 |
| 15 | 33 | 13.110 | 12.009 | 11.365 | 12.701 | 13.084 | 11.939 | 11.343 | 12.694 | 13.123 | 11.960 | 11.376 | 12.722 | 13.136 | 11.968 | 11.388 | 12.734 |
| 16 | 33 | 10.247 | 9.748 | 8.882 | 10.105 | 10.235 | 9.721 | 8.871 | 10.106 | 10.252 | 9.731 | 8.886 | 10.120 | 10.258 | 9.735 | 8.891 | 10.125 |
| 17 | 33 | 13.410 | 12.566 | 11.626 | 13.139 | 13.385 | 12.508 | 11.604 | 13.139 | 13.422 | 12.529 | 11.636 | 13.166 | 13.435 | 12.536 | 11.647 | 13.178 |
| 18 | 33 | 8.676 | 8.005 | 7.517 | 8.386 | 8.666 | 7.978 | 7.508 | 8.386 | 8.681 | 7.986 | 7.521 | 8.397 | 8.686 | 7.989 | 7.525 | 8.402 |
| 19 | 33 | 9.170 | 8.343 | 7.944 | 8.848 | 9.159 | 8.314 | 7.935 | 8.813 | 9.174 | 8.323 | 7.948 | 8.826 | 9.179 | 8.326 | 7.953 | 8.830 |
| 20 | 33 | 9.517 | 8.796 | 8.246 | 9.209 | 9.504 | 8.765 | 8.235 | 9.210 | 9.522 | 8.775 | 8.250 | 9.224 | 9.528 | 8.778 | 8.256 | 9.230 |
| 21 | 33 | 15.471 | 14.254 | 13.413 | 14.997 | 15.416 | 14.106 | 13.365 | 14.979 | 15.500 | 14.153 | 13.438 | 15.040 | 15.531 | 14.170 | 13.465 | 15.067 |
| 22 | 33 | 15.028 | 13.976 | 13.028 | 14.647 | 14.968 | 13.811 | 12.976 | 14.622 | 15.060 | 13.862 | 13.056 | 14.689 | 15.095 | 13.882 | 13.086 | 14.720 |
| 23 | 33 | 8.508 | 8.028 | 7.371 | 8.301 | 8.482 | 7.941 | 7.349 | 8.283 | 8.524 | 7.965 | 7.385 | 8.312 | 8.540 | 7.975 | 7.399 | 8.326 |
| 24 | 33 | 11.068 | 10.459 | 9.589 | 10.827 | 10.970 | 10.111 | 9.505 | 10.658 | 11.139 | 10.206 | 9.650 | 10.767 | 11.210 | 10.246 | 9.713 | 10.826 |
| 25 | 33 | 7.469 | 7.881 | 6.470 | 7.747 | 7.251 | 6.919 | 6.281 | 7.288 | 7.697 | 7.176 | 6.667 | 7.537 | 7.923 | 7.310 | 6.870 | 7.712 |
| 26 | 33 | 3.841 | 4.690 | 3.326 | 4.753 | 3.596 | 3.172 | 3.114 | 3.560 | 4.232 | 3.472 | 3.664 | 4.035 | 4.632 | 3.659 | 4.030 | 4.449 |
| 27 | 33 | 8.227 | 8.422 | 7.129 | 8.424 | 8.097 | 7.983 | 7.016 | 8.262 | 8.328 | 8.128 | 7.216 | 8.410 | 8.429 | 8.193 | 7.306 | 8.495 |
| 28 | 132 | 5.381 | 5.067 | 4.671 | 5.287 | 5.369 | 5.060 | 4.661 | 5.270 | 5.393 | 5.074 | 4.682 | 5.298 | 5.405 | 5.081 | 4.693 | 5.309 |
| 29 | 33 | 4.119 | 3.895 | 3.568 | 4.060 | 4.088 | 3.803 | 3.541 | 3.968 | 4.136 | 3.831 | 3.583 | 4.014 | 4.155 | 3.842 | 3.599 | 4.029 |
| 30 | 33 | 4.315 | 3.840 | 3.737 | 4.220 | 4.287 | 3.753 | 3.713 | 4.139 | 4.330 | 3.775 | 3.751 | 4.180 | 4.347 | 3.783 | 3.765 | 4.193 |

Table D22: IEC Simulated Results for Case 3 at 10\% penetration level and DG located at Bus 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.552 | 12.795 | 9.293 | 12.082 | 10.547 | 12.791 | 9.289 | 12.077 | 10.555 | 12.798 | 9.295 | 12.085 | 10.558 | 12.801 | 9.298 | 12.087 |
| 2 | 132 | 10.066 | 10.955 | 8.800 | 10.638 | 10.058 | 10.949 | 8.794 | 10.629 | 10.071 | 10.959 | 8.804 | 10.642 | 10.076 | 10.962 | 8.808 | 10.646 |
| 3 | 132 | 6.147 | 6.058 | 5.342 | 6.160 | 6.141 | 6.054 | 5.337 | 6.152 | 6.151 | 6.061 | 5.346 | 6.163 | 6.156 | 6.064 | 5.350 | 6.167 |
| 4 | 132 | 8.156 | 7.754 | 7.092 | 8.098 | 8.144 | 7.747 | 7.082 | 8.082 | 8.166 | 7.760 | 7.101 | 8.106 | 8.176 | 7.766 | 7.110 | 8.115 |
| 5 | 132 | 7.500 | 6.968 | 6.525 | 7.350 | 7.497 | 6.966 | 6.523 | 7.347 | 7.502 | 6.969 | 6.527 | 7.352 | 7.504 | 6.970 | 6.528 | 7.353 |
| 6 | 132 | 9.544 | 8.905 | 8.304 | 9.414 | 9.521 | 8.891 | 8.285 | 9.384 | 9.565 | 8.917 | 8.323 | 9.432 | 9.585 | 8.929 | 8.341 | 9.452 |
| 7 | 132 | 6.143 | 5.672 | 5.330 | 6.002 | 6.138 | 5.669 | 5.326 | 5.995 | 6.147 | 5.674 | 5.334 | 6.005 | 6.151 | 5.677 | 5.338 | 6.009 |
| 8 | 132 | 7.154 | 6.981 | 6.228 | 7.138 | 7.141 | 6.973 | 6.218 | 7.121 | 7.165 | 6.988 | 6.238 | 7.147 | 7.176 | 6.995 | 6.247 | 7.157 |
| 9 | 33 | 15.988 | 16.104 | 13.890 | 16.255 | 15.971 | 16.081 | 13.875 | 16.253 | 16.001 | 16.101 | 13.901 | 16.273 | 16.014 | 16.110 | 13.913 | 16.283 |
| 10 | 33 | 19.239 | 18.079 | 16.693 | 19.022 | 19.203 | 18.025 | 16.663 | 19.023 | 19.258 | 18.056 | 16.710 | 19.064 | 19.280 | 18.069 | 16.729 | 19.082 |
| 11 | 11 | 23.036 | 27.526 | 20.069 | 26.201 | 23.027 | 27.519 | 20.062 | 26.198 | 23.042 | 27.532 | 20.074 | 26.207 | 23.048 | 27.539 | 20.080 | 26.213 |
| 12 | 33 | 16.128 | 15.090 | 14.003 | 15.907 | 16.112 | 15.070 | 13.989 | 15.908 | 16.136 | 15.084 | 14.010 | 15.926 | 16.145 | 15.089 | 14.018 | 15.934 |
| 13 | 11 | 25.529 | 30.857 | 22.194 | 29.815 | 25.518 | 30.847 | 22.185 | 29.808 | 25.535 | 30.863 | 22.200 | 29.821 | 25.542 | 30.869 | 22.205 | 29.827 |
| 14 | 33 | 8.259 | 7.715 | 7.157 | 8.054 | 8.254 | 7.708 | 7.153 | 8.055 | 8.261 | 7.712 | 7.159 | 8.061 | 8.263 | 7.714 | 7.161 | 8.063 |
| 15 | 33 | 13.096 | 11.964 | 11.353 | 12.685 | 13.080 | 11.937 | 11.339 | 12.685 | 13.103 | 11.949 | 11.359 | 12.702 | 13.111 | 11.954 | 11.366 | 12.710 |
| 16 | 33 | 10.242 | 9.731 | 8.878 | 10.103 | 10.235 | 9.721 | 8.871 | 10.104 | 10.246 | 9.728 | 8.881 | 10.113 | 10.250 | 9.730 | 8.885 | 10.117 |
| 17 | 33 | 13.400 | 12.529 | 11.617 | 13.131 | 13.385 | 12.507 | 11.604 | 13.134 | 13.408 | 12.520 | 11.623 | 13.151 | 13.416 | 12.525 | 11.631 | 13.158 |
| 18 | 33 | 8.672 | 7.988 | 7.513 | 8.382 | 8.666 | 7.978 | 7.508 | 8.384 | 8.675 | 7.983 | 7.516 | 8.391 | 8.678 | 7.984 | 7.518 | 8.394 |
| 19 | 33 | 9.165 | 8.325 | 7.941 | 8.832 | 9.159 | 8.314 | 7.935 | 8.815 | 9.168 | 8.319 | 7.943 | 8.823 | 9.171 | 8.321 | 7.946 | 8.825 |
| 20 | 33 | 9.512 | 8.776 | 8.241 | 9.206 | 9.504 | 8.765 | 8.235 | 9.208 | 9.515 | 8.771 | 8.244 | 9.216 | 9.519 | 8.773 | 8.248 | 9.220 |
| 21 | 33 | 15.438 | 14.157 | 13.384 | 14.958 | 15.406 | 14.100 | 13.356 | 14.958 | 15.453 | 14.126 | 13.397 | 14.993 | 15.471 | 14.136 | 13.412 | 15.009 |
| 22 | 33 | 14.988 | 13.866 | 12.993 | 14.599 | 14.954 | 13.802 | 12.964 | 14.597 | 15.005 | 13.831 | 13.008 | 14.635 | 15.024 | 13.842 | 13.024 | 14.652 |
| 23 | 33 | 8.486 | 7.969 | 7.352 | 8.270 | 8.471 | 7.934 | 7.339 | 8.267 | 8.493 | 7.947 | 7.358 | 8.283 | 8.501 | 7.952 | 7.365 | 8.290 |
| 24 | 33 | 10.958 | 10.212 | 9.493 | 10.658 | 10.903 | 10.073 | 9.447 | 10.571 | 10.986 | 10.120 | 9.518 | 10.631 | 11.017 | 10.137 | 9.545 | 10.659 |
| 25 | 33 | 7.097 | 7.117 | 6.148 | 7.125 | 6.979 | 6.747 | 6.046 | 6.968 | 7.173 | 6.865 | 6.213 | 7.101 | 7.253 | 6.914 | 6.284 | 7.169 |
| 26 | 33 | 3.081 | 2.932 | 2.669 | 3.071 | 3.060 | 2.869 | 2.650 | 3.008 | 3.092 | 2.888 | 2.678 | 3.038 | 3.104 | 2.895 | 2.689 | 3.047 |
| 27 | 33 | 8.472 | 9.102 | 7.341 | 8.945 | 8.194 | 8.053 | 7.101 | 8.422 | 8.699 | 8.360 | 7.537 | 8.744 | 8.934 | 8.507 | 7.747 | 8.933 |
| 28 | 132 | 5.400 | 5.078 | 4.688 | 5.304 | 5.383 | 5.068 | 4.674 | 5.278 | 5.421 | 5.090 | 4.706 | 5.323 | 5.441 | 5.102 | 4.724 | 5.342 |
| 29 | 33 | 4.857 | 5.762 | 4.207 | 5.756 | 4.524 | 4.056 | 3.919 | 4.505 | 5.258 | 4.412 | 4.553 | 4.961 | 5.678 | 4.614 | 4.935 | 5.380 |
| 30 | 33 | 4.580 | 4.542 | 3.967 | 4.635 | 4.422 | 3.819 | 3.830 | 4.184 | 4.720 | 3.965 | 4.088 | 4.495 | 4.864 | 4.034 | 4.217 | 4.628 |

Table D23: IEC Simulated Results for Case 4 at $\mathbf{1 0 \%}$ penetration level and DG located at Bus 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.551 | 12.794 | 9.292 | 9.292 | 10.546 | 12.790 | 9.288 | 12.076 | 10.553 | 12.796 | 9.294 | 12.083 | 10.556 | 12.798 | 9.296 | 12.085 |
| 2 | 132 | 10.063 | 10.953 | 8.798 | 8.798 | 10.057 | 10.948 | 8.792 | 10.629 | 10.067 | 10.956 | 8.801 | 10.639 | 10.072 | 10.959 | 8.805 | 10.643 |
| 3 | 132 | 6.145 | 6.057 | 5.340 | 5.340 | 6.139 | 6.053 | 5.336 | 6.152 | 6.148 | 6.059 | 5.343 | 6.161 | 6.152 | 6.061 | 5.347 | 6.164 |
| 4 | 132 | 8.151 | 7.751 | 7.088 | 7.088 | 8.140 | 7.745 | 7.079 | 8.080 | 8.159 | 7.756 | 7.095 | 8.100 | 8.168 | 7.761 | 7.102 | 8.108 |
| 5 | 132 | 7.499 | 6.968 | 6.525 | 6.525 | 7.497 | 6.966 | 6.522 | 7.347 | 7.501 | 6.968 | 6.526 | 7.351 | 7.502 | 6.969 | 6.527 | 7.352 |
| 6 | 132 | 9.533 | 8.899 | 8.295 | 8.295 | 9.512 | 8.886 | 8.277 | 9.378 | 9.551 | 8.909 | 8.310 | 9.420 | 9.568 | 8.919 | 8.326 | 9.436 |
| 7 | 132 | 6.141 | 5.671 | 5.329 | 5.329 | 6.136 | 5.668 | 5.325 | 5.995 | 6.144 | 5.673 | 5.332 | 6.003 | 6.148 | 5.675 | 5.335 | 6.006 |
| 8 | 132 | 7.148 | 6.978 | 6.223 | 6.223 | 7.137 | 6.970 | 6.214 | 7.119 | 7.157 | 6.983 | 6.231 | 7.141 | 7.167 | 6.989 | 6.239 | 7.149 |
| 9 | 33 | 15.982 | 16.099 | 13.885 | 13.885 | 15.966 | 16.078 | 13.871 | 16.248 | 15.993 | 16.095 | 13.894 | 16.265 | 16.003 | 16.102 | 13.904 | 16.274 |
| 10 | 33 | 19.229 | 18.071 | 16.685 | 16.685 | 19.198 | 18.022 | 16.658 | 19.016 | 19.245 | 18.049 | 16.699 | 19.052 | 19.262 | 18.059 | 16.714 | 19.067 |
| 11 | 11 | 23.032 | 27.524 | 20.066 | 20.066 | 23.025 | 27.517 | 20.060 | 26.195 | 23.038 | 27.528 | 20.071 | 26.204 | 23.043 | 27.534 | 20.075 | 26.208 |
| 12 | 33 | 16.124 | 15.087 | 13.999 | 13.999 | 16.110 | 15.069 | 13.988 | 15.905 | 16.130 | 15.080 | 14.005 | 15.921 | 16.138 | 15.085 | 14.012 | 15.928 |
| 13 | 11 | 25.526 | 30.854 | 22.192 | 22.192 | 25.517 | 30.845 | 22.184 | 29.806 | 25.531 | 30.859 | 22.196 | 29.817 | 25.536 | 30.864 | 22.201 | 29.822 |
| 14 | 33 | 8.258 | 7.714 | 7.156 | 7.156 | 8.254 | 7.708 | 7.152 | 8.055 | 8.260 | 7.712 | 7.158 | 8.060 | 8.262 | 7.713 | 7.159 | 8.062 |
| 15 | 33 | 13.092 | 11.960 | 11.350 | 11.350 | 13.079 | 11.936 | 11.338 | 12.683 | 13.098 | 11.946 | 11.355 | 12.698 | 13.105 | 11.950 | 11.360 | 12.704 |
| 16 | 33 | 10.241 | 9.730 | 8.876 | 8.876 | 10.234 | 9.721 | 8.871 | 10.103 | 10.244 | 9.726 | 8.879 | 10.111 | 10.247 | 9.728 | 8.882 | 10.114 |
| 17 | 33 | 13.396 | 12.526 | 11.614 | 11.614 | 13.383 | 12.506 | 11.602 | 13.131 | 13.402 | 12.517 | 11.619 | 13.146 | 13.409 | 12.521 | 11.625 | 13.152 |
| 18 | 33 | 8.671 | 7.987 | 7.512 | 7.512 | 8.666 | 7.978 | 7.508 | 8.383 | 8.673 | 7.982 | 7.514 | 8.389 | 8.675 | 7.983 | 7.516 | 8.391 |
| 19 | 33 | 9.164 | 8.323 | 7.939 | 7.939 | 9.158 | 8.314 | 7.935 | 8.815 | 9.166 | 8.318 | 7.941 | 8.822 | 9.169 | 8.320 | 7.944 | 8.823 |
| 20 | 33 | 9.510 | 8.775 | 8.240 | 8.240 | 9.504 | 8.764 | 8.234 | 9.207 | 9.513 | 8.770 | 8.242 | 9.214 | 9.516 | 8.771 | 8.245 | 9.217 |
| 21 | 33 | 15.430 | 14.149 | 13.377 | 13.377 | 15.403 | 14.099 | 13.354 | 14.952 | 15.443 | 14.121 | 13.388 | 14.983 | 15.457 | 14.128 | 13.400 | 14.996 |
| 22 | 33 | 14.980 | 13.858 | 12.986 | 12.986 | 14.950 | 13.800 | 12.961 | 14.591 | 14.994 | 13.825 | 12.998 | 14.625 | 15.009 | 13.833 | 13.011 | 14.639 |
| 23 | 33 | 8.483 | 7.965 | 7.349 | 7.349 | 8.470 | 7.934 | 7.338 | 8.264 | 8.488 | 7.944 | 7.354 | 8.279 | 8.495 | 7.948 | 7.359 | 8.285 |
| 24 | 33 | 10.944 | 10.196 | 9.482 | 9.482 | 10.897 | 10.069 | 9.441 | 10.561 | 10.967 | 10.109 | 9.501 | 10.614 | 10.992 | 10.123 | 9.523 | 10.637 |
| 25 | 33 | 7.061 | 7.071 | 6.117 | 6.117 | 6.957 | 6.733 | 6.027 | 6.940 | 7.121 | 6.833 | 6.169 | 7.057 | 7.187 | 6.874 | 6.227 | 7.113 |
| 26 | 33 | 3.076 | 2.925 | 2.664 | 2.664 | 3.058 | 2.868 | 2.648 | 3.008 | 3.085 | 2.884 | 2.672 | 3.032 | 3.095 | 2.890 | 2.680 | 3.040 |
| 27 | 33 | 8.367 | 8.955 | 7.250 | 7.250 | 8.121 | 8.003 | 7.037 | 8.333 | 8.547 | 8.267 | 7.406 | 8.617 | 8.736 | 8.387 | 7.575 | 8.773 |
| 28 | 132 | 5.390 | 5.072 | 4.679 | 4.679 | 5.374 | 5.062 | 4.665 | 5.271 | 5.407 | 5.082 | 4.694 | 5.310 | 5.424 | 5.092 | 4.709 | 5.326 |
| 29 | 33 | 4.350 | 4.563 | 3.767 | 3.767 | 4.197 | 3.867 | 3.635 | 4.113 | 4.478 | 4.020 | 3.878 | 4.288 | 4.611 | 4.093 | 3.998 | 4.405 |
| 30 | 33 | 5.056 | 5.891 | 4.378 | 4.378 | 4.697 | 3.957 | 4.068 | 4.522 | 5.459 | 4.290 | 4.727 | 5.131 | 5.885 | 4.471 | 5.115 | 5.553 |

Table D24: IEC Simulated Results for Case 5 at $\mathbf{1 0 \%}$ penetration level and DG located at Bus 7 and 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.562 | 12.827 | 9.301 | 12.114 | 10.545 | 12.789 | 9.287 | 12.074 | 10.561 | 12.804 | 9.301 | 12.089 | 10.571 | 12.813 | 9.309 | 12.098 |
| 2 | 132 | 10.085 | 11.051 | 8.817 | 10.704 | 10.056 | 10.948 | 8.792 | 10.624 | 10.085 | 10.969 | 8.816 | 10.652 | 10.103 | 10.984 | 8.832 | 10.668 |
| 3 | 132 | 6.158 | 6.127 | 5.352 | 6.194 | 6.139 | 6.053 | 5.335 | 6.149 | 6.158 | 6.065 | 5.351 | 6.168 | 6.170 | 6.073 | 5.362 | 6.178 |
| 4 | 132 | 8.181 | 7.907 | 7.114 | 8.164 | 8.140 | 7.745 | 7.079 | 8.076 | 8.180 | 7.769 | 7.113 | 8.116 | 8.207 | 7.785 | 7.137 | 8.140 |
| 5 | 132 | 7.539 | 7.177 | 6.559 | 7.447 | 7.500 | 6.968 | 6.525 | 7.342 | 7.538 | 6.989 | 6.558 | 7.379 | 7.563 | 7.004 | 6.580 | 7.401 |
| 6 | 132 | 9.601 | 9.230 | 8.353 | 9.547 | 9.515 | 8.888 | 8.280 | 9.372 | 9.598 | 8.936 | 8.351 | 9.457 | 9.655 | 8.969 | 8.402 | 9.509 |
| 7 | 132 | 6.295 | 6.311 | 5.462 | 6.345 | 6.171 | 5.687 | 5.355 | 5.997 | 6.288 | 5.753 | 5.456 | 6.119 | 6.373 | 5.802 | 5.532 | 6.199 |
| 8 | 132 | 7.174 | 7.115 | 6.246 | 7.198 | 7.136 | 6.970 | 6.213 | 7.115 | 7.174 | 6.993 | 6.245 | 7.153 | 7.199 | 7.009 | 6.267 | 7.176 |
| 9 | 33 | 16.005 | 16.114 | 13.905 | 16.271 | 15.969 | 16.080 | 13.874 | 16.251 | 16.005 | 16.103 | 13.904 | 16.275 | 16.028 | 16.119 | 13.925 | 16.293 |
| 10 | 33 | 19.253 | 18.082 | 16.706 | 19.040 | 19.202 | 18.024 | 16.662 | 19.019 | 19.253 | 18.053 | 16.706 | 19.056 | 19.284 | 18.071 | 16.733 | 19.082 |
| 11 | 11 | 23.044 | 27.534 | 20.079 | 26.209 | 23.026 | 27.518 | 20.061 | 26.197 | 23.044 | 27.534 | 20.076 | 26.208 | 23.055 | 27.545 | 20.086 | 26.218 |
| 12 | 33 | 16.137 | 15.093 | 14.010 | 15.917 | 16.112 | 15.070 | 13.989 | 15.907 | 16.136 | 15.084 | 14.010 | 15.925 | 16.151 | 15.092 | 14.023 | 15.938 |
| 13 | 11 | 25.535 | 30.863 | 22.200 | 29.821 | 25.518 | 30.847 | 22.185 | 29.807 | 25.535 | 30.863 | 22.199 | 29.821 | 25.546 | 30.873 | 22.209 | 29.830 |
| 14 | 33 | 8.261 | 7.715 | 7.158 | 8.056 | 8.254 | 7.709 | 7.153 | 8.055 | 8.261 | 7.712 | 7.159 | 8.060 | 8.264 | 7.714 | 7.162 | 8.064 |
| 15 | 33 | 13.099 | 11.962 | 11.356 | 12.691 | 13.079 | 11.936 | 11.339 | 12.683 | 13.099 | 11.947 | 11.356 | 12.698 | 13.110 | 11.953 | 11.365 | 12.708 |
| 16 | 33 | 10.246 | 9.732 | 8.881 | 10.107 | 10.235 | 9.721 | 8.871 | 10.104 | 10.246 | 9.727 | 8.881 | 10.112 | 10.252 | 9.731 | 8.886 | 10.118 |
| 17 | 33 | 13.406 | 12.531 | 11.622 | 13.140 | 13.385 | 12.507 | 11.604 | 13.133 | 13.406 | 12.520 | 11.622 | 13.148 | 13.419 | 12.527 | 11.633 | 13.159 |
| 18 | 33 | 8.674 | 7.988 | 7.515 | 8.385 | 8.666 | 7.978 | 7.508 | 8.383 | 8.674 | 7.982 | 7.515 | 8.390 | 8.678 | 7.985 | 7.519 | 8.393 |
| 19 | 33 | 9.167 | 8.325 | 7.942 | 8.832 | 9.159 | 8.314 | 7.935 | 8.815 | 9.167 | 8.319 | 7.942 | 8.823 | 9.172 | 8.322 | 7.946 | 8.826 |
| 20 | 33 | 9.514 | 8.776 | 8.244 | 9.210 | 9.504 | 8.765 | 8.235 | 9.207 | 9.514 | 8.770 | 8.244 | 9.215 | 9.520 | 8.774 | 8.248 | 9.220 |
| 21 | 33 | 15.444 | 14.153 | 13.389 | 14.968 | 15.405 | 14.100 | 13.356 | 14.953 | 15.444 | 14.121 | 13.389 | 14.982 | 15.466 | 14.134 | 13.408 | 15.002 |
| 22 | 33 | 14.993 | 13.861 | 12.997 | 14.608 | 14.953 | 13.802 | 12.963 | 14.591 | 14.993 | 13.824 | 12.998 | 14.622 | 15.017 | 13.838 | 13.018 | 14.642 |
| 23 | 33 | 8.486 | 7.964 | 7.352 | 8.271 | 8.470 | 7.934 | 7.338 | 8.263 | 8.486 | 7.943 | 7.352 | 8.276 | 8.495 | 7.948 | 7.359 | 8.284 |
| 24 | 33 | 10.951 | 10.187 | 9.488 | 10.632 | 10.897 | 10.069 | 9.441 | 10.555 | 10.952 | 10.100 | 9.488 | 10.597 | 10.983 | 10.118 | 9.515 | 10.625 |
| 25 | 33 | 7.066 | 7.034 | 6.121 | 7.055 | 6.947 | 6.726 | 6.018 | 6.915 | 7.069 | 6.801 | 6.123 | 7.003 | 7.142 | 6.847 | 6.188 | 7.066 |
| 26 | 33 | 3.078 | 2.919 | 2.665 | 3.059 | 3.058 | 2.868 | 2.648 | 3.010 | 3.078 | 2.880 | 2.666 | 3.028 | 3.089 | 2.886 | 2.675 | 3.037 |
| 27 | 33 | 8.370 | 8.826 | 7.252 | 8.770 | 8.068 | 7.965 | 6.991 | 8.244 | 8.376 | 8.158 | 7.258 | 8.451 | 8.582 | 8.290 | 7.441 | 8.619 |
| 28 | 132 | 5.407 | 5.168 | 4.694 | 5.337 | 5.366 | 5.058 | 4.658 | 5.265 | 5.406 | 5.082 | 4.693 | 5.308 | 5.435 | 5.099 | 4.719 | 5.335 |
| 29 | 33 | 4.661 | 5.172 | 4.037 | 5.163 | 4.272 | 3.910 | 3.700 | 4.199 | 4.671 | 4.122 | 4.045 | 4.463 | 4.986 | 4.288 | 4.328 | 4.769 |
| 30 | 33 | 4.513 | 4.344 | 3.909 | 4.494 | 4.337 | 3.777 | 3.756 | 4.148 | 4.517 | 3.868 | 3.912 | 4.332 | 4.641 | 3.930 | 4.022 | 4.444 |

Table D25: IEC Simulated Results for Case 6 at 10\% penetration level and DG located at Bus 26 and 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.554 | 12.796 | 9.294 | 12.083 | 10.546 | 12.789 | 9.288 | 12.076 | 10.554 | 12.797 | 9.294 | 12.083 | 10.558 | 12.801 | 9.298 | 12.087 |
| 2 | 132 | 10.068 | 10.957 | 8.802 | 10.640 | 10.056 | 10.947 | 8.792 | 10.628 | 10.069 | 10.957 | 8.802 | 10.640 | 10.076 | 10.962 | 8.808 | 10.646 |
| 3 | 132 | 6.150 | 6.060 | 5.344 | 6.161 | 6.139 | 6.053 | 5.335 | 6.151 | 6.150 | 6.060 | 5.345 | 6.162 | 6.156 | 6.064 | 5.350 | 6.167 |
| 4 | 132 | 8.162 | 7.758 | 7.098 | 8.102 | 8.139 | 7.744 | 7.078 | 8.079 | 8.163 | 7.758 | 7.098 | 8.103 | 8.177 | 7.767 | 7.111 | 8.115 |
| 5 | 132 | 7.501 | 6.968 | 6.526 | 7.351 | 7.496 | 6.966 | 6.522 | 7.347 | 7.501 | 6.969 | 6.526 | 7.351 | 7.503 | 6.970 | 6.528 | 7.353 |
| 6 | 132 | 9.554 | 8.911 | 8.313 | 9.422 | 9.510 | 8.885 | 8.275 | 9.375 | 9.555 | 8.911 | 8.314 | 9.423 | 9.584 | 8.928 | 8.340 | 9.449 |
| 7 | 132 | 6.145 | 5.673 | 5.332 | 6.003 | 6.136 | 5.668 | 5.324 | 5.994 | 6.145 | 5.673 | 5.332 | 6.003 | 6.151 | 5.676 | 5.337 | 6.008 |
| 8 | 132 | 7.158 | 6.984 | 6.232 | 7.141 | 7.135 | 6.969 | 6.212 | 7.117 | 7.159 | 6.984 | 6.233 | 7.142 | 7.173 | 6.994 | 6.246 | 7.155 |
| 9 | 33 | 16.006 | 16.141 | 13.906 | 16.276 | 15.966 | 16.078 | 13.871 | 16.251 | 16.007 | 16.105 | 13.907 | 16.280 | 16.031 | 16.121 | 13.928 | 16.300 |
| 10 | 33 | 19.278 | 18.177 | 16.727 | 19.064 | 19.195 | 18.021 | 16.656 | 19.023 | 19.280 | 18.069 | 16.729 | 19.087 | 19.325 | 18.096 | 16.768 | 19.128 |
| 11 | 11 | 23.045 | 27.535 | 20.077 | 26.211 | 23.025 | 27.517 | 20.060 | 26.197 | 23.045 | 27.536 | 20.077 | 26.211 | 23.057 | 27.547 | 20.088 | 26.222 |
| 12 | 33 | 16.142 | 15.126 | 14.015 | 15.918 | 16.108 | 15.068 | 13.986 | 15.907 | 16.143 | 15.087 | 14.016 | 15.934 | 16.161 | 15.098 | 14.031 | 15.950 |
| 13 | 11 | 25.540 | 30.867 | 22.203 | 29.827 | 25.516 | 30.845 | 22.183 | 29.808 | 25.540 | 30.868 | 22.204 | 29.828 | 25.553 | 30.880 | 22.215 | 29.840 |
| 14 | 33 | 8.263 | 7.726 | 7.160 | 8.055 | 8.252 | 7.707 | 7.151 | 8.054 | 8.263 | 7.714 | 7.160 | 8.063 | 8.268 | 7.716 | 7.164 | 8.068 |
| 15 | 33 | 13.112 | 12.011 | 11.367 | 12.703 | 13.078 | 11.936 | 11.338 | 12.686 | 13.113 | 11.955 | 11.368 | 12.713 | 13.131 | 11.965 | 11.384 | 12.730 |
| 16 | 33 | 10.249 | 9.749 | 8.883 | 10.107 | 10.233 | 9.720 | 8.870 | 10.104 | 10.249 | 9.729 | 8.884 | 10.117 | 10.257 | 9.734 | 8.891 | 10.124 |
| 17 | 33 | 13.414 | 12.568 | 11.629 | 13.143 | 13.381 | 12.505 | 11.600 | 13.133 | 13.415 | 12.525 | 11.630 | 13.159 | 13.432 | 12.535 | 11.645 | 13.176 |
| 18 | 33 | 8.678 | 8.006 | 7.518 | 8.387 | 8.664 | 7.977 | 7.507 | 8.384 | 8.678 | 7.985 | 7.518 | 8.394 | 8.684 | 7.988 | 7.524 | 8.400 |
| 19 | 33 | 9.171 | 8.343 | 7.945 | 8.849 | 9.157 | 8.313 | 7.933 | 8.812 | 9.171 | 8.321 | 7.946 | 8.824 | 9.178 | 8.325 | 7.952 | 8.829 |
| 20 | 33 | 9.518 | 8.797 | 8.247 | 9.210 | 9.502 | 8.764 | 8.233 | 9.207 | 9.519 | 8.773 | 8.247 | 9.220 | 9.527 | 8.777 | 8.254 | 9.228 |
| 21 | 33 | 15.477 | 14.257 | 13.417 | 15.002 | 15.402 | 14.098 | 13.353 | 14.961 | 15.478 | 14.140 | 13.419 | 15.019 | 15.518 | 14.163 | 13.454 | 15.055 |
| 22 | 33 | 15.033 | 13.979 | 13.032 | 14.652 | 14.951 | 13.801 | 12.961 | 14.602 | 15.035 | 13.848 | 13.033 | 14.665 | 15.079 | 13.873 | 13.072 | 14.706 |
| 23 | 33 | 8.509 | 8.029 | 7.372 | 8.302 | 8.472 | 7.935 | 7.340 | 8.271 | 8.510 | 7.957 | 7.373 | 8.299 | 8.530 | 7.969 | 7.390 | 8.317 |
| 24 | 33 | 11.067 | 10.458 | 9.588 | 10.825 | 10.921 | 10.083 | 9.462 | 10.603 | 11.070 | 10.167 | 9.591 | 10.708 | 11.157 | 10.217 | 9.667 | 10.782 |
| 25 | 33 | 7.449 | 7.868 | 6.453 | 7.733 | 7.075 | 6.809 | 6.129 | 7.100 | 7.459 | 7.037 | 6.461 | 7.344 | 7.720 | 7.194 | 6.693 | 7.552 |
| 26 | 33 | 3.653 | 4.180 | 3.164 | 4.191 | 3.297 | 3.005 | 2.855 | 3.229 | 3.662 | 3.198 | 3.171 | 3.531 | 3.969 | 3.359 | 3.448 | 3.840 |
| 27 | 33 | 8.472 | 9.091 | 7.341 | 8.949 | 8.077 | 7.973 | 6.999 | 8.279 | 8.482 | 8.226 | 7.349 | 8.559 | 8.742 | 8.390 | 7.580 | 8.776 |
| 28 | 132 | 5.405 | 5.081 | 4.692 | 5.307 | 5.369 | 5.059 | 4.661 | 5.267 | 5.406 | 5.081 | 4.693 | 5.308 | 5.431 | 5.097 | 4.716 | 5.332 |
| 29 | 33 | 4.319 | 4.435 | 3.741 | 4.380 | 4.127 | 3.826 | 3.574 | 4.025 | 4.323 | 3.936 | 3.744 | 4.159 | 4.452 | 4.008 | 3.859 | 4.272 |
| 30 | 33 | 4.888 | 5.298 | 4.233 | 5.270 | 4.460 | 3.838 | 3.863 | 4.240 | 4.898 | 4.047 | 4.242 | 4.651 | 5.233 | 4.202 | 4.542 | 4.971 |

Table D26: IEC Simulated Results for Case 1 at $\mathbf{3 0 \%}$ penetration level and DG located at Bus 7

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.616 | 12.878 | 9.348 | 12.161 | 10.545 | 12.789 | 9.288 | 12.072 | 10.602 | 12.842 | 9.336 | 12.120 | 10.577 | 12.819 | 9.315 | 12.103 |
| 2 | 132 | 10.194 | 11.135 | 8.910 | 10.796 | 10.058 | 10.949 | 8.793 | 10.623 | 10.169 | 11.034 | 8.889 | 10.714 | 10.117 | 10.994 | 8.844 | 10.679 |
| 3 | 132 | 6.220 | 6.167 | 5.405 | 6.246 | 6.139 | 6.053 | 5.336 | 6.149 | 6.206 | 6.095 | 5.393 | 6.203 | 6.174 | 6.075 | 5.366 | 6.181 |
| 4 | 132 | 8.317 | 7.990 | 7.231 | 8.282 | 8.141 | 7.745 | 7.080 | 8.076 | 8.288 | 7.832 | 7.206 | 8.198 | 8.215 | 7.790 | 7.144 | 8.147 |
| 5 | 132 | 7.746 | 7.299 | 6.738 | 7.622 | 7.506 | 6.971 | 6.531 | 7.340 | 7.705 | 7.083 | 6.702 | 7.505 | 7.607 | 7.029 | 6.619 | 7.436 |
| 6 | 132 | 9.905 | 9.413 | 8.616 | 9.815 | 9.519 | 8.890 | 8.283 | 9.370 | 9.845 | 9.075 | 8.565 | 9.650 | 9.676 | 8.981 | 8.420 | 9.526 |
| 7 | 132 | 7.103 | 6.827 | 6.161 | 6.991 | 6.215 | 5.712 | 5.393 | 6.009 | 6.984 | 6.123 | 6.058 | 6.688 | 6.546 | 5.897 | 5.683 | 6.351 |
| 8 | 132 | 7.288 | 7.188 | 6.344 | 7.297 | 7.135 | 6.969 | 6.212 | 7.113 | 7.263 | 7.049 | 6.322 | 7.221 | 7.199 | 7.010 | 6.268 | 7.175 |
| 9 | 33 | 16.091 | 16.160 | 13.978 | 16.337 | 15.972 | 16.082 | 13.877 | 16.253 | 16.076 | 16.151 | 13.966 | 16.334 | 16.019 | 16.113 | 13.918 | 16.283 |
| 10 | 33 | 19.329 | 18.096 | 16.770 | 19.107 | 19.210 | 18.028 | 16.669 | 19.021 | 19.314 | 18.088 | 16.758 | 19.103 | 19.258 | 18.056 | 16.710 | 19.053 |
| 11 | 11 | 23.085 | 27.572 | 20.111 | 26.240 | 23.028 | 27.520 | 20.063 | 26.197 | 23.079 | 27.567 | 20.106 | 26.239 | 23.051 | 27.541 | 20.082 | 26.212 |
| 12 | 33 | 16.183 | 15.110 | 14.050 | 15.959 | 16.116 | 15.072 | 13.993 | 15.909 | 16.173 | 15.105 | 14.042 | 15.956 | 16.143 | 15.088 | 14.016 | 15.928 |
| 13 | 11 | 25.567 | 30.893 | 22.227 | 29.846 | 25.520 | 30.849 | 22.187 | 29.808 | 25.561 | 30.887 | 22.222 | 29.844 | 25.539 | 30.867 | 22.203 | 29.822 |
| 14 | 33 | 8.271 | 7.718 | 7.167 | 8.068 | 8.256 | 7.709 | 7.154 | 8.056 | 8.268 | 7.716 | 7.164 | 8.066 | 8.262 | 7.713 | 7.160 | 8.061 |
| 15 | 33 | 13.121 | 11.959 | 11.374 | 12.714 | 13.082 | 11.938 | 11.341 | 12.683 | 13.114 | 11.955 | 11.368 | 12.710 | 13.099 | 11.947 | 11.356 | 12.696 |
| 16 | 33 | 10.264 | 9.738 | 8.897 | 10.126 | 10.237 | 9.722 | 8.873 | 10.105 | 10.260 | 9.736 | 8.893 | 10.124 | 10.248 | 9.729 | 8.883 | 10.113 |
| 17 | 33 | 13.440 | 12.539 | 11.651 | 13.172 | 13.389 | 12.509 | 11.607 | 13.134 | 13.432 | 12.534 | 11.645 | 13.169 | 13.410 | 12.522 | 11.626 | 13.149 |
| 18 | 33 | 8.684 | 7.988 | 7.523 | 8.397 | 8.668 | 7.979 | 7.509 | 8.384 | 8.681 | 7.986 | 7.521 | 8.395 | 8.675 | 7.983 | 7.515 | 8.389 |
| 19 | 33 | 9.179 | 8.325 | 7.952 | 8.833 | 9.161 | 8.315 | 7.937 | 8.818 | 9.176 | 8.323 | 7.949 | 8.830 | 9.169 | 8.320 | 7.943 | 8.825 |
| 20 | 33 | 9.528 | 8.778 | 8.255 | 9.225 | 9.506 | 8.766 | 8.237 | 9.208 | 9.524 | 8.776 | 8.252 | 9.223 | 9.516 | 8.771 | 8.245 | 9.215 |
| 21 | 33 | 15.478 | 14.140 | 13.418 | 15.004 | 15.411 | 14.103 | 13.361 | 14.953 | 15.468 | 14.134 | 13.410 | 15.000 | 15.439 | 14.119 | 13.385 | 14.973 |
| 22 | 33 | 15.023 | 13.840 | 13.023 | 14.639 | 14.959 | 13.805 | 12.968 | 14.591 | 15.013 | 13.835 | 13.014 | 14.635 | 14.986 | 13.820 | 12.991 | 14.610 |
| 23 | 33 | 8.488 | 7.944 | 7.354 | 8.276 | 8.472 | 7.935 | 7.340 | 8.263 | 8.485 | 7.943 | 7.351 | 8.274 | 8.479 | 7.939 | 7.346 | 8.268 |
| 24 | 33 | 10.931 | 10.088 | 9.470 | 10.571 | 10.901 | 10.072 | 9.445 | 10.548 | 10.925 | 10.085 | 9.465 | 10.568 | 10.914 | 10.079 | 9.456 | 10.557 |
| 25 | 33 | 6.955 | 6.730 | 6.025 | 6.890 | 6.938 | 6.720 | 6.011 | 6.877 | 6.952 | 6.728 | 6.022 | 6.888 | 6.945 | 6.724 | 6.017 | 6.882 |
| 26 | 33 | 3.063 | 2.871 | 2.652 | 3.019 | 3.060 | 2.870 | 2.650 | 3.017 | 3.062 | 2.871 | 2.652 | 3.018 | 3.061 | 2.870 | 2.651 | 3.018 |
| 27 | 33 | 8.020 | 7.928 | 6.949 | 8.117 | 7.993 | 7.911 | 6.926 | 8.098 | 8.016 | 7.926 | 6.946 | 8.116 | 8.004 | 7.918 | 6.936 | 8.105 |
| 28 | 132 | 5.458 | 5.199 | 4.737 | 5.381 | 5.354 | 5.051 | 4.648 | 5.259 | 5.440 | 5.101 | 4.723 | 5.332 | 5.397 | 5.077 | 4.686 | 5.301 |
| 29 | 33 | 4.086 | 3.802 | 3.539 | 3.981 | 4.080 | 3.799 | 3.534 | 3.976 | 4.085 | 3.801 | 3.538 | 3.980 | 4.082 | 3.800 | 3.536 | 3.978 |
| 30 | 33 | 4.287 | 3.753 | 3.713 | 4.151 | 4.282 | 3.751 | 3.708 | 4.147 | 4.286 | 3.753 | 3.712 | 4.150 | 4.284 | 3.752 | 3.710 | 4.149 |

Table D27: IEC Simulated Results for Case 2 at $\mathbf{3 0 \%}$ penetration level and DG located at Bus 26

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.564 | 12.807 | 9.304 | 12.092 | 10.547 | 12.790 | 9.289 | 12.077 | 10.559 | 12.802 | 9.299 | 12.087 | 10.555 | 12.798 | 9.296 | 12.085 |
| 2 | 132 | 10.087 | 10.971 | 8.818 | 10.654 | 10.057 | 10.948 | 8.793 | 10.629 | 10.078 | 10.964 | 8.810 | 10.646 | 10.071 | 10.959 | 8.804 | 10.642 |
| 3 | 132 | 6.168 | 6.071 | 5.360 | 6.175 | 6.140 | 6.054 | 5.336 | 6.152 | 6.159 | 6.606 | 5.353 | 6.168 | 6.152 | 6.061 | 5.347 | 6.164 |
| 4 | 132 | 8.205 | 7.783 | 7.135 | 8.135 | 8.142 | 7.746 | 7.080 | 8.082 | 8.184 | 7.771 | 7.117 | 8.119 | 8.168 | 7.762 | 7.103 | 8.108 |
| 5 | 132 | 7.507 | 6.972 | 6.531 | 7.355 | 7.497 | 6.966 | 6.523 | 7.347 | 7.504 | 6.970 | 6.529 | 7.353 | 7.502 | 6.969 | 6.527 | 7.352 |
| 6 | 132 | 9.637 | 8.958 | 8.385 | 9.487 | 9.514 | 8.887 | 8.279 | 9.380 | 9.596 | 8.935 | 8.350 | 9.454 | 9.563 | 8.916 | 8.321 | 9.431 |
| 7 | 132 | 6.160 | 5.682 | 5.345 | 6.015 | 6.136 | 5.668 | 5.325 | 5.995 | 6.153 | 5.677 | 5.339 | 6.009 | 6.147 | 5.674 | 5.334 | 6.005 |
| 8 | 132 | 7.198 | 7.008 | 6.266 | 7.172 | 7.137 | 6.970 | 6.214 | 7.120 | 7.178 | 6.996 | 6.249 | 7.156 | 7.162 | 6.986 | 6.235 | 7.145 |
| 9 | 33 | 16.101 | 16.212 | 13.988 | 16.360 | 15.973 | 16.083 | 13.878 | 16.259 | 16.060 | 16.141 | 13.952 | 16.332 | 16.029 | 16.120 | 13.926 | 16.299 |
| 10 | 33 | 19.465 | 18.307 | 16.889 | 19.232 | 19.209 | 18.029 | 16.668 | 19.040 | 19.386 | 18.132 | 16.820 | 19.197 | 19.332 | 18.100 | 16.774 | 19.136 |
| 11 | 11 | 23.093 | 27.580 | 20.118 | 26.258 | 23.029 | 27.521 | 20.064 | 26.201 | 23.072 | 27.561 | 20.101 | 26.238 | 23.056 | 27.546 | 20.087 | 26.221 |
| 12 | 33 | 16.211 | 15.173 | 14.075 | 15.980 | 16.113 | 15.070 | 13.990 | 15.913 | 16.181 | 15.110 | 14.049 | 15.975 | 16.162 | 15.099 | 14.032 | 15.952 |
| 13 | 11 | 25.592 | 30.918 | 22.249 | 29.883 | 25.520 | 30.849 | 22.187 | 29.813 | 25.570 | 30.896 | 22.229 | 29.860 | 25.554 | 30.881 | 22.216 | 29.841 |
| 14 | 33 | 8.280 | 7.738 | 7.175 | 8.070 | 8.253 | 7.708 | 7.152 | 8.056 | 8.272 | 7.719 | 7.168 | 8.074 | 8.268 | 7.717 | 7.165 | 8.069 |
| 15 | 33 | 13.190 | 12.065 | 11.435 | 12.772 | 13.084 | 11.939 | 11.343 | 12.694 | 13.158 | 11.980 | 11.406 | 12.759 | 13.136 | 11.968 | 11.388 | 12.734 |
| 16 | 33 | 10.280 | 9.771 | 8.910 | 10.135 | 10.235 | 9.721 | 8.871 | 10.106 | 10.266 | 9.740 | 8.898 | 10.135 | 10.258 | 9.735 | 8.891 | 10.125 |
| 17 | 33 | 13.483 | 12.615 | 11.688 | 13.204 | 13.385 | 12.508 | 11.604 | 13.139 | 13.453 | 12.547 | 11.663 | 13.200 | 13.435 | 12.536 | 11.647 | 13.178 |
| 18 | 33 | 8.703 | 8.024 | 7.540 | 8.409 | 8.666 | 7.978 | 7.508 | 8.386 | 8.692 | 7.993 | 7.531 | 8.410 | 8.686 | 7.989 | 7.525 | 8.402 |
| 19 | 33 | 9.197 | 8.361 | 7.968 | 8.872 | 9.159 | 8.314 | 7.935 | 8.813 | 9.186 | 8.329 | 7.958 | 8.832 | 9.179 | 8.326 | 7.953 | 8.830 |
| 20 | 33 | 9.549 | 8.818 | 8.274 | 9.238 | 9.504 | 8.765 | 8.235 | 9.210 | 9.536 | 8.783 | 8.262 | 9.239 | 9.528 | 8.778 | 8.256 | 9.230 |
| 21 | 33 | 15.654 | 14.378 | 13.571 | 15.160 | 15.416 | 14.106 | 13.365 | 14.979 | 15.580 | 14.197 | 13.507 | 15.123 | 15.531 | 14.170 | 13.465 | 15.067 |
| 22 | 33 | 15.234 | 14.119 | 13.206 | 14.833 | 14.968 | 13.811 | 12.976 | 14.622 | 15.151 | 13.914 | 13.134 | 14.784 | 15.095 | 13.882 | 13.086 | 14.720 |
| 23 | 33 | 8.609 | 8.103 | 7.458 | 8.391 | 8.482 | 7.941 | 7.349 | 8.283 | 8.569 | 7.991 | 7.424 | 8.357 | 8.540 | 7.975 | 7.399 | 8.326 |
| 24 | 33 | 11.545 | 10.808 | 10.002 | 11.258 | 10.970 | 10.111 | 9.505 | 10.658 | 11.354 | 10.325 | 9.837 | 10.973 | 11.210 | 10.246 | 9.713 | 10.826 |
| 25 | 33 | 9.329 | 9.493 | 8.081 | 9.446 | 7.251 | 6.919 | 6.281 | 7.288 | 8.521 | 7.637 | 7.381 | 8.277 | 7.923 | 7.310 | 6.870 | 7.712 |
| 26 | 33 | 10.488 | 12.730 | 9.077 | 12.429 | 3.596 | 3.172 | 3.114 | 3.560 | 6.464 | 4.281 | 5.596 | 5.955 | 4.632 | 3.659 | 4.030 | 4.449 |
| 27 | 33 | 8.933 | 8.995 | 7.740 | 9.057 | 8.097 | 7.983 | 7.016 | 8.262 | 8.645 | 8.329 | 7.491 | 8.717 | 8.429 | 8.193 | 7.306 | 8.495 |
| 28 | 132 | 5.467 | 5.117 | 4.746 | 5.358 | 5.369 | 5.060 | 4.661 | 5.270 | 5.434 | 5.098 | 4.717 | 5.330 | 5.405 | 5.081 | 4.693 | 5.309 |
| 29 | 33 | 4.231 | 3.977 | 3.665 | 4.158 | 4.088 | 3.803 | 3.541 | 3.968 | 4.186 | 3.859 | 3.625 | 4.046 | 4.155 | 3.842 | 3.599 | 4.029 |
| 30 | 33 | 4.412 | 3.905 | 3.821 | 4.305 | 4.287 | 3.753 | 3.713 | 4.139 | 4.373 | 3.796 | 3.787 | 4.207 | 4.347 | 3.783 | 3.765 | 4.193 |

Table D28: IEC Simulated Results for Case 3 at 30\% penetration level and DG located at Bus 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.573 | 12.815 | 9.311 | 12.100 | 10.547 | 12.791 | 9.289 | 12.077 | 10.564 | 12.806 | 9.303 | 12.092 | 10.558 | 12.801 | 9.298 | 12.087 |
| 2 | 132 | 10.102 | 10.983 | 8.831 | 10.667 | 10.058 | 10.949 | 8.794 | 10.629 | 10.087 | 10.971 | 8.818 | 10.654 | 10.076 | 10.962 | 8.808 | 10.646 |
| 3 | 132 | 6.180 | 6.079 | 5.371 | 6.186 | 6.141 | 6.054 | 5.337 | 6.152 | 6.166 | 6.070 | 5.359 | 6.174 | 6.156 | 6.064 | 5.350 | 6.167 |
| 4 | 132 | 8.232 | 7.799 | 7.158 | 8.160 | 8.144 | 7.747 | 7.082 | 8.082 | 8.200 | 7.780 | 7.130 | 8.133 | 8.176 | 7.766 | 7.110 | 8.115 |
| 5 | 132 | 7.513 | 6.975 | 6.536 | 7.360 | 7.497 | 6.966 | 6.523 | 7.347 | 7.507 | 6.972 | 6.531 | 7.356 | 7.504 | 6.970 | 6.528 | 7.353 |
| 6 | 132 | 9.708 | 8.998 | 8.446 | 9.553 | 9.521 | 8.891 | 8.285 | 9.384 | 9.640 | 8.960 | 8.388 | 9.493 | 9.585 | 8.929 | 8.341 | 9.452 |
| 7 | 132 | 6.174 | 5.689 | 5.357 | 6.027 | 6.138 | 5.669 | 5.326 | 5.995 | 6.161 | 5.682 | 5.346 | 6.016 | 6.151 | 5.677 | 5.338 | 6.009 |
| 8 | 132 | 7.239 | 7.034 | 6.302 | 7.209 | 7.141 | 6.973 | 6.218 | 7.121 | 7.204 | 7.012 | 6.271 | 7.178 | 7.176 | 6.995 | 6.247 | 7.157 |
| 9 | 33 | 16.085 | 16.172 | 13.974 | 16.337 | 15.971 | 16.081 | 13.875 | 16.253 | 16.044 | 16.130 | 13.939 | 16.313 | 16.014 | 16.110 | 13.913 | 16.283 |
| 10 | 33 | 19.384 | 18.172 | 16.819 | 19.148 | 19.203 | 18.025 | 16.663 | 19.023 | 19.321 | 18.093 | 16.764 | 19.126 | 19.280 | 18.069 | 16.729 | 19.082 |
| 11 | 11 | 23.084 | 27.572 | 20.111 | 26.246 | 23.027 | 27.519 | 20.062 | 26.198 | 23.064 | 27.553 | 20.093 | 26.228 | 23.048 | 27.539 | 20.080 | 26.213 |
| 12 | 33 | 16.190 | 15.128 | 14.056 | 15.960 | 16.112 | 15.070 | 13.989 | 15.908 | 16.162 | 15.099 | 14.033 | 15.953 | 16.145 | 15.089 | 14.018 | 15.934 |
| 13 | 11 | 25.575 | 30.901 | 22.234 | 29.862 | 25.518 | 30.847 | 22.185 | 29.808 | 25.555 | 30.882 | 22.217 | 29.843 | 25.542 | 30.869 | 22.205 | 29.827 |
| 14 | 33 | 8.273 | 7.723 | 7.169 | 8.066 | 8.254 | 7.708 | 7.153 | 8.055 | 8.267 | 7.716 | 7.163 | 8.067 | 8.263 | 7.714 | 7.161 | 8.063 |
| 15 | 33 | 13.149 | 11.997 | 11.398 | 12.732 | 13.080 | 11.937 | 11.339 | 12.685 | 13.125 | 11.961 | 11.378 | 12.726 | 13.111 | 11.954 | 11.366 | 12.710 |
| 16 | 33 | 10.269 | 9.748 | 8.901 | 10.126 | 10.235 | 9.721 | 8.871 | 10.104 | 10.257 | 9.734 | 8.890 | 10.125 | 10.250 | 9.730 | 8.885 | 10.117 |
| 17 | 33 | 13.455 | 12.563 | 11.665 | 13.179 | 13.385 | 12.507 | 11.604 | 13.134 | 13.431 | 12.534 | 11.643 | 13.175 | 13.416 | 12.525 | 11.631 | 13.158 |
| 18 | 33 | 8.691 | 8.000 | 7.529 | 8.399 | 8.666 | 7.978 | 7.508 | 8.384 | 8.682 | 7.987 | 7.522 | 8.399 | 8.678 | 7.984 | 7.518 | 8.394 |
| 19 | 33 | 9.185 | 8.337 | 7.958 | 8.849 | 9.159 | 8.314 | 7.935 | 8.815 | 9.176 | 8.324 | 7.950 | 8.827 | 9.171 | 8.321 | 7.946 | 8.825 |
| 20 | 33 | 9.536 | 8.791 | 8.262 | 9.227 | 9.504 | 8.765 | 8.235 | 9.208 | 9.525 | 8.776 | 8.253 | 9.227 | 9.519 | 8.773 | 8.248 | 9.220 |
| 21 | 33 | 15.552 | 14.229 | 13.482 | 15.058 | 15.409 | 14.100 | 13.356 | 14.958 | 15.501 | 14.153 | 13.438 | 15.043 | 15.471 | 14.136 | 13.412 | 15.009 |
| 22 | 33 | 15.111 | 13.946 | 13.100 | 14.708 | 14.954 | 13.802 | 12.964 | 14.597 | 15.056 | 13.860 | 13.052 | 14.689 | 15.024 | 13.842 | 13.024 | 14.652 |
| 23 | 33 | 8.537 | 8.006 | 7.396 | 8.316 | 8.471 | 7.934 | 7.339 | 8.267 | 8.514 | 7.960 | 7.376 | 8.306 | 8.501 | 7.952 | 7.365 | 8.290 |
| 24 | 33 | 11.167 | 10.363 | 9.674 | 10.842 | 10.903 | 10.073 | 9.447 | 10.571 | 11.074 | 10.169 | 9.594 | 10.721 | 11.017 | 10.137 | 9.545 | 10.659 |
| 25 | 33 | 7.697 | 7.614 | 6.667 | 7.686 | 6.979 | 6.747 | 6.046 | 6.968 | 7.429 | 7.020 | 6.435 | 7.351 | 7.253 | 6.914 | 6.284 | 7.169 |
| 26 | 33 | 3.162 | 2.994 | 2.738 | 3.144 | 3.060 | 2.869 | 2.650 | 3.008 | 3.126 | 2.907 | 2.707 | 3.059 | 3.104 | 2.865 | 2.689 | 3.047 |
| 27 | 33 | 10.539 | 11.030 | 9.130 | 10.845 | 8.194 | 8.053 | 7.101 | 8.422 | 9.566 | 8.881 | 8.288 | 9.550 | 8.934 | 8.507 | 7.747 | 8.933 |
| 28 | 132 | 5.566 | 5.174 | 4.832 | 5.449 | 5.383 | 5.068 | 4.674 | 5.278 | 5.498 | 5.135 | 4.773 | 5.387 | 5.441 | 5.102 | 4.724 | 5.342 |
| 29 | 33 | 11.570 | 13.881 | 10.014 | 13.513 | 4.524 | 4.056 | 3.919 | 4.505 | 7.493 | 5.295 | 6.487 | 6.828 | 5.678 | 4.614 | 4.935 | 5.380 |
| 30 | 33 | 5.904 | 5.705 | 5.113 | 5.967 | 4.422 | 3.819 | 3.830 | 4.184 | 5.274 | 4.211 | 4.567 | 4.929 | 4.864 | 4.034 | 4.217 | 4.628 |

Table D29: IEC Simulated Results for Case 4 at $\mathbf{3 0 \%}$ penetration level and DG located at Bus 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.568 | 12.810 | 9.307 | 12.095 | 10.546 | 12.790 | 9.288 | 12.076 | 10.560 | 12.803 | 9.300 | 12.089 | 10.556 | 12.798 | 9.296 | 12.085 |
| 2 | 132 | 10.094 | 10.976 | 8.824 | 10.660 | 10.057 | 10.948 | 8.792 | 10.629 | 10.081 | 10.966 | 8.813 | 10.649 | 10.072 | 10.959 | 8.805 | 10.643 |
| 3 | 132 | 6.172 | 6.074 | 5.364 | 6.179 | 6.139 | 6.053 | 5.336 | 6.152 | 6.160 | 6.067 | 5.354 | 6.170 | 6.152 | 6.061 | 5.347 | 6.164 |
| 4 | 132 | 8.214 | 7.789 | 7.142 | 8.144 | 8.140 | 7.745 | 7.079 | 8.080 | 8.187 | 7.773 | 7.119 | 8.122 | 8.168 | 7.761 | 7.102 | 8.108 |
| 5 | 132 | 7.510 | 6.973 | 6.534 | 7.357 | 7.497 | 6.966 | 6.522 | 7.347 | 7.505 | 6.971 | 6.530 | 7.354 | 7.502 | 6.969 | 6.527 | 7.352 |
| 6 | 132 | 9.670 | 8.977 | 8.414 | 9.519 | 9.512 | 8.886 | 8.277 | 9.378 | 9.613 | 8.944 | 8.364 | 9.468 | 9.568 | 8.919 | 8.326 | 9.436 |
| 7 | 132 | 6.167 | 5.685 | 5.351 | 6.021 | 6.136 | 5.668 | 5.325 | 5.995 | 6.156 | 5.679 | 5.341 | 6.011 | 6.148 | 5.675 | 5.335 | 6.006 |
| 8 | 132 | 7.220 | 7.022 | 6.285 | 7.192 | 7.137 | 6.970 | 6.214 | 7.119 | 7.190 | 7.003 | 6.259 | 7.166 | 7.167 | 6.989 | 6.239 | 7.149 |
| 9 | 33 | 16.063 | 16.155 | 13.954 | 16.319 | 15.966 | 16.078 | 13.871 | 16.248 | 16.028 | 16.119 | 13.925 | 16.299 | 16.003 | 16.102 | 13.904 | 16.274 |
| 10 | 33 | 19.349 | 18.146 | 16.788 | 19.119 | 19.198 | 18.022 | 16.658 | 19.016 | 19.295 | 18.078 | 16.742 | 19.103 | 19.262 | 18.059 | 16.714 | 19.067 |
| 11 | 11 | 23.073 | 27.561 | 20.101 | 26.236 | 23.025 | 27.517 | 20.060 | 26.195 | 23.056 | 27.545 | 20.086 | 26.221 | 23.043 | 27.534 | 20.075 | 26.208 |
| 12 | 33 | 16.174 | 15.117 | 14.043 | 15.948 | 16.110 | 15.069 | 13.988 | 15.905 | 16.152 | 15.093 | 14.023 | 15.943 | 16.138 | 15.085 | 14.012 | 15.928 |
| 13 | 11 | 25.564 | 30.890 | 22.224 | 29.851 | 25.517 | 30.845 | 22.184 | 29.806 | 25.547 | 30.874 | 22.210 | 29.835 | 25.536 | 30.864 | 22.201 | 29.822 |
| 14 | 33 | 8.269 | 7.720 | 7.166 | 8.063 | 8.254 | 7.708 | 7.152 | 8.055 | 8.264 | 7.714 | 7.161 | 8.065 | 8.262 | 7.713 | 7.159 | 8.062 |
| 15 | 33 | 13.135 | 11.987 | 11.387 | 12.720 | 13.079 | 11.936 | 11.338 | 12.683 | 13.115 | 11.956 | 11.370 | 12.717 | 13.105 | 11.950 | 11.360 | 12.704 |
| 16 | 33 | 10.262 | 9.743 | 8.895 | 10.120 | 10.234 | 9.721 | 8.871 | 10.103 | 10.252 | 9.731 | 8.886 | 10.120 | 10.247 | 9.728 | 8.882 | 10.114 |
| 17 | 33 | 13.441 | 12.554 | 11.653 | 13.168 | 13.383 | 12.506 | 11.602 | 13.131 | 13.421 | 12.528 | 11.635 | 13.166 | 13.409 | 12.521 | 11.625 | 13.152 |
| 18 | 33 | 8.686 | 7.996 | 7.525 | 8.395 | 8.666 | 7.978 | 7.508 | 8.383 | 8.679 | 7.985 | 7.519 | 8.396 | 8.675 | 7.983 | 7.516 | 8.391 |
| 19 | 33 | 9.180 | 8.333 | 7.953 | 8.844 | 9.158 | 8.314 | 7.935 | 8.815 | 9.173 | 8.322 | 7.947 | 8.825 | 9.169 | 8.320 | 7.944 | 8.823 |
| 20 | 33 | 9.529 | 8.786 | 8.257 | 9.221 | 9.504 | 8.764 | 8.234 | 9.207 | 9.520 | 8.774 | 8.249 | 9.223 | 9.516 | 8.771 | 8.245 | 9.217 |
| 21 | 33 | 15.523 | 14.208 | 13.457 | 15.034 | 15.403 | 14.099 | 13.354 | 14.952 | 15.480 | 14.142 | 13.421 | 15.024 | 15.457 | 14.128 | 13.400 | 14.996 |
| 22 | 33 | 15.080 | 13.923 | 13.073 | 14.681 | 14.950 | 13.800 | 12.961 | 14.591 | 15.034 | 13.848 | 13.033 | 14.668 | 15.009 | 13.833 | 13.011 | 14.639 |
| 23 | 33 | 8.524 | 7.995 | 7.385 | 8.304 | 8.470 | 7.934 | 7.338 | 8.264 | 8.505 | 7.954 | 7.368 | 8.297 | 8.495 | 7.948 | 7.359 | 8.285 |
| 24 | 33 | 11.114 | 10.319 | 9.629 | 10.791 | 10.897 | 10.069 | 9.441 | 10.561 | 11.037 | 10.148 | 9.562 | 10.687 | 10.992 | 10.123 | 9.523 | 10.637 |
| 25 | 33 | 7.544 | 7.471 | 6.535 | 7.533 | 6.957 | 6.733 | 6.027 | 6.940 | 7.325 | 6.958 | 6.345 | 7.259 | 7.187 | 6.874 | 6.227 | 7.113 |
| 26 | 33 | 3.141 | 2.975 | 2.720 | 3.124 | 3.085 | 2.868 | 2.648 | 3.008 | 3.111 | 2.899 | 2.695 | 3.048 | 3.095 | 2.890 | 2.680 | 3.040 |
| 27 | 33 | 9.974 | 10.453 | 8.642 | 10.294 | 8.121 | 8.003 | 7.037 | 8.333 | 9.220 | 8.680 | 7.988 | 9.255 | 8.736 | 8.387 | 7.575 | 8.773 |
| 28 | 132 | 5.529 | 5.153 | 4.799 | 5.414 | 5.374 | 5.062 | 4.665 | 5.271 | 5.471 | 5.120 | 4.750 | 5.362 | 5.424 | 5.092 | 4.709 | 5.326 |
| 29 | 33 | 5.583 | 5.715 | 4.835 | 5.720 | 4.197 | 3.867 | 3.635 | 4.113 | 4.990 | 4.283 | 4.321 | 4.747 | 4.611 | 4.093 | 3.998 | 4.405 |
| 30 | 33 | 11.793 | 14.051 | 10.208 | 13.648 | 4.697 | 3.957 | 4.068 | 4.522 | 7.692 | 5.058 | 6.660 | 7.001 | 5.885 | 4.471 | 5.115 | 5.553 |

Table D30: IEC Simulated Results for Case 5 at $\mathbf{3 0 \%}$ penetration level and DG located at Bus 7 and 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.632 | 12.905 | 9.362 | 12.187 | 10.545 | 12.789 | 9.287 | 12.074 | 10.583 | 12.824 | 9.319 | 12.105 | 10.571 | 12.813 | 9.309 | 12.098 |
| 2 | 132 | 10.222 | 11.197 | 8.934 | 10.846 | 10.056 | 10.948 | 8.792 | 10.624 | 10.128 | 11.002 | 8.853 | 10.684 | 10.103 | 10.984 | 8.832 | 10.668 |
| 3 | 132 | 6.248 | 6.215 | 5.429 | 6.283 | 6.139 | 6.053 | 5.335 | 6.149 | 6.185 | 6.082 | 5.375 | 6.187 | 6.170 | 6.073 | 5.362 | 6.178 |
| 4 | 132 | 8.381 | 8.099 | 7.286 | 8.362 | 8.140 | 7.745 | 7.079 | 8.076 | 8.242 | 7.805 | 7.166 | 8.163 | 8.207 | 7.785 | 7.137 | 8.140 |
| 5 | 132 | 7.748 | 7.396 | 6.739 | 7.664 | 7.500 | 6.968 | 6.525 | 7.342 | 7.610 | 7.030 | 6.620 | 7.433 | 7.563 | 7.004 | 6.580 | 7.401 |
| 6 | 132 | 10.049 | 9.656 | 8.740 | 9.993 | 9.515 | 8.888 | 8.280 | 9.372 | 9.739 | 9.015 | 8.473 | 9.566 | 9.655 | 8.969 | 8.402 | 9.509 |
| 7 | 132 | 7.099 | 7.184 | 6.157 | 7.189 | 6.171 | 5.687 | 5.355 | 5.997 | 6.570 | 5.907 | 5.700 | 6.350 | 6.373 | 5.802 | 5.532 | 6.199 |
| 8 | 132 | 7.363 | 7.297 | 6.409 | 7.386 | 7.136 | 6.970 | 6.213 | 7.115 | 7.230 | 7.029 | 6.294 | 7.196 | 7.199 | 7.009 | 6.267 | 7.176 |
| 9 | 33 | 16.177 | 16.231 | 14.052 | 16.406 | 15.969 | 16.080 | 13.874 | 16.251 | 16.056 | 16.137 | 13.948 | 16.320 | 16.028 | 16.119 | 13.925 | 16.293 |
| 10 | 33 | 19.461 | 18.212 | 16.884 | 19.205 | 19.202 | 18.024 | 16.662 | 19.019 | 19.308 | 18.085 | 16.753 | 19.107 | 19.284 | 18.071 | 16.733 | 19.082 |
| 11 | 11 | 23.128 | 27.613 | 20.148 | 26.280 | 23.026 | 27.518 | 20.061 | 26.197 | 23.069 | 27.558 | 20.098 | 26.232 | 23.055 | 27.545 | 20.086 | 26.218 |
| 12 | 33 | 16.238 | 15.154 | 14.097 | 15.998 | 16.112 | 15.070 | 13.989 | 15.907 | 16.164 | 15.100 | 14.034 | 15.951 | 16.151 | 15.092 | 14.023 | 15.938 |
| 13 | 11 | 25.608 | 30.932 | 22.261 | 29.888 | 25.518 | 30.847 | 22.185 | 29.807 | 25.555 | 30.882 | 22.217 | 29.841 | 25.546 | 30.873 | 22.209 | 29.830 |
| 14 | 33 | 8.283 | 7.728 | 7.177 | 8.075 | 8.254 | 7.709 | 7.153 | 8.055 | 8.266 | 7.715 | 7.163 | 8.066 | 8.264 | 7.714 | 7.162 | 8.064 |
| 15 | 33 | 13.169 | 12.006 | 11.415 | 12.748 | 13.079 | 11.936 | 11.339 | 12.683 | 13.115 | 11.956 | 11.370 | 12.714 | 13.110 | 11.953 | 11.365 | 12.708 |
| 16 | 33 | 10.288 | 9.759 | 8.917 | 10.141 | 10.235 | 9.721 | 8.871 | 10.104 | 10.257 | 9.734 | 8.890 | 10.123 | 10.252 | 9.731 | 8.886 | 10.118 |
| 17 | 33 | 13.489 | 12.582 | 11.693 | 13.206 | 13.385 | 12.507 | 11.604 | 13.133 | 13.428 | 12.532 | 11.641 | 13.169 | 13.419 | 12.527 | 11.633 | 13.159 |
| 18 | 33 | 8.700 | 8.004 | 7.537 | 8.407 | 8.666 | 7.978 | 7.508 | 8.383 | 8.680 | 7.986 | 7.520 | 8.396 | 8.678 | 7.985 | 7.519 | 8.393 |
| 19 | 33 | 9.197 | 8.342 | 7.968 | 8.858 | 9.159 | 8.314 | 7.935 | 8.815 | 9.174 | 8.323 | 7.948 | 8.827 | 9.172 | 8.322 | 7.946 | 8.826 |
| 20 | 33 | 9.549 | 8.798 | 8.274 | 9.238 | 9.504 | 8.765 | 8.235 | 9.207 | 9.523 | 8.775 | 8.251 | 9.223 | 9.520 | 8.774 | 8.248 | 9.220 |
| 21 | 33 | 15.582 | 14.242 | 13.508 | 15.081 | 15.405 | 14.100 | 13.356 | 14.953 | 15.476 | 14.139 | 13.416 | 15.014 | 15.466 | 14.134 | 13.408 | 15.002 |
| 22 | 33 | 15.136 | 13.955 | 13.120 | 14.725 | 14.953 | 13.802 | 12.963 | 14.591 | 15.025 | 13.842 | 13.025 | 14.654 | 15.017 | 13.838 | 13.018 | 14.642 |
| 23 | 33 | 8.536 | 8.002 | 7.395 | 8.314 | 8.470 | 7.934 | 7.338 | 8.263 | 8.495 | 7.949 | 7.360 | 8.286 | 8.495 | 7.948 | 7.359 | 8.284 |
| 24 | 33 | 11.128 | 10.326 | 9.640 | 10.803 | 10.897 | 10.069 | 9.441 | 10.555 | 10.982 | 10.117 | 9.514 | 10.630 | 10.983 | 10.118 | 9.515 | 10.625 |
| 25 | 33 | 7.509 | 7.442 | 6.504 | 7.502 | 6.947 | 6.726 | 6.018 | 6.915 | 7.138 | 6.844 | 6.184 | 7.076 | 7.142 | 6.847 | 6.188 | 7.066 |
| 26 | 33 | 3.139 | 2.973 | 2.718 | 3.121 | 3.058 | 2.868 | 2.648 | 3.010 | 3.087 | 2.885 | 2.673 | 3.033 | 3.089 | 2.886 | 2.675 | 3.037 |
| 27 | 33 | 9.781 | 10.271 | 8.473 | 10.110 | 8.068 | 7.965 | 6.991 | 8.244 | 8.597 | 8.299 | 7.449 | 8.672 | 8.582 | 8.290 | 7.441 | 8.619 |
| 28 | 132 | 5.612 | 5.335 | 4.871 | 5.533 | 5.366 | 5.058 | 4.658 | 5.265 | 5.460 | 5.113 | 4.740 | 5.350 | 5.435 | 5.099 | 4.719 | 5.335 |
| 29 | 33 | 7.810 | 9.040 | 6.761 | 8.836 | 4.272 | 3.910 | 3.700 | 4.199 | 5.074 | 4.324 | 4.395 | 4.792 | 4.986 | 4.288 | 4.328 | 4.769 |
| 30 | 33 | 5.386 | 5.209 | 4.664 | 5.431 | 4.337 | 3.777 | 3.756 | 4.148 | 4.652 | 3.932 | 4.029 | 4.429 | 4.641 | 3.93 | 4.022 | 4.444 |

Table D31: IEC Simulated Results for Case 6 at 30\% penetration level and DG located at Bus 26 and 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.574 | 12.816 | 9.312 | 12.100 | 10.546 | 12.789 | 9.288 | 12.076 | 10.563 | 12.806 | 9.303 | 12.091 | 10.558 | 12.801 | 9.298 | 12.087 |
| 2 | 132 | 10.104 | 10.984 | 8.833 | 10.668 | 10.056 | 10.947 | 8.792 | 10.628 | 10.085 | 10.970 | 8.817 | 10.652 | 10.076 | 10.962 | 8.808 | 10.646 |
| 3 | 132 | 6.183 | 6.081 | 5.373 | 6.188 | 6.139 | 6.053 | 5.335 | 6.151 | 6.166 | 6.070 | 5.358 | 6.173 | 6.156 | 6.064 | 5.350 | 6.167 |
| 4 | 132 | 8.239 | 7.803 | 7.164 | 8.165 | 8.139 | 7.744 | 7.078 | 8.079 | 8.199 | 7.780 | 7.130 | 8.130 | 8.177 | 7.767 | 7.111 | 8.115 |
| 5 | 132 | 7.513 | 6.975 | 6.536 | 7.360 | 7.496 | 6.966 | 6.522 | 7.347 | 7.506 | 6.972 | 6.531 | 7.355 | 7.503 | 6.970 | 6.528 | 7.353 |
| 6 | 132 | 9.714 | 9.002 | 8.452 | 9.556 | 9.510 | 8.885 | 8.275 | 9.375 | 9.632 | 8.955 | 8.381 | 9.483 | 9.584 | 8.928 | 8.340 | 9.449 |
| 7 | 132 | 6.175 | 5.690 | 5.358 | 6.027 | 6.136 | 5.668 | 5.324 | 5.994 | 6.159 | 5.681 | 5.345 | 6.014 | 6.151 | 5.676 | 5.337 | 6.008 |
| 8 | 132 | 7.239 | 7.034 | 6.302 | 7.208 | 7.135 | 6.969 | 6.212 | 7.117 | 7.198 | 7.008 | 6.266 | 7.172 | 7.173 | 6.994 | 6.246 | 7.155 |
| 9 | 33 | 16.131 | 16.235 | 14.014 | 16.382 | 15.966 | 16.078 | 13.871 | 16.251 | 16.066 | 16.145 | 13.958 | 16.336 | 16.031 | 16.121 | 13.928 | 16.300 |
| 10 | 33 | 19.499 | 18.337 | 16.918 | 19.254 | 19.195 | 18.021 | 16.656 | 19.023 | 19.380 | 18.128 | 16.816 | 19.189 | 19.325 | 18.096 | 16.768 | 19.128 |
| 11 | 11 | 23.107 | 27.594 | 20.131 | 26.269 | 23.025 | 27.517 | 20.060 | 26.197 | 23.075 | 27.564 | 20.103 | 26.240 | 23.057 | 27.547 | 20.088 | 26.222 |
| 12 | 33 | 16.229 | 15.187 | 14.090 | 15.992 | 16.108 | 15.068 | 13.986 | 15.907 | 16.182 | 15.110 | 14.050 | 15.974 | 16.161 | 15.098 | 14.031 | 15.950 |
| 13 | 11 | 25.604 | 30.930 | 22.259 | 29.893 | 25.516 | 30.845 | 22.183 | 29.808 | 25.570 | 30.897 | 22.230 | 29.860 | 25.553 | 30.880 | 22.215 | 29.840 |
| 14 | 33 | 8.284 | 7.741 | 7.178 | 8.072 | 8.252 | 7.707 | 7.151 | 8.054 | 8.272 | 7.719 | 7.168 | 8.074 | 8.268 | 7.716 | 7.164 | 8.068 |
| 15 | 33 | 13.200 | 12.075 | 11.443 | 12.778 | 13.078 | 11.936 | 11.338 | 12.686 | 13.152 | 11.977 | 11.402 | 12.753 | 13.131 | 11.965 | 11.384 | 12.730 |
| 16 | 33 | 10.287 | 9.777 | 8.916 | 10.139 | 10.233 | 9.720 | 8.870 | 10.104 | 10.266 | 9.740 | 8.898 | 10.135 | 10.257 | 9.734 | 8.891 | 10.124 |
| 17 | 33 | 13.497 | 12.627 | 11.701 | 13.213 | 13.381 | 12.505 | 11.600 | 13.133 | 13.452 | 12.546 | 11.662 | 13.198 | 13.432 | 12.535 | 11.645 | 13.176 |
| 18 | 33 | 8.707 | 8.028 | 7.544 | 8.412 | 8.664 | 7.977 | 7.507 | 8.384 | 8.691 | 7.992 | 7.529 | 8.408 | 8.684 | 7.988 | 7.524 | 8.400 |
| 19 | 33 | 9.202 | 8.366 | 7.973 | 8.879 | 9.157 | 8.313 | 7.933 | 8.812 | 9.185 | 8.329 | 7.958 | 8.832 | 9.178 | 8.325 | 7.952 | 8.829 |
| 20 | 33 | 9.555 | 8.824 | 8.279 | 9.241 | 9.502 | 8.764 | 8.233 | 9.207 | 9.535 | 8.782 | 8.261 | 9.238 | 9.527 | 8.777 | 8.254 | 9.228 |
| 21 | 33 | 15.671 | 14.399 | 13.585 | 15.170 | 15.402 | 14.098 | 13.353 | 14.961 | 15.566 | 14.189 | 13.494 | 15.108 | 15.518 | 14.163 | 13.454 | 15.055 |
| 22 | 33 | 15.249 | 14.140 | 13.219 | 14.840 | 14.951 | 13.801 | 12.961 | 14.602 | 15.132 | 13.903 | 13.118 | 14.765 | 15.079 | 13.873 | 13.072 | 14.706 |
| 23 | 33 | 8.610 | 8.110 | 7.459 | 8.390 | 8.472 | 7.935 | 7.340 | 8.271 | 8.556 | 7.984 | 7.412 | 8.345 | 8.530 | 7.969 | 7.390 | 8.317 |
| 24 | 33 | 11.523 | 10.826 | 9.983 | 11.265 | 10.921 | 10.083 | 9.462 | 10.603 | 11.280 | 10.284 | 9.773 | 10.908 | 11.157 | 10.217 | 9.667 | 10.782 |
| 25 | 33 | 9.125 | 9.478 | 7.903 | 9.378 | 7.075 | 6.809 | 6.129 | 7.100 | 8.190 | 7.457 | 7.094 | 8.000 | 7.720 | 7.194 | 6.693 | 7.552 |
| 26 | 33 | 6.785 | 7.993 | 5.873 | 7.832 | 3.297 | 3.005 | 2.855 | 3.229 | 4.793 | 3.709 | 4.150 | 4.508 | 3.969 | 3.359 | 3.448 | 3.840 |
| 27 | 33 | 10.108 | 10.737 | 8.757 | 10.500 | 8.077 | 7.973 | 6.999 | 8.279 | 9.181 | 8.656 | 7.954 | 9.214 | 8.742 | 8.390 | 7.580 | 8.776 |
| 28 | 132 | 5.553 | 5.167 | 4.820 | 5.436 | 5.369 | 5.059 | 4.661 | 5.267 | 5.478 | 5.123 | 4.755 | 5.367 | 5.431 | 5.097 | 4.716 | 5.332 |
| 29 | 33 | 5.188 | 5.328 | 4.493 | 5.314 | 4.127 | 3.826 | 3.574 | 4.025 | 4.687 | 4.130 | 4.059 | 4.481 | 4.452 | 4.008 | 3.859 | 4.272 |
| 30 | 33 | 8.120 | 9.277 | 7.030 | 9.047 | 4.460 | 3.838 | 3.863 | 4.240 | 6.050 | 4.520 | 5.239 | 5.612 | 5.233 | 4.202 | 4.542 | 4.971 |

Table D32: IEC Simulated Results for Case 1 at $\mathbf{4 2 \%}$ penetration level and DG located at Bus 7

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.748 | 13.044 | 9.463 | 12.320 | 10.548 | 12.793 | 9.291 | 12.069 | 10.626 | 12.865 | 9.357 | 12.139 | 10.661 | 12.898 | 9.387 | 12.170 |
| 2 | 132 | 10.460 | 11.493 | 9.140 | 11.126 | 10.047 | 10.962 | 8.809 | 10.607 | 10.218 | 11.071 | 8.931 | 10.751 | 10.287 | 11.124 | 8.991 | 10.811 |
| 3 | 132 | 6.390 | 6.393 | 5.551 | 6.445 | 6.151 | 6.061 | 5.346 | 6.142 | 6.235 | 6.114 | 5.418 | 6.225 | 6.276 | 6.140 | 5.454 | 6.260 |
| 4 | 132 | 8.707 | 8.502 | 7.568 | 8.730 | 8.176 | 7.766 | 7.111 | 8.069 | 8.355 | 7.871 | 7.264 | 8.250 | 8.445 | 7.925 | 7.343 | 8.330 |
| 5 | 132 | 8.115 | 7.899 | 7.056 | 8.111 | 7.548 | 6.995 | 6.569 | 7.328 | 7.797 | 7.134 | 6.782 | 7.575 | 7.922 | 7.204 | 6.893 | 7.685 |
| 6 | 132 | 11.109 | 10.795 | 9.661 | 11.106 | 9.615 | 8.944 | 8.369 | 9.374 | 10.001 | 9.162 | 8.700 | 9.774 | 10.206 | 9.278 | 8.883 | 9.962 |
| 7 | 132 | 9.041 | 10.093 | 7.837 | 9.863 | 6.487 | 5.869 | 5.631 | 6.386 | 7.416 | 6.338 | 6.432 | 7.044 | 7.999 | 6.625 | 6.958 | 7.602 |
| 8 | 132 | 7.715 | 7.703 | 6.713 | 7.767 | 7.166 | 6.989 | 6.241 | 7.108 | 7.322 | 7.085 | 6.373 | 7.266 | 7.400 | 7.134 | 6.442 | 7.336 |
| 9 | 33 | 23.655 | 27.278 | 20.551 | 26.624 | 16.019 | 16.115 | 13.918 | 16.317 | 16.126 | 16.184 | 14.009 | 16.376 | 16.185 | 16.224 | 14.061 | 16.420 |
| 10 | 33 | 28.813 | 32.515 | 25.013 | 31.990 | 19.254 | 18.056 | 16.708 | 19.083 | 19.363 | 18.116 | 16.800 | 19.145 | 19.423 | 18.151 | 16.852 | 19.189 |
| 11 | 11 | 25.945 | 30.197 | 22.591 | 28.739 | 23.054 | 27.545 | 20.086 | 26.232 | 23.104 | 27.590 | 20.127 | 26.261 | 23.132 | 27.617 | 20.152 | 26.282 |
| 12 | 33 | 16.462 | 15.894 | 14.291 | 16.268 | 16.135 | 15.084 | 14.010 | 15.939 | 16.200 | 15.120 | 14.065 | 15.979 | 16.233 | 15.139 | 14.094 | 16.005 |
| 13 | 11 | 25.775 | 31.095 | 22.407 | 30.070 | 25.538 | 30.866 | 22.202 | 29.834 | 25.580 | 30.906 | 22.238 | 29.862 | 25.603 | 30.928 | 22.258 | 29.880 |
| 14 | 33 | 8.337 | 7.929 | 7.224 | 8.192 | 8.256 | 7.710 | 7.155 | 8.060 | 8.273 | 7.719 | 7.169 | 8.071 | 8.280 | 7.724 | 7.175 | 8.078 |
| 15 | 33 | 13.425 | 12.719 | 11.637 | 13.168 | 13.088 | 11.941 | 11.346 | 12.696 | 13.128 | 11.963 | 11.380 | 12.723 | 13.147 | 11.973 | 11.397 | 12.738 |
| 16 | 33 | 10.786 | 10.696 | 9.348 | 10.758 | 10.243 | 9.726 | 8.879 | 10.116 | 10.270 | 9.742 | 8.902 | 10.133 | 10.284 | 9.750 | 8.914 | 10.144 |
| 17 | 33 | 15.860 | 16.250 | 13.749 | 16.066 | 13.403 | 12.518 | 11.620 | 13.156 | 13.452 | 12.546 | 11.662 | 13.187 | 13.478 | 12.561 | 11.684 | 13.207 |
| 18 | 33 | 8.992 | 8.605 | 7.790 | 8.888 | 8.669 | 7.980 | 7.511 | 8.389 | 8.686 | 7.989 | 7.525 | 8.400 | 8.694 | 7.994 | 7.532 | 8.407 |
| 19 | 33 | 9.728 | 9.278 | 8.428 | 9.644 | 9.163 | 8.317 | 7.939 | 8.816 | 9.182 | 8.327 | 7.955 | 8.834 | 9.191 | 8.332 | 7.963 | 8.842 |
| 20 | 33 | 10.336 | 10.089 | 8.955 | 10.308 | 9.510 | 8.768 | 8.240 | 9.215 | 9.532 | 8.780 | 8.259 | 9.230 | 9.543 | 8.787 | 8.269 | 9.239 |
| 21 | 33 | 19.186 | 19.738 | 16.633 | 19.562 | 15.428 | 14.113 | 13.377 | 14.981 | 15.494 | 14.149 | 13.432 | 15.022 | 15.527 | 14.167 | 13.461 | 15.048 |
| 22 | 33 | 18.326 | 18.884 | 15.887 | 18.675 | 14.975 | 13.815 | 12.982 | 14.617 | 15.038 | 13.849 | 13.035 | 14.657 | 15.069 | 13.867 | 13.063 | 14.682 |
| 23 | 33 | 8.665 | 8.363 | 7.507 | 8.582 | 8.473 | 7.936 | 7.341 | 8.267 | 8.491 | 7.946 | 7.356 | 8.279 | 8.499 | 7.950 | 7.363 | 8.286 |
| 24 | 33 | 11.453 | 11.093 | 9.922 | 11.433 | 10.904 | 10.074 | 9.448 | 10.556 | 10.936 | 10.091 | 9.474 | 10.578 | 10.951 | 10.100 | 9.487 | 10.590 |
| 25 | 33 | 6.994 | 6.846 | 6.059 | 6.923 | 6.941 | 6.721 | 6.013 | 6.883 | 6.958 | 6.732 | 6.027 | 6.894 | 6.966 | 6.737 | 6.035 | 6.901 |
| 26 | 33 | 3.068 | 2.889 | 2.657 | 3.038 | 3.060 | 2.870 | 2.650 | 3.016 | 3.063 | 2.871 | 2.653 | 3.019 | 3.064 | 2.872 | 2.654 | 3.020 |
| 27 | 33 | 8.050 | 7.984 | 6.975 | 8.127 | 8.002 | 7.918 | 6.934 | 8.111 | 8.028 | 7.933 | 6.956 | 8.126 | 8.041 | 7.942 | 6.968 | 8.136 |
| 28 | 132 | 5.721 | 5.527 | 4.965 | 5.674 | 5.375 | 5.064 | 4.667 | 5.256 | 5.480 | 5.124 | 4.757 | 5.363 | 5.533 | 5.156 | 4.804 | 5.410 |
| 29 | 33 | 4.091 | 3.812 | 3.543 | 3.996 | 4.081 | 3.799 | 3.535 | 3.976 | 4.087 | 3.803 | 3.540 | 3.981 | 4.089 | 3.804 | 3.542 | 3.984 |
| 30 | 33 | 4.291 | 3.763 | 3.717 | 4.165 | 4.282 | 3.751 | 3.709 | 4.146 | 4.287 | 3.754 | 3.713 | 4.151 | 4.290 | 3.755 | 3.716 | 4.153 |

Table D33: IEC Simulated Results for Case 2 at 42\% penetration level and DG located at Bus 26

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.623 | 12.862 | 9.355 | 12.138 | 10.554 | 12.797 | 9.295 | 12.081 | 10.561 | 12.804 | 9.301 | 12.089 | 10.564 | 12.806 | 9.303 | 12.091 |
| 2 | 132 | 10.199 | 11.057 | 8.915 | 10.740 | 10.071 | 10.959 | 8.804 | 10.636 | 10.082 | 10.967 | 8.814 | 10.649 | 10.086 | 10.970 | 8.817 | 10.652 |
| 3 | 132 | 6.248 | 6.122 | 5.429 | 6.237 | 6.153 | 6.062 | 5.348 | 6.160 | 6.163 | 6.068 | 5.356 | 6171 | 6.167 | 6.071 | 5.360 | 6.174 |
| 4 | 132 | 8.387 | 7.890 | 7.292 | 8.280 | 8.174 | 7.765 | 7.108 | 8.101 | 8.194 | 7.777 | 7.125 | 8.126 | 8.203 | 7.782 | 7.133 | 8.133 |
| 5 | 132 | 7.551 | 6.997 | 6.569 | 7.387 | 7.501 | 6.969 | 6.526 | 7.349 | 7.505 | 6.971 | 6.530 | 7.354 | 7.507 | 6.972 | 6.531 | 7.355 |
| 6 | 132 | 10.311 | 9.334 | 8.972 | 10.044 | 9.581 | 8.925 | 8.337 | 9.424 | 9.616 | 8.946 | 8.367 | 9.468 | 9.633 | 8.956 | 8.382 | 9.483 |
| 7 | 132 | 6.278 | 5.748 | 5.448 | 6.107 | 6.148 | 5.675 | 5.335 | 6.002 | 6.156 | 5.679 | 5.342 | 6.011 | 6.159 | 5.681 | 5.345 | 6.014 |
| 8 | 132 | 7.449 | 7.164 | 6.484 | 7.374 | 7.170 | 6.991 | 6.242 | 7.140 | 7.187 | 7.002 | 6.257 | 7.163 | 7.196 | 7.008 | 6.265 | 7.170 |
| 9 | 33 | 22.967 | 26.682 | 19.961 | 26.055 | 16.034 | 16.124 | 13.931 | 16.327 | 16.079 | 16.153 | 13.969 | 16.350 | 16.097 | 16.166 | 13.985 | 16.367 |
| 10 | 33 | 28.136 | 32.005 | 24.436 | 31.471 | 19.311 | 18.090 | 16.756 | 19.165 | 19.420 | 18.152 | 16.850 | 19.234 | 19.456 | 18.174 | 16.882 | 19.268 |
| 11 | 11 | 25.746 | 30.021 | 22.421 | 28.585 | 23.061 | 27.551 | 20.091 | 26.237 | 23.082 | 27.570 | 20.109 | 26.248 | 23.091 | 27.578 | 20.117 | 26.256 |
| 12 | 33 | 16.371 | 15.861 | 14.214 | 16.201 | 16.150 | 15.093 | 14.022 | 15.960 | 16.194 | 15.118 | 14.060 | 15.988 | 16.208 | 15.126 | 14.072 | 16.002 |
| 13 | 11 | 25.716 | 31.039 | 22.356 | 30.029 | 25.550 | 30.878 | 22.213 | 29.851 | 25.579 | 30.906 | 22.238 | 29.871 | 25.590 | 30.916 | 22.247 | 29.882 |
| 14 | 33 | 8.322 | 7.928 | 7.211 | 8.187 | 8.259 | 7.712 | 7.157 | 8.067 | 8.275 | 7.721 | 7.171 | 8.078 | 8.279 | 7.723 | 7.174 | 8.082 |
| 15 | 33 | 13.424 | 12.759 | 11.637 | 13.192 | 13.125 | 11.962 | 11.378 | 12.744 | 13.172 | 11.987 | 11.418 | 12.774 | 13.186 | 11.996 | 11.431 | 12.788 |
| 16 | 33 | 10.728 | 10.665 | 9.299 | 10.712 | 10.249 | 9.730 | 8.884 | 10.127 | 10.272 | 9.743 | 8.903 | 10.142 | 10.278 | 9.747 | 8.909 | 10.148 |
| 17 | 33 | 15.688 | 16.143 | 13.602 | 15.927 | 13.419 | 12.528 | 11.634 | 13.183 | 13.465 | 12.554 | 11.673 | 13.214 | 13.479 | 12.562 | 11.685 | 13.227 |
| 18 | 33 | 8.972 | 8.605 | 7.774 | 8.881 | 8.678 | 7.985 | 7.518 | 8.402 | 8.696 | 7.995 | 7.534 | 8.415 | 8.702 | 7.998 | 7.539 | 8.420 |
| 19 | 33 | 9.693 | 9.266 | 8.398 | 9.622 | 9.170 | 8.321 | 7.945 | 8.815 | 9.190 | 8.332 | 7.962 | 8.835 | 9.196 | 8.335 | 7.967 | 8.838 |
| 20 | 33 | 10.285 | 10.066 | 8.911 | 10.272 | 9.518 | 8.773 | 8.247 | 9.230 | 9.541 | 8.786 | 8.267 | 9.246 | 9.547 | 8.789 | 8.272 | 9.252 |
| 21 | 33 | 19.100 | 19.763 | 16.562 | 19.544 | 15.508 | 14.159 | 13.446 | 15.092 | 15.612 | 14.215 | 13.534 | 15.157 | 15.645 | 14.233 | 13.563 | 15.188 |
| 22 | 33 | 18.318 | 18.985 | 15.882 | 18.739 | 15.074 | 13.873 | 13.068 | 14.751 | 15.187 | 13.934 | 13.165 | 14.821 | 15.225 | 13.956 | 13.198 | 14.857 |
| 23 | 33 | 8.763 | 8.490 | 7.592 | 8.701 | 8.537 | 7.973 | 7.396 | 8.347 | 8.587 | 8.002 | 7.439 | 8.375 | 8.605 | 8.012 | 7.455 | 8.392 |
| 24 | 33 | 12.084 | 11.825 | 10.468 | 12.143 | 11.245 | 10.267 | 9.743 | 10.957 | 11.442 | 10.374 | 9.913 | 11.058 | 11.527 | 10.421 | 9.987 | 11.133 |
| 25 | 33 | 9.664 | 9.873 | 8.371 | 9.840 | 8.278 | 7.534 | 7.171 | 8.361 | 8.900 | 7.837 | 7.709 | 8.621 | 9.261 | 8.024 | 8.029 | 8.924 |
| 26 | 33 | 14.193 | 17.740 | 12.282 | 17.374 | 5.800 | 4.208 | 5.023 | 5.863 | 8.192 | 4.722 | 7.091 | 7.451 | 10.257 | 5.158 | 8.967 | 9.452 |
| 27 | 33 | 9.026 | 9.098 | 7.820 | 9.139 | 8.496 | 8.247 | 7.362 | 8.703 | 8.778 | 8.412 | 7.606 | 8.846 | 8.906 | 8.491 | 7.719 | 8.960 |
| 28 | 132 | 5.627 | 5.209 | 4.884 | 5.486 | 5.427 | 5.094 | 4.712 | 5.311 | 5.450 | 5.107 | 4.732 | 5.343 | 5.465 | 5.116 | 4.744 | 5.355 |
| 29 | 33 | 4.244 | 3.990 | 3.676 | 4.175 | 4.146 | 3.837 | 3.591 | 4.024 | 4.206 | 3.870 | 3.643 | 4.061 | 4.226 | 3.882 | 3.660 | 4.080 |
| 30 | 33 | 4.422 | 3.917 | 3.830 | 4.319 | 4.335 | 3.777 | 3.755 | 4.161 | 4.389 | 3.804 | 3.802 | 4.218 | 4.407 | 3.813 | 3.817 | 4.231 |

Table D34: IEC Simulated Results for Case 3 at 42\% penetration level and DG located at Bus 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.631 | 12.870 | 9.362 | 12.146 | 10.557 | 12.800 | 9.298 | 12.082 | 10.568 | 12.810 | 9.307 | 12.095 | 10.572 | 12.814 | 9.311 | 12.099 |
| 2 | 132 | 10.213 | 10.068 | 8.928 | 10.753 | 10.078 | 10.964 | 8.810 | 10.640 | 10.094 | 10.976 | 8.824 | 10.659 | 10.101 | 10.982 | 8.830 | 10.665 |
| 3 | 132 | 6.259 | 6.129 | 5.439 | 6.247 | 6.159 | 6.066 | 5.353 | 6.163 | 6.173 | 6.074 | 5.364 | 6.179 | 6.179 | 6.078 | 5.370 | 6.185 |
| 4 | 132 | 8.413 | 7.906 | 7.315 | 8.305 | 8.188 | 7.773 | 7.120 | 8.109 | 8.215 | 7.789 | 7.144 | 8.144 | 8.229 | 7.798 | 7.156 | 8.157 |
| 5 | 132 | 7.556 | 7.000 | 6.574 | 7.392 | 7.503 | 6.970 | 6.528 | 7.350 | 7.510 | 6.973 | 6.534 | 7.357 | 7.512 | 6.975 | 6.536 | 7.359 |
| 6 | 132 | 10.385 | 9.374 | 9.036 | 10.113 | 9.624 | 8.950 | 8.375 | 9.451 | 9.674 | 8.979 | 8.417 | 9.520 | 9.703 | 8.996 | 8.443 | 9.547 |
| 7 | 132 | 6.291 | 5.755 | 5.459 | 6.119 | 6.155 | 5.679 | 5.341 | 6.006 | 6.167 | 5.685 | 5.351 | 6.021 | 6.173 | 5.689 | 5.356 | 6.025 |
| 8 | 132 | 7.492 | 7.190 | 6.521 | 7.413 | 7.194 | 7.006 | 6.264 | 7.155 | 7.221 | 7.023 | 6.287 | 7.192 | 7.237 | 7.033 | 6.300 | 7.206 |
| 9 | 33 | 23.015 | 26.720 | 20.002 | 26.084 | 16.025 | 16.118 | 13.922 | 16.314 | 16.064 | 16.143 | 13.956 | 16.331 | 16.082 | 16.155 | 13.972 | 16.346 |
| 10 | 33 | 28.130 | 31.962 | 24.429 | 31.432 | 19.268 | 18.064 | 16.719 | 19.106 | 19.349 | 18.110 | 16.788 | 19.155 | 19.378 | 18.127 | 16.814 | 19.181 |
| 11 | 11 | 25.760 | 30.033 | 22.433 | 28.592 | 23.056 | 27.546 | 20.087 | 26.230 | 23.074 | 27.562 | 20.102 | 26.238 | 23.083 | 27.571 | 20.110 | 26.246 |
| 12 | 33 | 16.357 | 15.838 | 14.202 | 16.184 | 16.139 | 15.086 | 14.013 | 15.943 | 16.174 | 15.106 | 14.043 | 15.965 | 16.187 | 15.113 | 14.054 | 15.976 |
| 13 | 11 | 25.704 | 31.028 | 22.347 | 30.014 | 25.540 | 30.869 | 22.205 | 29.837 | 25.564 | 30.891 | 22.224 | 29.852 | 25.573 | 30.899 | 22.232 | 29.861 |
| 14 | 33 | 8.317 | 7.919 | 7.207 | 8.179 | 8.257 | 7.710 | 7.155 | 8.062 | 8.269 | 7.717 | 7.166 | 8.070 | 8.272 | 7.719 | 7.168 | 8.073 |
| 15 | 33 | 13.389 | 12.713 | 11.607 | 13.151 | 13.100 | 11.948 | 11.356 | 12.713 | 13.135 | 11.967 | 11.387 | 12.736 | 13.146 | 11.973 | 11.396 | 12.746 |
| 16 | 33 | 10.726 | 10.659 | 9.297 | 10.708 | 10.245 | 9.727 | 8.880 | 10.119 | 10.262 | 9.737 | 8.895 | 10.130 | 10.267 | 9.741 | 8.899 | 10.135 |
| 17 | 33 | 15.688 | 16.134 | 13.602 | 15.922 | 13.406 | 12.520 | 11.623 | 13.163 | 13.441 | 12.540 | 11.653 | 13.186 | 13.453 | 12.547 | 11.662 | 13.196 |
| 18 | 33 | 8.965 | 8.593 | 7.767 | 8.871 | 8.671 | 7.981 | 7.513 | 8.393 | 8.686 | 7.989 | 7.525 | 8.403 | 8.690 | 7.991 | 7.528 | 8.407 |
| 19 | 33 | 9.688 | 9.257 | 8.394 | 9.615 | 9.165 | 8.318 | 7.940 | 8.815 | 9.180 | 8.326 | 7.953 | 8.830 | 9.184 | 8.328 | 7.957 | 8.833 |
| 20 | 33 | 10.281 | 10.058 | 8.908 | 10.266 | 9.512 | 8.769 | 8.242 | 9.220 | 9.529 | 8.779 | 8.257 | 9.232 | 9.534 | 8.782 | 8.261 | 9.236 |
| 21 | 33 | 19.021 | 19.653 | 16.493 | 19.445 | 15.450 | 14.125 | 13.395 | 15.018 | 15.522 | 14.165 | 13.457 | 15.065 | 15.546 | 14.178 | 13.477 | 15.087 |
| 22 | 33 | 18.210 | 18.842 | 15.788 | 18.608 | 15.001 | 13.830 | 13.005 | 14.662 | 15.080 | 13.873 | 13.072 | 14.713 | 15.105 | 13.888 | 13.094 | 14.737 |
| 23 | 33 | 8.693 | 8.406 | 7.531 | 8.624 | 8.490 | 7.946 | 7.355 | 8.294 | 8.524 | 7.965 | 7.385 | 8.316 | 8.535 | 7.971 | 7.394 | 8.326 |
| 24 | 33 | 11.678 | 11.366 | 10.117 | 11.708 | 10.988 | 10.122 | 9.520 | 10.684 | 11.114 | 10.192 | 9.629 | 10.762 | 11.157 | 10.216 | 9.666 | 10.801 |
| 25 | 33 | 7.819 | 7.806 | 6.773 | 7.878 | 7.247 | 6.918 | 6.279 | 7.296 | 7.549 | 7.092 | 6.539 | 7.467 | 7.671 | 7.165 | 6.647 | 7.576 |
| 26 | 33 | 3.175 | 3.018 | 2.750 | 3.168 | 3.091 | 2.887 | 2.677 | 3.017 | 3.141 | 2.916 | 2.720 | 3.069 | 3.158 | 2.926 | 2.735 | 3.081 |
| 27 | 33 | 10.958 | 11.474 | 9.494 | 11.246 | 9.118 | 8.667 | 7.902 | 9.498 | 10.008 | 9.133 | 8.670 | 9.960 | 10.455 | 9.381 | 9.067 | 10.340 |
| 28 | 132 | 5.740 | 5.273 | 4.982 | 5.590 | 5.496 | 5.134 | 4.772 | 5.356 | 5.533 | 5.155 | 4.803 | 5.416 | 5.562 | 5.173 | 4.829 | 5.444 |
| 29 | 33 | 15.278 | 18.937 | 13.222 | 18.485 | 6.457 | 5.092 | 5.593 | 6.672 | 9.224 | 5.808 | 7.986 | 8.296 | 11.324 | 6.329 | 9.891 | 10.317 |
| 30 | 33 | 6.196 | 5.982 | 5.366 | 6.268 | 5.025 | 4.111 | 4.353 | 4.839 | 5.563 | 4.330 | 4.818 | 5.157 | 5.853 | 4.448 | 5.075 | 5.412 |

Table D35: IEC Simulated Results for Case 4 at 42\% penetration level and DG located at Bus 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.626 | 12.865 | 9.357 | 12.141 | 10.554 | 12.797 | 9.295 | 12.080 | 10.564 | 12.806 | 9.303 | 12.091 | 10.567 | 12.810 | 9.306 | 12.094 |
| 2 | 132 | 10.204 | 11.061 | 8.919 | 10.745 | 10.071 | 10.959 | 8.805 | 10.636 | 10.087 | 10.971 | 8.818 | 10.653 | 10.092 | 10.975 | 8.823 | 10.658 |
| 3 | 132 | 6.251 | 6.124 | 5.432 | 6.240 | 6.153 | 6.062 | 5.348 | 6.159 | 6.166 | 6.070 | 5.359 | 6.174 | 6.171 | 6.074 | 5.363 | 6.178 |
| 4 | 132 | 8.393 | 7.894 | 7.298 | 8.288 | 8.174 | 7.765 | 7.109 | 8.100 | 8.200 | 7.780 | 7.130 | 8.131 | 8.212 | 7.788 | 7.141 | 8.142 |
| 5 | 132 | 7.553 | 6.998 | 6.571 | 7.390 | 7.501 | 6.969 | 6.527 | 7.349 | 7.507 | 6.972 | 6.531 | 7.355 | 7.509 | 6.973 | 6.533 | 7.357 |
| 6 | 132 | 10.337 | 9.348 | 8.995 | 10.072 | 9.594 | 8.933 | 8.348 | 9.429 | 9.641 | 8.960 | 8.388 | 9.491 | 9.666 | 8.975 | 8.411 | 9.514 |
| 7 | 132 | 6.283 | 5.750 | 5.452 | 6.112 | 6.150 | 5.676 | 5.337 | 6.002 | 6.161 | 5.682 | 5.346 | 6.015 | 6.166 | 5.685 | 5.350 | 6.019 |
| 8 | 132 | 7.469 | 7.176 | 6.501 | 7.393 | 7.179 | 6.996 | 6.250 | 7.144 | 7.204 | 7.012 | 6.272 | 7.177 | 7.217 | 7.021 | 6.284 | 7.189 |
| 9 | 33 | 22.961 | 26.672 | 19.956 | 26.037 | 16.008 | 16.106 | 13.908 | 16.297 | 16.044 | 16.130 | 13.939 | 16.314 | 16.060 | 16.140 | 13.952 | 16.328 |
| 10 | 33 | 28.044 | 31.887 | 24.355 | 31.356 | 19.245 | 18.051 | 16.700 | 19.081 | 19.318 | 18.092 | 16.762 | 19.127 | 19.343 | 18.106 | 16.783 | 19.149 |
| 11 | 11 | 25.743 | 30.018 | 22.419 | 28.579 | 23.047 | 27.538 | 20.079 | 26.221 | 23.064 | 27.553 | 20.093 | 26.229 | 23.072 | 27.560 | 20.100 | 26.236 |
| 12 | 33 | 16.340 | 15.826 | 14.187 | 16.169 | 16.129 | 15.081 | 14.005 | 15.933 | 16.161 | 15.098 | 14.032 | 15.953 | 16.172 | 15.105 | 14.041 | 15.962 |
| 13 | 11 | 25.692 | 31.016 | 22.336 | 30.002 | 25.533 | 30.862 | 22.198 | 29.829 | 25.554 | 30.881 | 22.216 | 29.843 | 25.562 | 30.889 | 22.223 | 29.850 |
| 14 | 33 | 8.313 | 7.916 | 7.203 | 8.176 | 8.255 | 7.709 | 7.154 | 8.059 | 8.266 | 7.715 | 7.163 | 8.067 | 8.268 | 7.717 | 7.165 | 8.070 |
| 15 | 33 | 13.374 | 12.702 | 11.594 | 13.138 | 13.092 | 11.944 | 11.350 | 12.704 | 13.123 | 11.961 | 11.377 | 12.725 | 13.133 | 11.966 | 11.385 | 12.734 |
| 16 | 33 | 10.717 | 10.653 | 9.290 | 10.701 | 10.241 | 9.725 | 8.877 | 10.114 | 10.256 | 9.734 | 8.890 | 10.124 | 10.261 | 9.737 | 8.894 | 10.129 |
| 17 | 33 | 15.666 | 16.118 | 13.583 | 15.904 | 13.398 | 12.516 | 11.616 | 13.154 | 13.429 | 12.533 | 11.642 | 13.175 | 13.439 | 12.539 | 11.651 | 13.184 |
| 18 | 33 | 8.959 | 8.589 | 7.762 | 8.866 | 8.669 | 7.980 | 7.511 | 8.390 | 8.682 | 7.987 | 7.521 | 8.399 | 8.685 | 7.989 | 7.524 | 8.402 |
| 19 | 33 | 9.681 | 9.253 | 8.388 | 9.609 | 9.162 | 8.316 | 7.938 | 8.814 | 9.176 | 8.323 | 7.949 | 8.827 | 9.179 | 8.325 | 7.953 | 8.829 |
| 20 | 33 | 10.273 | 10.052 | 8.901 | 10.259 | 9.509 | 8.767 | 8.239 | 9.216 | 9.524 | 8.776 | 8.252 | 9.227 | 9.528 | 8.778 | 8.256 | 9.231 |
| 21 | 33 | 18.972 | 19.615 | 16.451 | 19.402 | 15.434 | 14.116 | 13.381 | 14.999 | 15.498 | 14.152 | 13.436 | 15.042 | 15.518 | 14.163 | 13.453 | 15.061 |
| 22 | 33 | 18.159 | 18.801 | 15.744 | 18.563 | 14.983 | 13.820 | 12.990 | 14.642 | 15.053 | 13.859 | 13.050 | 14.688 | 15.075 | 13.871 | 13.068 | 14.708 |
| 23 | 33 | 8.678 | 8.394 | 7.518 | 8.610 | 8.483 | 7.941 | 7.349 | 8.285 | 8.513 | 7.959 | 7.375 | 8.305 | 8.522 | 7.964 | 7.383 | 8.314 |
| 24 | 33 | 11.614 | 11.312 | 10.062 | 11.648 | 10.958 | 10.105 | 9.494 | 10.649 | 11.069 | 10.167 | 9.590 | 10.721 | 11.106 | 10.187 | 9.622 | 10.754 |
| 25 | 33 | 7.645 | 7.644 | 6.623 | 7.704 | 7.158 | 6.862 | 6.201 | 7.198 | 7.422 | 7.016 | 6.429 | 7.354 | 7.523 | 7.077 | 6.518 | 7.444 |
| 26 | 33 | 3.153 | 2.998 | 2.731 | 3.146 | 3.080 | 2.881 | 2.667 | 3.012 | 3.124 | 2.906 | 2.705 | 3.056 | 3.138 | 2.914 | 2.718 | 3.067 |
| 27 | 33 | 10.289 | 10.793 | 8.914 | 10.594 | 8.816 | 8.472 | 7.639 | 9.170 | 9.561 | 8.881 | 8.283 | 9.576 | 9.908 | 9.081 | 8.591 | 9.875 |
| 28 | 132 | 5.696 | 5.248 | 4.944 | 5.550 | 5.464 | 5.115 | 4.743 | 5.331 | 5.500 | 5.136 | 4.775 | 5.386 | 5.525 | 5.151 | 4.797 | 5.410 |
| 29 | 33 | 5.863 | 8.989 | 5.077 | 6.009 | 4.738 | 4.174 | 4.104 | 4.726 | 5.261 | 4.414 | 4.556 | 4.989 | 5.535 | 4.543 | 4.800 | 5.215 |
| 30 | 33 | 15.504 | 19.135 | 13.417 | 18.637 | 6.550 | 4.826 | 5.674 | 6.591 | 9.424 | 5.501 | 8.159 | 8.473 | 11.539 | 5.953 | 10.076 | 10.495 |

Table D36: IEC Simulated Results for Case 5 at 42\% penetration level and DG located at Bus 7 and 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.710 | 12.991 | 9.430 | 12.265 | 10.549 | 12.794 | 9.292 | 12.067 | 10.604 | 12.844 | 9.338 | 12.122 | 10.629 | 12.868 | 9.360 | 12.144 |
| 2 | 132 | 10.374 | 11.362 | 9.066 | 11.001 | 10.071 | 10.959 | 8.806 | 10.617 | 10.169 | 11.034 | 8.889 | 10.715 | 10.216 | 11.071 | 8.931 | 10.757 |
| 3 | 132 | 6.352 | 6.318 | 5.518 | 6.383 | 6.152 | 6.061 | 5.347 | 6.147 | 6.214 | 6.101 | 5.400 | 6.210 | 6.244 | 6.120 | 5.427 | 6.236 |
| 4 | 132 | 8.622 | 8.329 | 7.494 | 8.595 | 8.176 | 7.766 | 7.111 | 8.080 | 8.308 | 7.844 | 7.224 | 8.215 | 8.375 | 7.884 | 7.283 | 8.275 |
| 5 | 132 | 7.881 | 7.589 | 6.854 | 7.825 | 7.519 | 6.979 | 6.543 | 7.332 | 7.666 | 7.061 | 6.669 | 7.475 | 7.742 | 7.105 | 6.736 | 7.542 |
| 6 | 132 | 10.894 | 10.361 | 9.475 | 10.776 | 9.611 | 8.942 | 8.365 | 9.396 | 9.889 | 9.100 | 8.603 | 9.688 | 10.038 | 9.185 | 8.736 | 9.825 |
| 7 | 132 | 7.677 | 8.075 | 6.657 | 8.001 | 6.308 | 5.765 | 5.475 | 6.131 | 6.799 | 6.028 | 5.898 | 6.537 | 7.096 | 6.187 | 6.166 | 6.821 |
| 8 | 132 | 7.667 | 7.566 | 6.672 | 7.668 | 7.177 | 6.995 | 6.249 | 7.123 | 7.296 | 7.069 | 6.351 | 7.248 | 7.357 | 7.108 | 6.406 | 7.304 |
| 9 | 33 | 23.490 | 27.137 | 20.410 | 26.487 | 16.016 | 16.113 | 13.916 | 16.317 | 16.120 | 16.180 | 14.004 | 16.377 | 16.173 | 16.216 | 14.051 | 16.418 |
| 10 | 33 | 28.690 | 32.431 | 24.909 | 31.898 | 19.247 | 18.053 | 16.702 | 19.091 | 19.390 | 18.133 | 16.823 | 19.183 | 19.454 | 18.170 | 16.879 | 19.235 |
| 11 | 11 | 25.898 | 30.155 | 22.551 | 28.703 | 23.053 | 27.544 | 20.085 | 26.232 | 23.102 | 27.588 | 20.126 | 26.261 | 23.127 | 27.612 | 20.148 | 26.281 |
| 12 | 33 | 16.451 | 15.895 | 14.282 | 16.260 | 16.130 | 15.082 | 14.006 | 15.939 | 16.202 | 15.122 | 14.067 | 15.987 | 16.234 | 15.140 | 14.095 | 16.013 |
| 13 | 11 | 25.769 | 31.090 | 22.402 | 30.070 | 25.535 | 30.864 | 22.200 | 29.835 | 25.583 | 30.909 | 22.241 | 29.868 | 25.605 | 30.931 | 22.260 | 29.888 |
| 14 | 33 | 8.336 | 7.931 | 7.224 | 8.194 | 8.254 | 7.709 | 7.153 | 8.059 | 8.274 | 7.720 | 7.170 | 8.074 | 8.281 | 7.724 | 7.176 | 8.081 |
| 15 | 33 | 13.440 | 12.742 | 11.650 | 13.192 | 13.087 | 11.941 | 11.346 | 12.702 | 13.143 | 11.971 | 11.393 | 12.741 | 13.165 | 11.983 | 11.412 | 12.760 |
| 16 | 33 | 10.776 | 10.691 | 9.340 | 10.749 | 10.240 | 9.725 | 8.876 | 10.116 | 10.272 | 9.743 | 8.904 | 10.138 | 10.286 | 9.751 | 8.915 | 10.149 |
| 17 | 33 | 15.829 | 16.231 | 13.722 | 16.042 | 13.398 | 12.516 | 11.616 | 13.157 | 13.460 | 12.550 | 11.668 | 13.199 | 13.486 | 12.566 | 11.691 | 13.221 |
| 18 | 33 | 8.992 | 8.609 | 7.790 | 8.892 | 8.667 | 7.979 | 7.509 | 8.389 | 8.690 | 7.991 | 7.529 | 8.406 | 8.699 | 7.996 | 7.536 | 8.414 |
| 19 | 33 | 9.724 | 9.279 | 8.424 | 9.643 | 9.160 | 8.315 | 7.937 | 8.812 | 9.185 | 8.329 | 7.958 | 8.835 | 9.195 | 8.334 | 7.966 | 8.842 |
| 20 | 33 | 10.328 | 10.087 | 8.949 | 10.304 | 9.507 | 8.767 | 8.238 | 9.216 | 9.536 | 8.783 | 8.262 | 9.237 | 9.547 | 8.789 | 8.272 | 9.247 |
| 21 | 33 | 19.209 | 19.784 | 16.654 | 19.607 | 15.426 | 14.112 | 13.374 | 14.995 | 15.533 | 14.170 | 13.465 | 15.069 | 15.575 | 14.194 | 13.503 | 15.105 |
| 22 | 33 | 18.375 | 18.955 | 15.929 | 18.748 | 14.974 | 13.815 | 12.981 | 14.634 | 15.084 | 13.876 | 13.076 | 14.712 | 15.128 | 13.901 | 13.115 | 14.749 |
| 23 | 33 | 8.705 | 8.412 | 7.542 | 8.633 | 8.476 | 7.937 | 7.343 | 8.278 | 8.517 | 7.961 | 7.379 | 8.308 | 8.533 | 7.970 | 7.392 | 8.322 |
| 24 | 33 | 11.670 | 11.352 | 10.110 | 11.699 | 10.926 | 10.087 | 9.467 | 10.614 | 11.066 | 10.164 | 9.587 | 10.711 | 11.117 | 10.193 | 9.631 | 10.757 |
| 25 | 33 | 7.654 | 7.663 | 6.630 | 7.729 | 7.060 | 6.800 | 6.116 | 7.088 | 7.361 | 6.979 | 6.376 | 7.285 | 7.484 | 7.054 | 6.485 | 7.391 |
| 26 | 33 | 3.156 | 3.002 | 2.733 | 3.151 | 3.068 | 2.874 | 2.657 | 3.006 | 3.117 | 2.902 | 2.700 | 3.054 | 3.134 | 2.912 | 2.715 | 3.067 |
| 27 | 33 | 10.234 | 10.791 | 8.865 | 10.543 | 8.491 | 8.259 | 7.358 | 8.813 | 9.313 | 8.732 | 8.069 | 9.313 | 9.710 | 8.966 | 8.422 | 9.643 |
| 28 | 132 | 5.822 | 5.513 | 5.052 | 5.727 | 5.437 | 5.099 | 4.721 | 5.298 | 5.546 | 5.163 | 4.814 | 5.422 | 5.607 | 5.198 | 4.868 | 5.478 |
| 29 | 33 | 9.657 | 11.649 | 8.359 | 11.372 | 5.092 | 4.385 | 4.411 | 5.193 | 6.661 | 5.000 | 5.767 | 6.130 | 7.702 | 5.385 | 6.713 | 7.146 |
| 30 | 33 | 5.682 | 5.528 | 4.921 | 5.766 | 4.614 | 3.915 | 3.997 | 4.417 | 5.100 | 4.136 | 4.417 | 4.793 | 5.345 | 4.245 | 4.635 | 5.013 |

Table D37: IEC Simulated Results for Case 6 at 42\% penetration level and DG located at Bus 26 and 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.635 | 12.874 | 9.365 | 12.148 | 10.553 | 12.796 | 9.294 | 12.078 | 10.568 | 12.810 | 9.307 | 12.094 | 10.573 | 12.815 | 9.311 | 12.099 |
| 2 | 132 | 10.220 | 11.074 | 8.934 | 10.757 | 10.070 | 10.958 | 8.804 | 10.633 | 10.094 | 10.976 | 8.824 | 10.658 | 10.103 | 10.983 | 8.832 | 10.666 |
| 3 | 132 | 6.267 | 6.134 | 5.446 | 6.252 | 6.153 | 6.062 | 5.348 | 6.157 | 6.173 | 6.075 | 5.365 | 6.179 | 6.182 | 6.080 | 5.372 | 6.186 |
| 4 | 132 | 8.431 | 7.916 | 7.331 | 8.318 | 8.175 | 7.765 | 7.109 | 8.096 | 8.217 | 7.791 | 7.145 | 8.144 | 8.236 | 7.802 | 7.162 | 8.161 |
| 5 | 132 | 7.558 | 7.001 | 6.576 | 7.393 | 7.501 | 6.968 | 6.526 | 7.348 | 7.509 | 6.973 | 6.533 | 7.357 | 7.512 | 6.975 | 6.536 | 7.359 |
| 6 | 132 | 10.420 | 9.393 | 9.066 | 10.138 | 9.593 | 8.932 | 8.348 | 9.421 | 9.671 | 8.977 | 8.414 | 9.514 | 9.708 | 8.999 | 8.448 | 9.548 |
| 7 | 132 | 6.297 | 5.758 | 5.464 | 6.123 | 6.149 | 5.675 | 5.336 | 6.000 | 6.166 | 5.685 | 5.351 | 6.019 | 6.174 | 5.689 | 5.357 | 6.025 |
| 8 | 132 | 7.504 | 7.197 | 6.532 | 7.421 | 7.176 | 6.995 | 6.248 | 7.138 | 7.217 | 7.021 | 6.283 | 7.187 | 7.236 | 7.033 | 6.300 | 7.204 |
| 9 | 33 | 23.082 | 26.785 | 20.060 | 26.153 | 16.021 | 16.116 | 13.920 | 16.322 | 16.096 | 16.164 | 13.983 | 16.364 | 16.126 | 16.185 | 14.009 | 16.390 |
| 10 | 33 | 28.299 | 32.149 | 24.576 | 31.610 | 19.267 | 18.065 | 16.719 | 19.131 | 19.430 | 18.158 | 16.859 | 19.240 | 19.486 | 18.191 | 16.908 | 19.291 |
| 11 | 11 | 25.780 | 30.051 | 22.451 | 28.612 | 23.055 | 27.546 | 20.087 | 26.235 | 23.090 | 27.577 | 20.116 | 26.255 | 23.105 | 27.592 | 20.129 | 26.268 |
| 12 | 33 | 16.401 | 15.882 | 14.240 | 16.226 | 16.134 | 15.084 | 14.009 | 15.948 | 16.201 | 15.122 | 14.066 | 15.994 | 16.224 | 15.135 | 14.086 | 16.015 |
| 13 | 11 | 25.737 | 31.059 | 22.375 | 30.048 | 25.539 | 30.868 | 22.204 | 29.843 | 25.584 | 30.911 | 22.242 | 29.876 | 25.601 | 30.927 | 22.256 | 29.891 |
| 14 | 33 | 8.329 | 7.933 | 7.217 | 8.193 | 8.254 | 7.708 | 7.153 | 8.062 | 8.276 | 7.721 | 7.172 | 8.079 | 8.282 | 7.725 | 7.177 | 8.085 |
| 15 | 33 | 13.446 | 12.776 | 11.656 | 13.214 | 13.103 | 11.950 | 11.359 | 12.726 | 13.172 | 11.987 | 11.418 | 12.773 | 13.194 | 12.000 | 11.438 | 12.794 |
| 16 | 33 | 10.743 | 10.676 | 9.312 | 10.724 | 10.242 | 9.726 | 8.877 | 10.121 | 10.274 | 9.745 | 8.905 | 10.144 | 10.284 | 9.751 | 8.914 | 10.153 |
| 17 | 33 | 15.729 | 16.173 | 13.638 | 15.964 | 13.402 | 12.518 | 11.619 | 13.170 | 13.470 | 12.557 | 11.677 | 13.217 | 13.491 | 12.569 | 11.696 | 13.237 |
| 18 | 33 | 8.982 | 8.612 | 7.782 | 8.890 | 8.670 | 7.980 | 7.512 | 8.396 | 8.697 | 7.995 | 7.535 | 8.415 | 8.705 | 8.000 | 7.542 | 8.423 |
| 19 | 33 | 9.704 | 9.274 | 8.408 | 9.632 | 9.162 | 8.316 | 7.938 | 8.809 | 9.192 | 8.332 | 7.963 | 8.836 | 9.200 | 8.337 | 7.971 | 8.842 |
| 20 | 33 | 10.300 | 10.076 | 8.924 | 10.285 | 9.509 | 8.768 | 8.239 | 9.222 | 9.543 | 8.786 | 8.268 | 9.247 | 9.552 | 8.792 | 8.277 | 9.256 |
| 21 | 33 | 19.174 | 19.824 | 16.626 | 19.617 | 15.459 | 14.132 | 13.403 | 15.051 | 15.609 | 14.213 | 13.532 | 15.153 | 15.659 | 14.241 | 13.575 | 15.198 |
| 22 | 33 | 18.390 | 19.047 | 15.944 | 18.812 | 15.017 | 13.840 | 13.019 | 14.703 | 15.180 | 13.931 | 13.160 | 14.814 | 15.236 | 13.962 | 13.208 | 14.865 |
| 23 | 33 | 8.775 | 8.505 | 7.602 | 8.717 | 8.506 | 7.956 | 7.370 | 8.321 | 8.578 | 7.997 | 7.432 | 8.368 | 8.604 | 8.012 | 7.454 | 8.391 |
| 24 | 33 | 12.112 | 11.882 | 10.493 | 12.199 | 11.100 | 10.187 | 9.618 | 10.835 | 11.386 | 10.343 | 9.864 | 11.009 | 11.499 | 10.406 | 9.964 | 11.108 |
| 25 | 33 | 9.623 | 10.043 | 8.334 | 9.970 | 7.738 | 7.230 | 6.704 | 7.895 | 8.604 | 7.682 | 7.452 | 8.375 | 9.045 | 7.917 | 7.844 | 8.740 |
| 26 | 33 | 8.634 | 10.558 | 7.472 | 10.353 | 4.292 | 3.544 | 3.717 | 4.340 | 5.670 | 4.031 | 4.909 | 5.264 | 6.690 | 4.374 | 5.838 | 6.278 |
| 27 | 33 | 10.579 | 11.251 | 9.165 | 10.955 | 8.625 | 8.355 | 7.474 | 9.005 | 9.581 | 8.892 | 8.300 | 9.591 | 10.023 | 9.146 | 8.694 | 9.968 |
| 28 | 132 | 5.741 | 5.273 | 4.983 | 5.588 | 5.454 | 5.110 | 4.736 | 5.319 | 5.515 | 5.145 | 4.787 | 5.398 | 5.548 | 5.165 | 4.817 | 5.430 |
| 29 | 33 | 5.474 | 5.641 | 4.740 | 5.636 | 4.408 | 3.991 | 3.818 | 4.385 | 4.906 | 4.242 | 4.248 | 4.678 | 5.147 | 4.363 | 4.464 | 4.875 |
| 30 | 33 | 9.982 | 11.934 | 8.640 | 11.621 | 5.278 | 4.250 | 4.571 | 5.228 | 6.937 | 4.827 | 6.006 | 6.356 | 8.004 | 5.167 | 6.974 | 7.388 |

Table D38: IEC Simulated Results for Case 1 at $\mathbf{8 5 \%}$ penetration level and DG located at Bus $\mathbf{7}$

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.752 | 13.048 | 9.466 | 12.323 | 10.576 | 12.820 | 9.316 | 12.109 | 10.672 | 12.908 | 9.397 | 12.176 | 10.704 | 12.939 | 9.425 | 12.205 |
| 2 | 132 | 10.472 | 11.503 | 9.150 | 11.137 | 10.140 | 11.013 | 8.867 | 10.635 | 10.313 | 11.144 | 9.013 | 10.825 | 10.375 | 11.192 | 9.068 | 10.881 |
| 3 | 132 | 6.387 | 6.391 | 5.548 | 6.443 | 6.191 | 6.087 | 5.382 | 6.160 | 6.292 | 6.150 | 5.467 | 6.269 | 6.329 | 6.174 | 5.500 | 6.302 |
| 4 | 132 | 8.700 | 8.496 | 7.560 | 8.723 | 8.274 | 7.824 | 7.197 | 8.119 | 8.485 | 7.946 | 7.376 | 8.354 | 8.567 | 7.995 | 7.449 | 8.429 |
| 5 | 132 | 8.282 | 8.003 | 7.201 | 8.246 | 7.676 | 7.068 | 6.681 | 7.449 | 7.977 | 7.232 | 6.938 | 7.716 | 8.093 | 7.297 | 7.042 | 7.821 |
| 6 | 132 | 10.824 | 10.612 | 9.410 | 10.864 | 9.851 | 9.078 | 8.575 | 9.547 | 10.310 | 9.330 | 8.967 | 10.025 | 10.501 | 9.437 | 9.139 | 10.205 |
| 7 | 132 | 10.332 | 11.123 | 8.955 | 10.916 | 7.089 | 6.205 | 6.154 | 7.073 | 8.384 | 6.783 | 7.270 | 7.860 | 9.021 | 7.069 | 7.853 | 8.494 |
| 8 | 132 | 7.623 | 7.642 | 6.633 | 7.691 | 7.253 | 7.044 | 6.317 | 7.163 | 7.436 | 7.155 | 6.472 | 7.356 | 7.507 | 7.200 | 6.535 | 7.422 |
| 9 | 33 | 16.358 | 16.335 | 14.207 | 16.554 | 16.110 | 16.177 | 13.997 | 16.414 | 16.220 | 16.245 | 14.089 | 16.453 | 16.271 | 16.280 | 14.135 | 16.490 |
| 10 | 33 | 19.595 | 18.248 | 16.998 | 19.324 | 19.343 | 18.109 | 16.785 | 19.177 | 19.456 | 18.170 | 16.880 | 19.222 | 19.508 | 18.200 | 16.926 | 19.259 |
| 11 | 11 | 23.216 | 27.693 | 20.223 | 26.350 | 23.101 | 27.589 | 20.127 | 26.283 | 23.150 | 27.632 | 20.166 | 26.300 | 23.174 | 27.656 | 20.188 | 26.317 |
| 12 | 33 | 16.327 | 15.192 | 14.174 | 16.081 | 16.180 | 15.111 | 14.049 | 15.988 | 16.250 | 15.149 | 14.108 | 16.022 | 16.280 | 15.166 | 14.134 | 16.044 |
| 13 | 11 | 25.669 | 30.990 | 22.314 | 29.938 | 25.572 | 30.900 | 22.233 | 29.873 | 25.616 | 30.940 | 22.269 | 29.894 | 25.636 | 30.959 | 22.286 | 29.910 |
| 14 | 33 | 8.300 | 7.735 | 7.192 | 8.095 | 8.263 | 7.714 | 7.160 | 8.068 | 8.283 | 7.725 | 7.177 | 8.081 | 8.290 | 7.729 | 7.183 | 8.086 |
| 15 | 33 | 13.197 | 12.001 | 11.440 | 12.781 | 13.108 | 11.952 | 11.364 | 12.719 | 13.154 | 11.977 | 11.403 | 12.746 | 13.171 | 11.987 | 11.418 | 12.760 |
| 16 | 33 | 10.322 | 9.772 | 8.946 | 10.175 | 10.259 | 9.736 | 8.893 | 10.135 | 10.290 | 9.754 | 8.919 | 10.151 | 10.302 | 9.761 | 8.930 | 10.106 |
| 17 | 33 | 13.549 | 12.601 | 11.744 | 13.264 | 13.436 | 12.538 | 11.649 | 13.193 | 13.490 | 12.568 | 11.694 | 13.219 | 13.513 | 12.581 | 11.714 | 13.236 |
| 18 | 33 | 8.715 | 8.005 | 7.550 | 8.425 | 8.677 | 7.984 | 7.517 | 8.398 | 8.697 | 7.995 | 7.535 | 8.410 | 8.704 | 7.999 | 7.541 | 8.416 |
| 19 | 33 | 9.215 | 8.345 | 7.983 | 8.861 | 9.172 | 8.322 | 7.947 | 8.820 | 9.195 | 8.334 | 7.966 | 8.844 | 9.203 | 8.338 | 7.973 | 8.851 |
| 20 | 33 | 9.572 | 8.803 | 8.293 | 9.264 | 9.521 | 8.775 | 8.250 | 9.229 | 9.548 | 8.789 | 8.272 | 9.244 | 9.557 | 8.795 | 8.281 | 9.252 |
| 21 | 33 | 15.620 | 14.217 | 13.539 | 15.123 | 15.470 | 14.137 | 13.413 | 15.028 | 15.543 | 14.176 | 13.474 | 15.065 | 15.573 | 14.192 | 13.500 | 15.087 |
| 22 | 33 | 15.157 | 13.915 | 13.138 | 14.754 | 15.014 | 13.837 | 13.016 | 14.661 | 15.084 | 13.875 | 13.075 | 14.697 | 15.112 | 13.891 | 13.100 | 14.719 |
| 23 | 33 | 8.519 | 7.962 | 7.380 | 8.304 | 8.480 | 7.940 | 7.347 | 8.276 | 8.501 | 7.952 | 7.365 | 8.289 | 8.509 | 7.956 | 7.371 | 8.295 |
| 24 | 33 | 10.990 | 10.121 | 9.520 | 10.624 | 10.918 | 10.082 | 9.460 | 10.574 | 10.956 | 10.103 | 9.492 | 10.597 | 10.969 | 10.110 | 9.503 | 10.607 |
| 25 | 33 | 6.988 | 6.750 | 6.053 | 6.919 | 6.950 | 6.727 | 6.021 | 6.894 | 6.969 | 6.739 | 6.037 | 6.904 | 6.977 | 6.744 | 6.044 | 6.910 |
| 26 | 33 | 3.068 | 2.874 | 2.657 | 3.023 | 3.061 | 2.870 | 2.651 | 3.017 | 3.065 | 2.872 | 2.654 | 3.020 | 3.066 | 2.873 | 2.655 | 3.021 |
| 27 | 33 | 8.080 | 7.967 | 7.000 | 8.167 | 8.022 | 7.931 | 6.952 | 8.133 | 8.049 | 7.947 | 6.974 | 8.144 | 8.060 | 7.954 | 6.984 | 8.152 |
| 28 | 132 | 5.683 | 5.503 | 4.931 | 5.641 | 5.435 | 5.098 | 4.719 | 5.286 | 5.557 | 5.169 | 4.824 | 5.424 | 5.606 | 5.197 | 4.866 | 5.468 |
| 29 | 33 | 4.097 | 3.808 | 3.548 | 3.990 | 4.084 | 3.801 | 3.537 | 3.977 | 4.090 | 3.805 | 3.543 | 3.984 | 4.093 | 3.806 | 3.545 | 3.987 |
| 30 | 33 | 4.296 | 3.758 | 3.721 | 4.159 | 4.285 | 3.752 | 3.711 | 4.148 | 4.291 | 3.756 | 3.716 | 4.154 | 4.293 | 3.757 | 3.718 | 4.156 |

Table D39: IEC Simulated Results for Case 2 at 85\% penetration level and DG located at Bus 26

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.568 | 12.810 | 9.307 | 12.094 | 10.560 | 12.803 | 9.300 | 12.085 | 10.565 | 12.807 | 9.304 | 12.091 | 10.566 | 12.809 | 9.305 | 12.093 |
| 2 | 132 | 10.093 | 10.976 | 8.823 | 10.657 | 10.081 | 10.966 | 8.813 | 10.644 | 10.088 | 10.972 | 8.819 | 10.653 | 10.091 | 10.974 | 8.821 | 10.655 |
| 3 | 132 | 6.174 | 6.075 | 5.365 | 6.179 | 6.163 | 6.068 | 5.356 | 6.167 | 6.169 | 6.072 | 5.361 | 6.175 | 6.172 | 6.074 | 5.364 | 6.177 |
| 4 | 132 | 8.219 | 7.792 | 7.147 | 8.144 | 8.195 | 7.777 | 7.127 | 8.119 | 8.208 | 7.785 | 7.137 | 8.135 | 8.214 | 7.789 | 7.142 | 8.140 |
| 5 | 132 | 7.509 | 6.973 | 6.533 | 7.356 | 7.504 | 6.970 | 6.529 | 7.352 | 7.507 | 6.972 | 6.531 | 7.355 | 7.508 | 6.973 | 6.532 | 7.356 |
| 6 | 132 | 9.667 | 8.975 | 8.411 | 9.508 | 9.624 | 8.950 | 8.374 | 9.460 | 9.643 | 8.961 | 8.391 | 9.489 | 9.656 | 8.969 | 8.402 | 9.500 |
| 7 | 132 | 6.165 | 5.684 | 5.350 | 6.018 | 6.156 | 5.679 | 5.342 | 6.008 | 6.161 | 5.682 | 5.346 | 6.015 | 6.163 | 5.683 | 5.348 | 6.016 |
| 8 | 132 | 7.212 | 7.018 | 6.279 | 7.182 | 7.191 | 7.004 | 6.260 | 7.158 | 7.201 | 7.010 | 6.269 | 7.173 | 7.207 | 7.014 | 6.274 | 7.178 |
| 9 | 33 | 16.128 | 16.232 | 14.012 | 16.387 | 16.078 | 16.154 | 13.968 | 16.367 | 16.105 | 16.171 | 13.992 | 16.377 | 16.118 | 16.180 | 14.003 | 16.389 |
| 10 | 33 | 19.513 | 18.341 | 16.931 | 19.279 | 19.396 | 18.140 | 16.830 | 19.246 | 19.468 | 18.181 | 16.892 | 19.285 | 19.494 | 18.196 | 16.914 | 19.310 |
| 11 | 11 | 23.107 | 27.594 | 20.131 | 26.273 | 23.083 | 27.571 | 20.110 | 26.257 | 23.095 | 27.583 | 20.121 | 26.262 | 23.102 | 27.589 | 20.126 | 26.268 |
| 12 | 33 | 16.229 | 15.184 | 14.090 | 15.997 | 16.182 | 15.112 | 14.050 | 15.991 | 16.212 | 15.128 | 14.076 | 16.008 | 16.222 | 15.134 | 14.084 | 16.018 |
| 13 | 11 | 25.606 | 30.932 | 22.261 | 29.900 | 25.574 | 30.902 | 22.234 | 29.876 | 25.593 | 30.919 | 22.250 | 29.887 | 25.600 | 30.926 | 22.256 | 29.894 |
| 14 | 33 | 8.283 | 7.740 | 7.178 | 8.073 | 8.268 | 7.717 | 7.165 | 8.076 | 8.279 | 7.723 | 7.174 | 8.083 | 8.281 | 7.724 | 7.176 | 8.086 |
| 15 | 33 | 13.209 | 12.078 | 11.451 | 12.791 | 13.160 | 11.981 | 11.408 | 12.777 | 13.191 | 11.998 | 11.435 | 12.795 | 13.201 | 12.004 | 11.444 | 12.805 |
| 16 | 33 | 10.287 | 9.776 | 8.916 | 10.141 | 10.264 | 9.739 | 8.897 | 10.141 | 10.279 | 9.748 | 8.910 | 10.150 | 10.284 | 9.750 | 8.914 | 10.155 |
| 17 | 33 | 13.499 | 12.626 | 11.702 | 13.220 | 13.451 | 12.547 | 11.661 | 13.215 | 13.482 | 12.564 | 11.688 | 13.233 | 13.492 | 12.570 | 11.696 | 13.243 |
| 18 | 33 | 8.708 | 8.028 | 7.545 | 8.414 | 8.689 | 7.991 | 7.528 | 8.414 | 8.702 | 7.998 | 7.540 | 8.422 | 8.706 | 8.000 | 7.543 | 8.426 |
| 19 | 33 | 9.203 | 8.365 | 7.973 | 8.877 | 9.183 | 8.327 | 7.956 | 8.823 | 9.197 | 8.335 | 7.968 | 8.838 | 9.201 | 8.337 | 7.971 | 8.840 |
| 20 | 33 | 9.556 | 8.823 | 8.280 | 9.244 | 9.532 | 8.781 | 8.260 | 9.244 | 9.549 | 8.790 | 8.273 | 9.254 | 9.553 | 8.792 | 8.277 | 9.259 |
| 21 | 33 | 15.697 | 14.409 | 13.608 | 15.203 | 15.587 | 14.203 | 13.514 | 15.167 | 15.656 | 14.239 | 13.573 | 15.204 | 15.680 | 14.253 | 13.593 | 15.227 |
| 22 | 33 | 15.284 | 14.156 | 13.249 | 14.882 | 15.162 | 13.922 | 13.144 | 14.835 | 15.237 | 13.963 | 13.209 | 14.875 | 15.264 | 13.978 | 13.232 | 14.901 |
| 23 | 33 | 8.635 | 8.123 | 7.481 | 8.416 | 8.580 | 7.998 | 7.433 | 8.386 | 8.612 | 8.016 | 7.461 | 8.401 | 8.625 | 8.024 | 7.472 | 8.413 |
| 24 | 33 | 11.679 | 10.911 | 10.118 | 11.370 | 11.444 | 10.377 | 9.915 | 11.134 | 11.567 | 10.442 | 10.021 | 11.181 | 11.629 | 10.476 | 10.075 | 11.236 |
| 25 | 33 | 10.060 | 10.115 | 8.714 | 10.093 | 9.088 | 7.967 | 7.873 | 9.079 | 9.497 | 8.141 | 8.226 | 9.172 | 9.790 | 8.284 | 8.484 | 9.424 |
| 26 | 33 | 25.137 | 31.544 | 21.751 | 30.793 | 9.253 | 5.211 | 8.014 | 9.111 | 13.304 | 5.540 | 11.515 | 11.867 | 17.425 | 5.970 | 15.253 | 15.769 |
| 27 | 33 | 9.145 | 9.171 | 7.924 | 9.268 | 8.791 | 8.431 | 7.617 | 8.972 | 8.971 | 8.531 | 7.773 | 9.038 | 9.066 | 8.589 | 7.856 | 9.124 |
| 28 | 132 | 5.493 | 5.132 | 4.769 | 5.377 | 5.463 | 5.114 | 4.742 | 5.341 | 5.474 | 5.121 | 4.752 | 5.361 | 5.484 | 5.127 | 4.761 | 5.370 |
| 29 | 33 | 4.259 | 3.998 | 3.689 | 4.181 | 4.193 | 3.864 | 3.632 | 4.069 | 4.233 | 3.886 | 3.667 | 4.090 | 4.248 | 3.894 | 3.679 | 4.104 |
| 30 | 33 | 4.435 | 3.921 | 3.841 | 4.324 | 4.376 | 3.797 | 3.791 | 4.191 | 4.413 | 3.816 | 3.822 | 4.232 | 4.426 | 3.822 | 3.833 | 4.241 |

Table D40: IEC Simulated Results for Case 3 at $\mathbf{8 5 \%}$ penetration level and DG located at Bus 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.580 | 12.822 | 9.318 | 12.105 | 10.568 | 12.810 | 9.307 | 12.090 | 10.575 | 12.816 | 9.312 | 12.100 | 10.578 | 12.819 | 9.315 | 12.103 |
| 2 | 132 | 10.115 | 10.993 | 8.843 | 10.676 | 10.095 | 10.978 | 8.826 | 10.654 | 10.105 | 10.985 | 8.834 | 10.668 | 10.111 | 10.989 | 8.839 | 10.672 |
| 3 | 132 | 6.192 | 6.087 | 5.381 | 6.195 | 6.175 | 6.076 | 5.367 | 6.175 | 6.183 | 6.081 | 5.373 | 6.187 | 6.188 | 6.084 | 5.377 | 6.191 |
| 4 | 132 | 8.260 | 7.816 | 7.182 | 8.181 | 8.224 | 7.794 | 7.152 | 8.139 | 8.239 | 7.803 | 7.164 | 8.163 | 8.250 | 7.810 | 7.173 | 8.172 |
| 5 | 132 | 7.517 | 6.978 | 6.540 | 7.363 | 7.509 | 6.973 | 6.533 | 7.355 | 7.513 | 6.976 | 6.537 | 7.360 | 7.515 | 6.977 | 6.539 | 7.362 |
| 6 | 132 | 9.772 | 9.034 | 8.502 | 9.602 | 9.704 | 8.995 | 8.443 | 9.518 | 9.726 | 9.008 | 8.462 | 9.562 | 9.749 | 9.022 | 8.483 | 9.583 |
| 7 | 132 | 6.185 | 5.696 | 5.367 | 6.035 | 6.170 | 5.687 | 5.354 | 6.018 | 6.177 | 5.691 | 5.360 | 6.028 | 6.181 | 5.693 | 5.363 | 6.032 |
| 8 | 132 | 7.272 | 7.055 | 6.331 | 7.234 | 7.236 | 7.032 | 6.300 | 7.190 | 7.248 | 7.040 | 6.310 | 7.214 | 7.260 | 7.048 | 6.321 | 7.225 |
| 9 | 33 | 16.121 | 16.197 | 14.005 | 16.370 | 16.072 | 16.149 | 13.963 | 16.355 | 16.094 | 16.163 | 13.981 | 16.359 | 16.108 | 16.173 | 13.994 | 16.371 |
| 10 | 33 | 19.434 | 18.203 | 16.862 | 19.195 | 19.338 | 18.105 | 16.780 | 19.173 | 19.392 | 18.135 | 16.826 | 19.198 | 19.415 | 18.148 | 16.845 | 19.218 |
| 11 | 11 | 23.102 | 27.589 | 20.126 | 26.264 | 23.079 | 27.568 | 20.107 | 26.251 | 23.089 | 27.576 | 20.115 | 26.252 | 23.096 | 27.583 | 20.121 | 26.258 |
| 12 | 33 | 16.210 | 15.141 | 14.074 | 15.980 | 16.169 | 15.103 | 14.039 | 15.972 | 16.193 | 15.117 | 14.059 | 15.983 | 16.202 | 15.122 | 14.067 | 15.992 |
| 13 | 11 | 25.590 | 30.916 | 22.247 | 29.879 | 25.562 | 30.890 | 22.224 | 29.859 | 25.577 | 30.904 | 22.236 | 29.867 | 25.584 | 30.911 | 22.242 | 29.873 |
| 14 | 33 | 8.277 | 7.725 | 7.172 | 8.070 | 8.264 | 7.714 | 7.161 | 8.069 | 8.273 | 7.719 | 7.169 | 8.075 | 8.275 | 7.721 | 7.171 | 8.077 |
| 15 | 33 | 13.166 | 12.008 | 11.413 | 12.748 | 13.125 | 11.962 | 11.378 | 12.738 | 13.150 | 11.975 | 11.400 | 12.752 | 13.159 | 11.980 | 11.407 | 12.760 |
| 16 | 33 | 10.277 | 9.753 | 8.908 | 10.134 | 10.257 | 9.735 | 8.891 | 10.131 | 10.269 | 9.742 | 8.901 | 10.138 | 10.274 | 9.744 | 8.905 | 10.142 |
| 17 | 33 | 13.473 | 12.574 | 11.680 | 13.196 | 13.433 | 12.536 | 11.646 | 13.190 | 13.457 | 12.549 | 11.666 | 13.202 | 13.466 | 12.554 | 11.674 | 13.211 |
| 18 | 33 | 8.696 | 8.003 | 7.534 | 8.404 | 8.680 | 7.986 | 7.521 | 8.402 | 8.691 | 7.992 | 7.529 | 8.408 | 8.694 | 7.994 | 7.532 | 8.411 |
| 19 | 33 | 9.191 | 8.340 | 7.963 | 8.854 | 9.174 | 8.323 | 7.949 | 8.821 | 9.186 | 8.329 | 7.958 | 8.833 | 9.189 | 8.331 | 7.961 | 8.835 |
| 20 | 33 | 9.543 | 8.795 | 8.268 | 9.233 | 9.523 | 8.776 | 8.251 | 9.231 | 9.536 | 8.783 | 8.262 | 9.239 | 9.540 | 8.785 | 8.266 | 9.243 |
| 21 | 33 | 15.588 | 14.253 | 13.514 | 15.094 | 15.504 | 14.156 | 13.442 | 15.072 | 15.555 | 14.183 | 13.485 | 15.099 | 15.574 | 14.194 | 13.501 | 15.116 |
| 22 | 33 | 15.151 | 13.973 | 13.134 | 14.746 | 15.060 | 13.863 | 13.056 | 14.720 | 15.115 | 13.894 | 13.103 | 14.750 | 15.135 | 13.905 | 13.120 | 14.768 |
| 23 | 33 | 8.554 | 8.018 | 7.410 | 8.331 | 8.514 | 7.960 | 7.377 | 8.318 | 8.539 | 7.974 | 7.397 | 8.331 | 8.547 | 7.979 | 7.405 | 8.339 |
| 24 | 33 | 11.237 | 10.415 | 9.735 | 10.900 | 11.088 | 10.178 | 9.607 | 10.780 | 11.176 | 10.226 | 9.682 | 10.825 | 11.209 | 10.245 | 9.711 | 10.855 |
| 25 | 33 | 7.928 | 7.805 | 6.867 | 7.887 | 7.531 | 7.090 | 6.524 | 7.566 | 7.739 | 7.204 | 6.704 | 7.654 | 7.839 | 7.262 | 6.791 | 7.743 |
| 26 | 33 | 3.188 | 3.015 | 2.761 | 3.167 | 3.129 | 2.909 | 2.710 | 3.043 | 3.164 | 2.929 | 2.741 | 3.084 | 3.177 | 2.937 | 2.752 | 3.093 |
| 27 | 33 | 11.562 | 11.961 | 10.017 | 11.842 | 10.113 | 9.257 | 8.763 | 10.448 | 10.768 | 9.549 | 9.329 | 10.673 | 11.169 | 9.759 | 9.683 | 11.019 |
| 28 | 132 | 5.635 | 5.213 | 4.831 | 5.504 | 5.578 | 5.181 | 4.842 | 5.426 | 5.588 | 5.187 | 4.850 | 5.462 | 5.611 | 5.200 | 4.871 | 5.484 |
| 29 | 33 | 26.227 | 32.757 | 22.696 | 31.918 | 9.727 | 6.341 | 8.425 | 9.886 | 14.340 | 6.832 | 12.413 | 12.656 | 18.500 | 7.391 | 16.182 | 16.599 |
| 30 | 33 | 6.614 | 6.312 | 5.727 | 6.639 | 5.679 | 4.390 | 4.919 | 5.435 | 6.073 | 4.528 | 5.259 | 5.566 | 6.341 | 4.627 | 5.496 | 5.790 |

Table D41: IEC Simulated Results for Case 4 at $\mathbf{8 5 \%}$ penetration level and DG located at Bus 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.574 | 12.816 | 9.312 | 12.100 | 10.563 | 12.805 | 9.302 | 12.087 | 10.569 | 12.811 | 9.308 | 12.095 | 10.572 | 12.814 | 9.310 | 12.098 |
| 2 | 132 | 10.105 | 10.985 | 8.833 | 10.667 | 10.086 | 10.971 | 8.818 | 10.647 | 10.096 | 10.978 | 8.826 | 10.660 | 10.101 | 10.982 | 8.830 | 10.664 |
| 3 | 132 | 6.183 | 6.081 | 5.373 | 6.187 | 6.167 | 6.071 | 5.360 | 6.169 | 6.175 | 6.076 | 5.366 | 6.180 | 6.179 | 6.078 | 5.370 | 6.184 |
| 4 | 132 | 8.238 | 7.803 | 7.163 | 8.162 | 8.206 | 7.783 | 7.136 | 8.125 | 8.220 | 7.792 | 7.148 | 8.147 | 8.229 | 7.798 | 7.156 | 8.155 |
| 5 | 132 | 7.513 | 6.975 | 6.537 | 7.360 | 7.506 | 6.972 | 6.531 | 7.353 | 7.510 | 6.974 | 6.534 | 7.357 | 7.512 | 6.975 | 6.536 | 7.359 |
| 6 | 132 | 9.725 | 9.008 | 8.461 | 9.561 | 9.662 | 8.972 | 8.408 | 9.486 | 9.685 | 8.985 | 8.427 | 9.526 | 9.705 | 8.997 | 8.445 | 9.545 |
| 7 | 132 | 6.177 | 5.691 | 5.359 | 6.028 | 6.163 | 5.683 | 5.348 | 6.012 | 6.169 | 5.687 | 5.353 | 6.021 | 6.173 | 5.689 | 5.356 | 6.025 |
| 8 | 132 | 7.248 | 7.040 | 6.309 | 7.213 | 7.214 | 7.019 | 6.281 | 7.173 | 7.227 | 7.027 | 6.292 | 7.195 | 7.238 | 7.033 | 6.301 | 7.205 |
| 9 | 33 | 16.093 | 16.176 | 13.981 | 16.347 | 16.048 | 16.133 | 13.943 | 16.333 | 16.069 | 16.147 | 13.960 | 16.338 | 16.082 | 16.155 | 13.971 | 16.349 |
| 10 | 33 | 19.390 | 18.173 | 16.824 | 19.158 | 19.305 | 18.086 | 16.751 | 19.139 | 19.354 | 18.113 | 16.793 | 19.163 | 19.374 | 18.125 | 16.810 | 19.181 |
| 11 | 11 | 23.088 | 27.576 | 20.114 | 26.252 | 23.067 | 27.557 | 20.097 | 26.240 | 23.077 | 27.565 | 20.104 | 26.242 | 23.083 | 27.571 | 20.110 | 26.247 |
| 12 | 33 | 16.192 | 15.128 | 14.058 | 15.964 | 16.155 | 15.095 | 14.026 | 15.957 | 16.177 | 15.107 | 14.045 | 15.968 | 16.185 | 15.112 | 14.052 | 15.976 |
| 13 | 11 | 25.577 | 30.903 | 22.236 | 29.866 | 25.552 | 30.880 | 22.214 | 29.848 | 25.566 | 30.893 | 22.226 | 29.855 | 25.572 | 30.898 | 22.231 | 29.861 |
| 14 | 33 | 8.272 | 7.722 | 7.169 | 8.066 | 8.261 | 7.712 | 7.159 | 8.065 | 8.269 | 7.717 | 7.166 | 8.071 | 8.271 | 7.718 | 7.167 | 8.073 |
| 15 | 33 | 13.149 | 11.996 | 11.399 | 12.734 | 13.113 | 11.955 | 11.368 | 12.726 | 13.136 | 11.968 | 11.388 | 12.739 | 13.144 | 11.972 | 11.394 | 12.746 |
| 16 | 33 | 10.269 | 9.747 | 8.901 | 10.127 | 10.251 | 9.731 | 8.886 | 10.125 | 10.263 | 9.738 | 8.895 | 10.131 | 10.266 | 9.740 | 8.898 | 10.135 |
| 17 | 33 | 13.457 | 12.563 | 11.666 | 13.182 | 13.421 | 12.529 | 11.635 | 13.177 | 13.443 | 12.541 | 11.654 | 13.189 | 13.450 | 12.545 | 11.660 | 13.196 |
| 18 | 33 | 8.690 | 7.999 | 7.529 | 8.399 | 8.676 | 7.984 | 7.517 | 8.398 | 8.686 | 7.989 | 7.525 | 8.404 | 8.688 | 7.991 | 7.527 | 8.406 |
| 19 | 33 | 9.185 | 8.336 | 7.958 | 8.848 | 9.170 | 8.320 | 7.945 | 8.819 | 9.180 | 8.326 | 7.954 | 8.829 | 9.183 | 8.328 | 7.956 | 8.831 |
| 20 | 33 | 9.536 | 8.790 | 8.262 | 9.227 | 9.518 | 8.773 | 8.247 | 9.226 | 9.530 | 8.779 | 8.257 | 9.233 | 9.533 | 8.781 | 8.260 | 9.236 |
| 21 | 33 | 15.554 | 14.228 | 13.484 | 15.064 | 15.479 | 14.142 | 13.420 | 15.045 | 15.526 | 14.167 | 13.460 | 15.071 | 15.541 | 14.176 | 13.473 | 15.086 |
| 22 | 33 | 15.114 | 13.945 | 13.102 | 14.714 | 15.033 | 13.848 | 13.032 | 14.691 | 15.083 | 13.876 | 13.075 | 14.720 | 15.100 | 13.885 | 13.090 | 14.736 |
| 23 | 33 | 8.538 | 8.005 | 7.397 | 8.317 | 8.503 | 7.953 | 7.367 | 8.306 | 8.525 | 7.966 | 7.386 | 8.318 | 8.532 | 7.970 | 7.392 | 8.325 |
| 24 | 33 | 11.173 | 10.362 | 9.680 | 10.839 | 11.041 | 10.152 | 9.566 | 10.732 | 11.121 | 10.196 | 9.635 | 10.774 | 11.149 | 10.212 | 9.659 | 10.800 |
| 25 | 33 | 7.733 | 7.626 | 6.698 | 7.694 | 7.392 | 7.005 | 6.404 | 7.425 | 7.577 | 7.109 | 6.563 | 7.508 | 7.659 | 7.158 | 6.636 | 7.582 |
| 26 | 33 | 3.163 | 2.993 | 2.740 | 3.143 | 3.111 | 2.899 | 2.695 | 3.033 | 3.143 | 2.917 | 2.722 | 3.068 | 3.154 | 2.924 | 2.732 | 3.076 |
| 27 | 33 | 10.746 | 11.151 | 9.310 | 11.048 | 9.603 | 8.954 | 8.321 | 9.931 | 10.142 | 9.213 | 8.787 | 10.128 | 10.449 | 9.382 | 9.058 | 10.394 |
| 28 | 132 | 5.587 | 5.186 | 4.850 | 5.461 | 5.534 | 5.156 | 4.805 | 5.391 | 5.547 | 5.163 | 4.815 | 5.425 | 5.567 | 5.175 | 4.833 | 5.443 |
| 29 | 33 | 6.270 | 6.329 | 5.430 | 6.366 | 5.363 | 4.487 | 4.645 | 5.308 | 5.747 | 4.634 | 4.977 | 5.427 | 6.005 | 4.746 | 5.205 | 5.641 |
| 30 | 33 | 26.456 | 32.965 | 22.894 | 32.078 | 9.765 | 5.901 | 8.458 | 9.733 | 14.540 | 6.373 | 12.586 | 12.838 | 18.718 | 6.849 | 16.370 | 16.780 |

Table D42: IEC Simulated Results for Case 5 at 85\% penetration level and DG located at Bus 7 and 29

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.730 | 13.027 | 9.447 | 12.305 | 10.561 | 12.806 | 9.303 | 12.086 | 10.647 | 12.885 | 9.375 | 12.155 | 10.682 | 12.918 | 9.406 | 12.186 |
| 2 | 132 | 10.420 | 11.462 | 9.105 | 11.094 | 10.100 | 10.982 | 8.832 | 10.620 | 10.256 | 11.100 | 8.964 | 10.780 | 10.323 | 11.153 | 9.023 | 10.839 |
| 3 | 132 | 6.372 | 6.381 | 5.535 | 6.430 | 6.175 | 6.076 | 5.368 | 6.154 | 6.270 | 6.136 | 5.448 | 6.251 | 6.312 | 6.163 | 5.485 | 6.288 |
| 4 | 132 | 8.667 | 8.476 | 7.533 | 8.696 | 8.235 | 7.800 | 7.163 | 8.102 | 8.437 | 7.919 | 7.335 | 8.315 | 8.530 | 7.974 | 7.417 | 8.398 |
| 5 | 132 | 8.103 | 7.892 | 7.046 | 8.103 | 7.558 | 7.001 | 6.578 | 7.333 | 7.812 | 7.142 | 6.795 | 7.586 | 7.926 | 7.207 | 6.897 | 7.687 |
| 6 | 132 | 10.736 | 10.557 | 9.334 | 10.790 | 9.754 | 9.023 | 8.490 | 9.458 | 10.191 | 9.266 | 8.864 | 9.928 | 10.405 | 9.386 | 9.056 | 10.125 |
| 7 | 132 | 8.997 | 10.056 | 7.798 | 9.820 | 6.518 | 5.886 | 5.658 | 6.421 | 7.471 | 6.365 | 6.480 | 7.089 | 8.003 | 6.627 | 6.962 | 7.601 |
| 8 | 132 | 7.624 | 7.643 | 6.634 | 7.693 | 7.237 | 7.033 | 6.302 | 7.150 | 7.416 | 7.143 | 6.455 | 7.341 | 7.500 | 7.196 | 6.530 | 7.417 |
| 9 | 33 | 16.394 | 16.375 | 14.238 | 16.584 | 16.089 | 16.163 | 13.979 | 16.400 | 16.228 | 16.252 | 14.097 | 16.471 | 16.296 | 16.297 | 14.157 | 16.522 |
| 10 | 33 | 19.694 | 18.351 | 17.084 | 19.398 | 19.330 | 18.103 | 16.774 | 19.190 | 19.511 | 18.203 | 16.927 | 19.293 | 19.589 | 18.248 | 16.996 | 19.354 |
| 11 | 11 | 23.234 | 27.710 | 20.239 | 26.372 | 23.091 | 27.580 | 20.118 | 26.276 | 23.155 | 27.637 | 20.171 | 26.309 | 23.187 | 27.668 | 20.200 | 26.334 |
| 12 | 33 | 16.357 | 15.223 | 14.199 | 16.098 | 16.167 | 15.104 | 14.038 | 15.984 | 16.262 | 15.156 | 14.118 | 16.041 | 16.302 | 15.179 | 14.153 | 16.073 |
| 13 | 11 | 25.693 | 31.013 | 22.334 | 29.967 | 25.565 | 30.893 | 22.226 | 29.872 | 25.627 | 30.950 | 22.278 | 29.911 | 25.654 | 30.978 | 22.302 | 29.934 |
| 14 | 33 | 8.307 | 7.742 | 7.198 | 8.096 | 8.259 | 7.711 | 7.157 | 8.067 | 8.286 | 7.727 | 7.180 | 8.086 | 8.295 | 7.732 | 7.188 | 8.094 |
| 15 | 33 | 13.239 | 12.048 | 11.476 | 12.810 | 13.109 | 11.953 | 11.365 | 12.730 | 13.180 | 11.992 | 11.425 | 12.777 | 13.206 | 12.006 | 11.448 | 12.800 |
| 16 | 33 | 10.335 | 9.787 | 8.957 | 10.182 | 10.254 | 9.733 | 8.888 | 10.134 | 10.296 | 9.758 | 8.924 | 10.160 | 10.313 | 9.768 | 8.939 | 10.174 |
| 17 | 33 | 13.582 | 12.636 | 11.773 | 13.284 | 13.426 | 12.533 | 11.641 | 13.194 | 13.507 | 12.578 | 11.709 | 13.243 | 13.539 | 12.596 | 11.737 | 13.270 |
| 18 | 33 | 8.727 | 8.020 | 7.561 | 8.431 | 8.674 | 7.983 | 7.515 | 8.400 | 8.704 | 7.999 | 7.541 | 8.420 | 8.714 | 8.005 | 7.550 | 8.429 |
| 19 | 33 | 9.228 | 8.360 | 7.994 | 8.883 | 9.168 | 8.320 | 7.944 | 8.813 | 9.201 | 8.337 | 7.972 | 8.845 | 9.213 | 8.344 | 7.982 | 8.855 |
| 20 | 33 | 9.587 | 8.820 | 8.306 | 9.271 | 9.517 | 8.772 | 8.247 | 9.230 | 9.555 | 8.793 | 8.279 | 9.255 | 9.569 | 8.801 | 8.291 | 9.267 |
| 21 | 33 | 15.720 | 14.324 | 13.626 | 15.199 | 15.476 | 14.141 | 13.418 | 15.057 | 15.607 | 14.211 | 13.529 | 15.139 | 15.657 | 14.239 | 13.573 | 15.181 |
| 22 | 33 | 15.273 | 14.039 | 13.238 | 14.843 | 15.025 | 13.844 | 13.026 | 14.699 | 15.160 | 13.918 | 13.141 | 14.784 | 15.210 | 13.947 | 13.185 | 14.827 |
| 23 | 33 | 8.577 | 8.030 | 7.430 | 8.351 | 8.493 | 7.947 | 7.358 | 8.300 | 8.542 | 7.975 | 7.400 | 8.333 | 8.558 | 7.985 | 7.414 | 8.347 |
| 24 | 33 | 11.257 | 10.421 | 9.752 | 10.916 | 10.996 | 10.127 | 9.528 | 10.698 | 11.148 | 10.211 | 9.658 | 10.793 | 11.200 | 10.240 | 9.704 | 10.840 |
| 25 | 33 | 7.830 | 7.723 | 6.782 | 7.807 | 7.258 | 6.925 | 6.288 | 7.310 | 7.571 | 7.105 | 6.558 | 7.488 | 7.696 | 7.179 | 6.668 | 7.598 |
| 26 | 33 | 3.177 | 3.007 | 2.752 | 3.158 | 3.092 | 2.888 | 2.678 | 3.018 | 3.144 | 2.918 | 2.723 | 3.071 | 3.161 | 2.927 | 2.738 | 3.084 |
| 27 | 33 | 11.044 | 11.502 | 9.567 | 11.322 | 9.151 | 8.688 | 7.930 | 9.535 | 10.065 | 9.165 | 8.720 | 10.010 | 10.514 | 9.412 | 9.118 | 10.390 |
| 28 | 132 | 5.850 | 5.606 | 5.076 | 5.789 | 5.527 | 5.152 | 4.800 | 5.372 | 5.668 | 5.232 | 4.919 | 5.520 | 5.743 | 5.276 | 4.987 | 5.589 |
| 29 | 33 | 15.380 | 19.040 | 13.310 | 18.586 | 6.498 | 5.111 | 5.629 | 6.713 | 9.316 | 8.533 | 8.065 | 8.377 | 11.392 | 6.343 | 9.950 | 10.375 |
| 30 | 33 | 6.208 | 5.987 | 5.376 | 6.274 | 5.037 | 4.116 | 4.363 | 4.851 | 5.579 | 4.337 | 4.832 | 5.170 | 5.863 | 4.452 | 5.084 | 5.420 |

Table D43: IEC Simulated Results for Case 6 at $\mathbf{8 5 \%}$ penetration level and DG located at Bus $\mathbf{2 6}$ and 30

| Bus |  | Wind |  |  |  | PV |  |  |  | Hybrid |  |  |  | Diesel Hybrid |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | kV | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG | 3-Ph | LG | LL | LLG |
| 1 | 132 | 10.585 | 12.827 | 9.322 | 12.108 | 10.564 | 12.807 | 9.304 | 12.085 | 10.576 | 12.818 | 9.314 | 12.101 | 10.581 | 12.823 | 9.318 | 12.105 |
| 2 | 132 | 10.124 | 10.999 | 8.850 | 10.682 | 10.090 | 10.973 | 8.821 | 10.646 | 10.108 | 10.988 | 8.837 | 10.669 | 10.116 | 10.994 | 8.843 | 10.676 |
| 3 | 132 | 6.201 | 6.093 | 5.389 | 6.201 | 6.172 | 6.074 | 5.364 | 6.170 | 6.187 | 6.084 | 5.377 | 6.189 | 6.194 | 6.088 | 5.383 | 6.195 |
| 4 | 132 | 8.282 | 7.829 | 7.201 | 8.197 | 8.218 | 7.791 | 7.147 | 8.128 | 8.250 | 7.810 | 7.173 | 8.169 | 8.266 | 7.819 | 7.187 | 8.183 |
| 5 | 132 | 7.519 | 6.979 | 6.542 | 7.364 | 7.507 | 6.972 | 6.531 | 7.352 | 7.514 | 6.976 | 6.538 | 7.360 | 7.517 | 6.978 | 6.540 | 7.362 |
| 6 | 132 | 9.808 | 9.055 | 8.533 | 9.629 | 9.686 | 8.985 | 8.428 | 9.491 | 9.740 | 9.016 | 8.474 | 9.570 | 9.773 | 9.035 | 8.504 | 9.599 |
| 7 | 132 | 6.192 | 5.699 | 5.372 | 6.039 | 6.166 | 5.685 | 5.350 | 6.012 | 6.179 | 5.692 | 5.362 | 6.029 | 6.185 | 5.696 | 5.367 | 6.034 |
| 8 | 132 | 7.287 | 7.064 | 6.343 | 7.244 | 7.223 | 7.024 | 6.289 | 7.173 | 7.252 | 7.042 | 6.313 | 7.215 | 7.269 | 7.053 | 6.328 | 7.230 |
| 9 | 33 | 16.197 | 16.284 | 14.071 | 16.443 | 16.090 | 16.162 | 13.979 | 16.389 | 16.146 | 16.198 | 14.027 | 16.412 | 16.172 | 16.216 | 14.050 | 16.434 |
| 10 | 33 | 19.607 | 18.413 | 17.011 | 19.353 | 19.379 | 18.132 | 16.816 | 19.249 | 19.516 | 18.208 | 16.933 | 19.327 | 19.563 | 18.236 | 16.974 | 19.371 |
| 11 | 11 | 23.141 | 27.625 | 20.160 | 26.303 | 23.090 | 27.579 | 20.117 | 26.270 | 23.116 | 27.602 | 20.138 | 26.280 | 23.128 | 27.614 | 20.149 | 26.291 |
| 12 | 33 | 16.271 | 15.215 | 14.127 | 16.030 | 16.178 | 15.110 | 14.047 | 15.995 | 16.235 | 15.142 | 14.096 | 16.029 | 16.254 | 15.153 | 14.112 | 16.046 |
| 13 | 11 | 25.636 | 30.961 | 22.287 | 29.929 | 25.573 | 30.901 | 22.233 | 29.881 | 25.610 | 30.935 | 22.264 | 29.903 | 25.623 | 30.949 | 22.276 | 29.916 |
| 14 | 33 | 8.292 | 7.747 | 7.186 | 8.080 | 8.263 | 7.714 | 7.161 | 8.073 | 8.284 | 7.726 | 7.178 | 8.088 | 8.288 | 7.728 | 7.182 | 8.093 |
| 15 | 33 | 13.241 | 12.105 | 11.478 | 12.816 | 13.145 | 11.974 | 11.396 | 12.772 | 13.205 | 12.006 | 11.447 | 12.808 | 13.224 | 12.016 | 11.464 | 12.825 |
| 16 | 33 | 10.304 | 9.790 | 8.931 | 10.155 | 10.260 | 9.737 | 8.894 | 10.141 | 10.289 | 9.753 | 8.918 | 10.159 | 10.297 | 9.758 | 8.925 | 10.167 |
| 17 | 33 | 13.535 | 12.654 | 11.734 | 13.248 | 13.442 | 12.542 | 11.654 | 13.214 | 13.501 | 12.575 | 11.704 | 13.250 | 13.519 | 12.586 | 11.720 | 13.267 |
| 18 | 33 | 8.720 | 8.038 | 7.555 | 8.423 | 8.684 | 7.988 | 7.524 | 8.412 | 8.708 | 8.002 | 7.544 | 8.427 | 8.715 | 8.005 | 7.550 | 8.434 |
| 19 | 33 | 9.216 | 8.376 | 7.985 | 8.891 | 9.177 | 8.324 | 7.951 | 8.816 | 9.203 | 8.338 | 7.973 | 8.842 | 9.210 | 8.342 | 7.979 | 8.847 |
| 20 | 33 | 9.571 | 8.835 | 8.293 | 9.256 | 9.526 | 8.777 | 8.254 | 9.242 | 9.556 | 8.794 | 8.280 | 9.261 | 9.564 | 8.799 | 8.287 | 9.269 |
| 21 | 33 | 15.763 | 14.466 | 13.665 | 15.255 | 15.555 | 14.186 | 13.486 | 15.153 | 15.683 | 14.254 | 13.596 | 15.229 | 15.725 | 14.278 | 13.633 | 15.268 |
| 22 | 33 | 15.353 | 14.217 | 13.308 | 14.937 | 15.124 | 13.901 | 13.111 | 14.817 | 15.264 | 13.978 | 13.232 | 14.900 | 15.310 | 14.004 | 13.272 | 14.943 |
| 23 | 33 | 8.658 | 8.150 | 7.501 | 8.436 | 8.557 | 7.985 | 7.414 | 8.374 | 8.617 | 8.019 | 7.466 | 8.407 | 8.639 | 8.032 | 7.484 | 8.427 |
| 24 | 33 | 11.764 | 11.017 | 10.191 | 11.480 | 11.333 | 10.318 | 9.819 | 11.069 | 11.571 | 10.444 | 10.024 | 11.188 | 11.670 | 10.499 | 10.111 | 11.275 |
| 25 | 33 | 10.358 | 10.609 | 8.971 | 10.564 | 8.590 | 7.725 | 7.442 | 8.750 | 9.415 | 8.101 | 8.155 | 9.118 | 9.864 | 8.322 | 8.553 | 9.499 |
| 26 | 33 | 14.350 | 17.910 | 12.418 | 17.543 | 5.899 | 4.248 | 5.109 | 5.965 | 8.336 | 4.753 | 7.216 | 7.569 | 10.380 | 5.176 | 9.075 | 9.551 |
| 27 | 33 | 11.364 | 11.949 | 9.845 | 11.722 | 9.425 | 8.868 | 8.167 | 9.585 | 10.385 | 9.346 | 8.997 | 10.349 | 10.848 | 9.596 | 9.407 | 10.749 |
| 28 | 132 | 5.646 | 5.220 | 4.901 | 5.511 | 5.545 | 5.162 | 4.814 | 5.389 | 5.581 | 5.183 | 4.845 | 5.453 | 5.612 | 5.201 | 4.872 | 5.482 |
| 29 | 33 | 5.979 | 6.101 | 5.178 | 6.120 | 4.841 | 4.230 | 4.193 | 4.837 | 5.373 | 4.467 | 4.653 | 5.098 | 5.648 | 4.593 | 4.897 | 5.324 |
| 30 | 33 | 15.717 | 19.363 | 13.601 | 18.869 | 6.694 | 4.885 | 5.798 | 6.737 | 9.620 | 5.544 | 8.328 | 8.628 | 11.717 | 5.982 | 10.231 | 10.635 |

